

$B_s^0 B_s^0$ Mixing

- $\Delta m_s / \Delta m_d \Rightarrow |V_{ts} / V_{td}|$ with less theory uncertainty.
- If SM fits are correct, it should be just around the corner:

$$15.4 < \Delta m_s < 20.3 \text{ ps}^{-1}.$$

- Experimental challenge: seeing very rapid oscillations.

Need $p(B_s^0)$ of each event to get proper time.

Difficult if missing particles exist, e.g. $\bar{B}_s^0 \rightarrow \ell^- \bar{\nu} D_s^+ X$.

Want full reconstruction $\bar{B}_s^0 \rightarrow D_s^+ \pi^-$, $D_s^+ \pi^+ \pi^- \pi^-$.

- Employ impact parameter track trigger (SVT) at level-2.

Resolution $\sim 40 \mu\text{m}$ for $p_T > 2 \text{ GeV}/c$.

- Expect 5000 to 30000 $\bar{B}_s^0 \rightarrow D_s^+ (n\pi)^-$ decays in 2 fb^{-1} .

S/B : 1/2 to 2.

$\sigma_t = 45 \oplus (\sigma_p/p) t$ fs ($\sim 14 \mu\text{m}$).

Flavor tagging: $\epsilon D^2 = 11\%$.

Can observe Δm_s up to 40 ps^{-1} as a $> 5\text{-}\sigma$ effect.

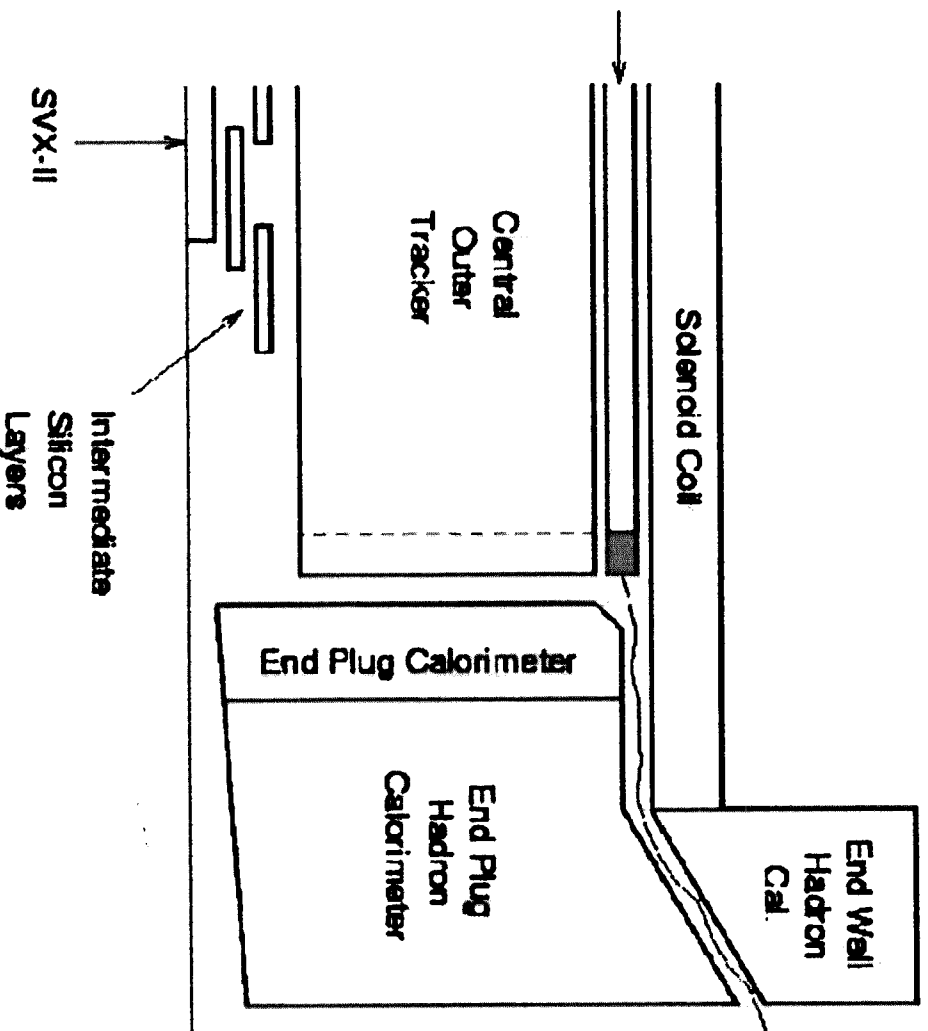
Once seen, Δm_s will be measured to a few %.

$\Rightarrow |V_{td}/V_{ts}|$ also determined to a few %.

New additions for B physics:

Time-of-flight counter
Innermost Si layer

CDF-II TOF counter



Detector

- Located at $r = 1.4$ m
- Inside 1.4 Tesla solenoid
- Scintillator Bicron BC408
4 x 4 x 270 cm³ 216本
- Hamamatsu R7761 PMTs
38 mm, 19-stage fine mesh
- Goal: $\sigma_T \sim 100$ ps

Purpose

- 2σ K/π separation
up to 1.6 GeV/c
- B flavor tagging

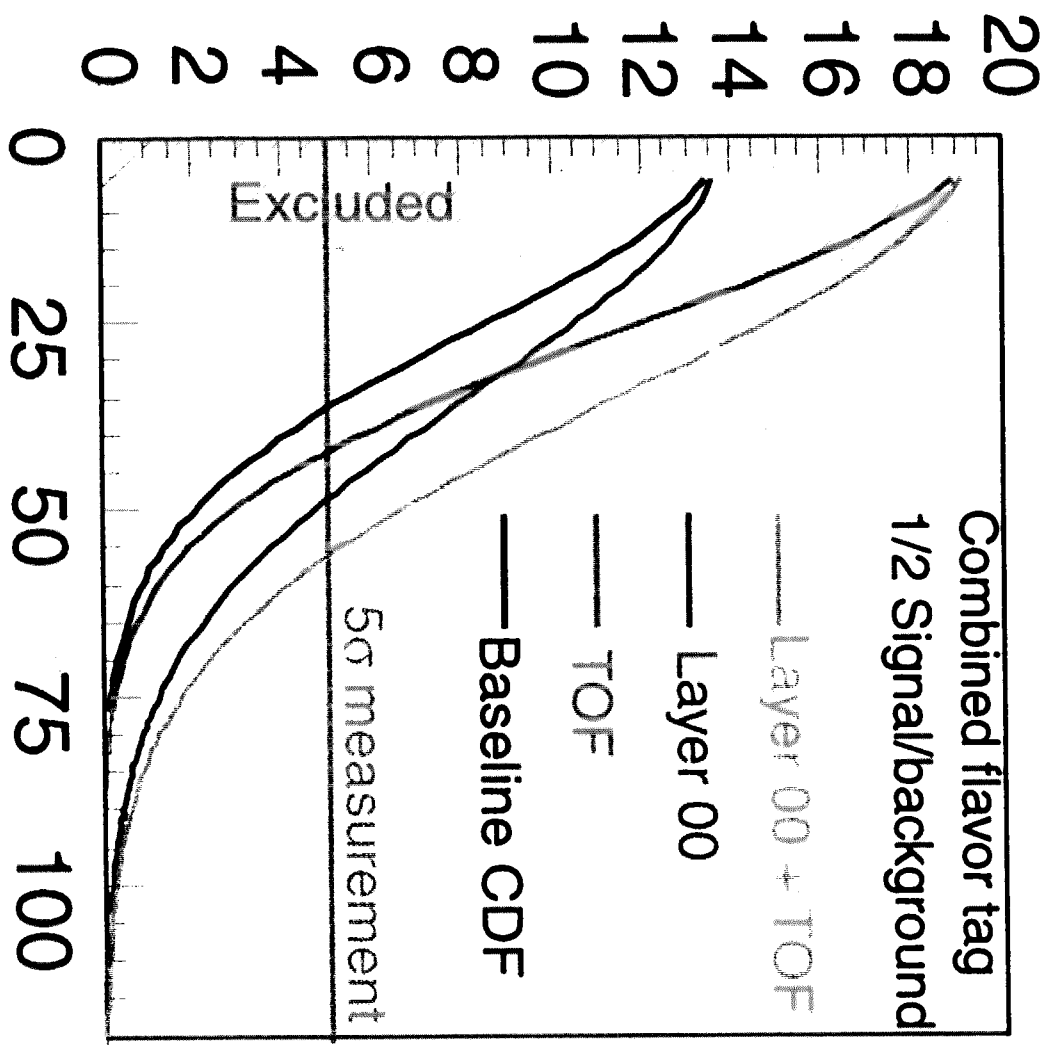
Impact of TOF and Layer 00 on B^0_s mixing

Signal

- $B^0_s \rightarrow D^-_s \pi^+, D^-_s \pi^+ \pi^- \pi^-$
 - ~ 20 k events / 2 fb^{-1}
- ## TOF
- Improves flavor tags.
 - Helps at lower x_s .
- ## Layer 00
- Improves vertex determination.
- proper time resolution.
- Helps at higher x_s .

Significance (σ)

Once the oscillations are established, Δm_s will be determined to a few %.



$B^0_s \leftrightarrow \bar{B}^0_s$ frequency $x_s = \Delta m_s \tau$

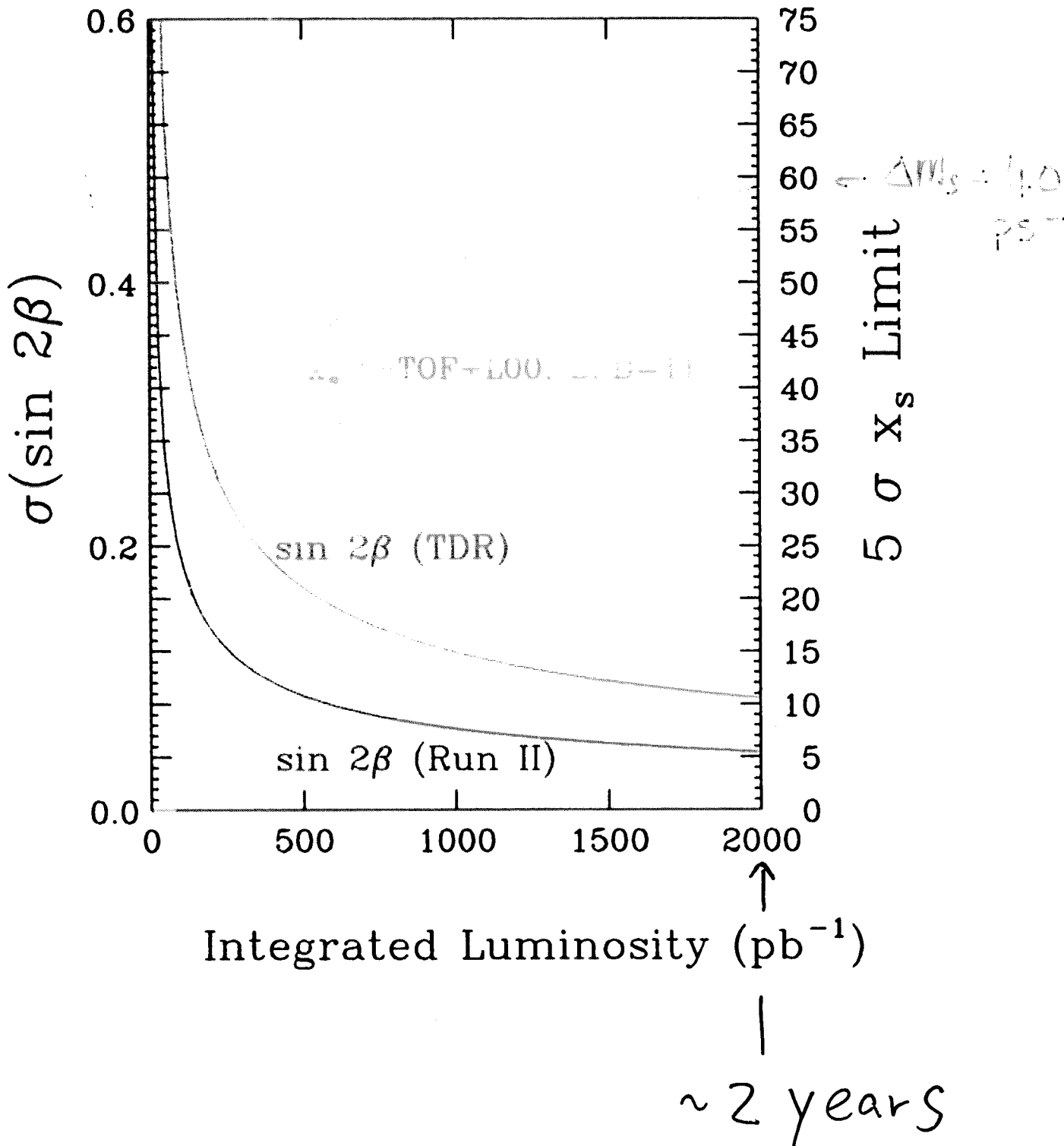
($\tau = 1.5 \text{ ps}$)

Run II projections

$\sin 2\beta$ precision from $J/\psi K^0_S$ (2 fb^{-1})

TDR: 10 k signal, $\epsilon D^2 = 6.7\% \rightarrow \pm 0.084$

New: 28 k signal, $\epsilon D^2 = 9.1\% \rightarrow \pm 0.043$



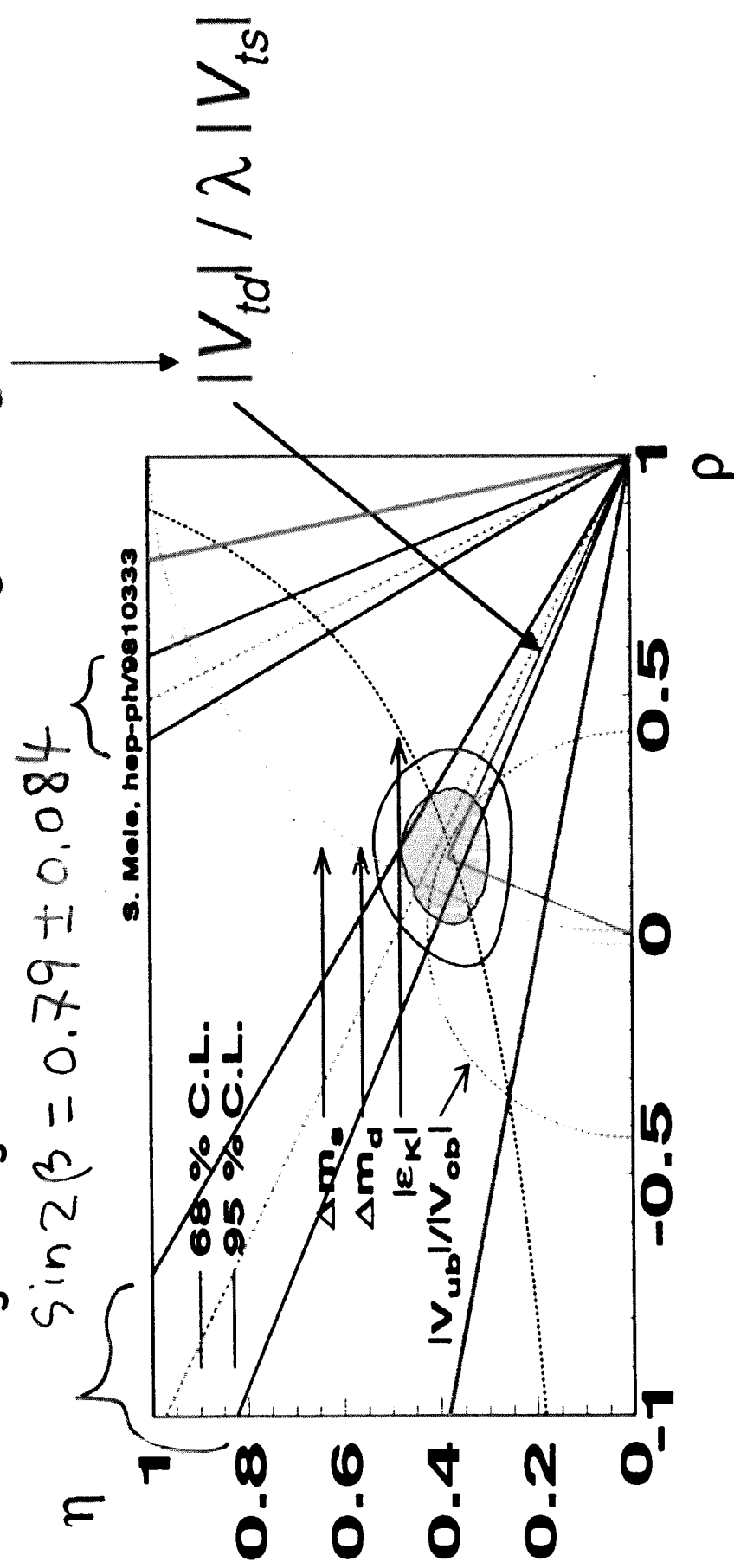
B Physics in CDF Run II

Two Major Goals:

I. Precision $\sin(2\beta)$ from $B^0/\bar{B}^0 \rightarrow J/\psi K^0_S$

II. $B^0_S - \bar{B}^0_S$ Oscillation $\rightarrow \Delta m_S / \Delta m_D$

$$\sin 2\beta = 0.79 \pm 0.084$$



Can be the first meaningful test of the unitarity triangle.

Run II (cont'd) Probing angle γ (phase of V_{ub})

- $B^0 \rightarrow \pi^+ \pi^-$ once thought to be the mode for $\sin 2(\pi - \gamma - \beta)$.
(assuming $b \rightarrow u$ tree dominance over penguin)
- CLEO finds much larger $K^+ \pi^-$ and tiny $\pi^+ \pi^-$.
- Not just small rates, but also means penguin pollution.
→ Relation to $\sin(2\alpha)$ less clear.
- Strategies proposed, but are challenging experimentally...

New approach : R. Fleischer, Phys. Lett. B 459, 306 (1999).

Throw in $B^0_s \rightarrow K^+ K^-$, measure asymmetries in both B^0 and B^0_s .

In general, for a decay $B^0 \rightarrow f$ ($f = \text{CP eigenstate}$):

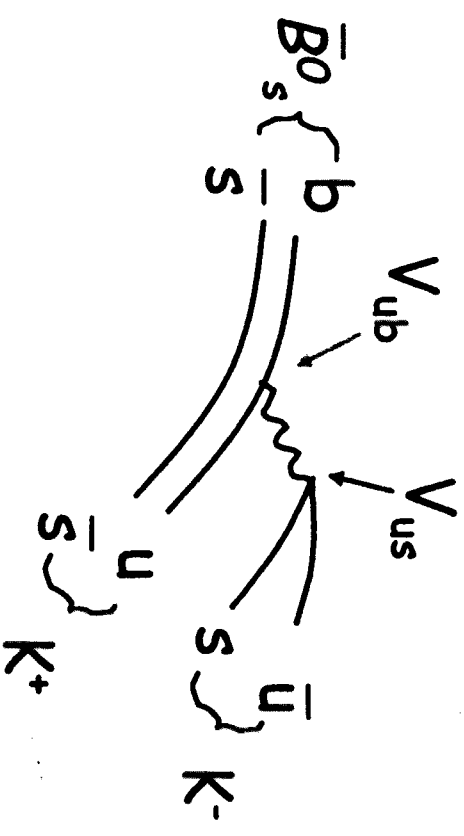
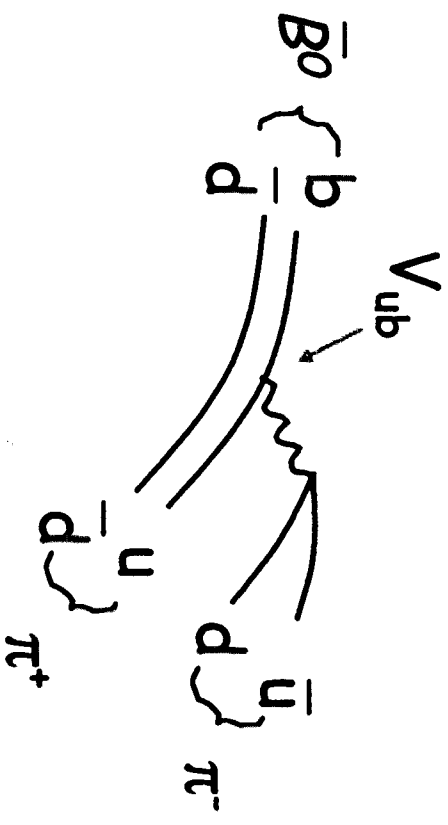
$$A_{\text{CP}}(t) = A^{\text{dir}} \cos(\Delta m t) + A^{\text{mix}} \sin(\Delta m t).$$

A^{dir} : "direct" CP violation, A^{mix} : CP violation thru mixing.

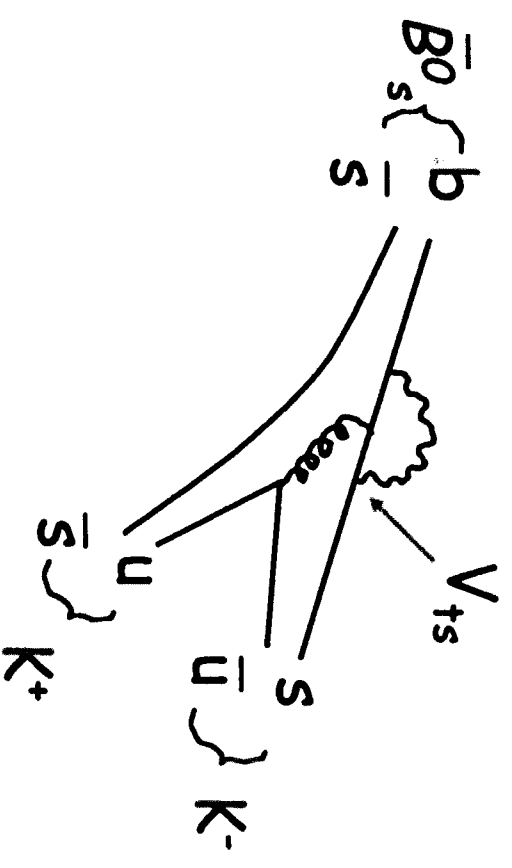
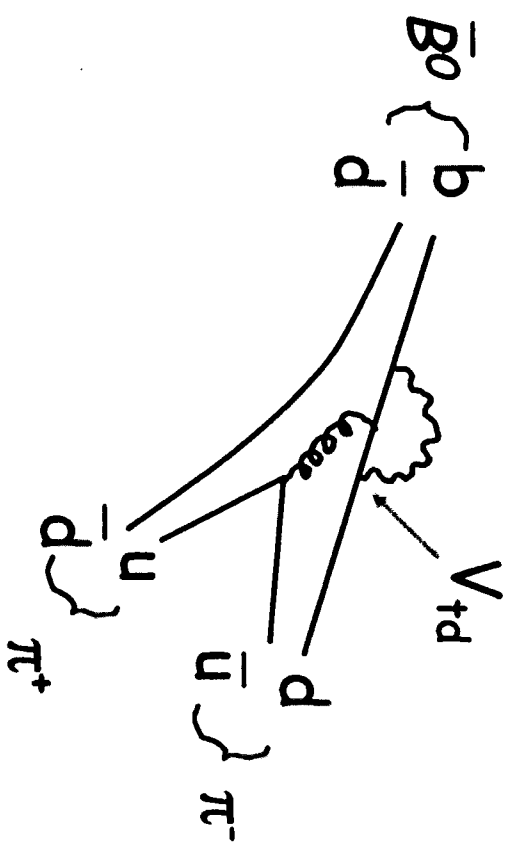
Experimentally, measure 4 A 's from $B^0 \rightarrow \pi^+ \pi^-$ and $B^0_s \rightarrow K^+ K^-$.

Then extract β , γ and penguin and tree decay amplitudes.

Tree



Penguin



Angle γ (phase of V_{ub}) continued

Four CP asymmetries to measure. ($\lambda = \sin \theta_c$)

- $A^{\text{dir}}(B^0 \rightarrow \pi^+ \pi^-) = -2d \sin \theta \sin \gamma / (1 - 2d \cos \theta \cos \gamma + d^2)$
- $A^{\text{mix}}(B^0 \rightarrow \pi^+ \pi^-) = [\sin 2(\beta + \gamma) - 2d \cos \theta \sin(2\beta + \gamma) + d^2 \sin 2\beta] / [1 - 2d \cos \theta \cos \gamma + d^2]$
- $A^{\text{dir}}(B^0_s \rightarrow K^+ K^-) \sim 2(\lambda^2/d) \sin \theta \sin \gamma$
- $A^{\text{mix}}(B^0_s \rightarrow K^+ K^-) \sim 2(\lambda^2/d) \cos \theta \sin \gamma$

Four unknowns to extract:

- β, γ = angles of the unitarity triangle.
- d = ratio of penguin (P) to tree (T) decay amplitudes,
 θ = phase of " P/T "
 $d e^{i\theta} \equiv \lambda |V_{cb}/V_{ub}| / (1 - \lambda^2/2) [P / (T+P)]$

If no penguin,
 $A^{\text{dir}} = 0$ (B^0, B^0_s)
 $A^{\text{mix}} = \sin 2(\beta + \gamma)$ (B^0)
 $A^{\text{mix}} = \sin(2\gamma)$ (B^0_s)

Expect ~ 5 k $B^0 \rightarrow \pi^+ \pi^-$, ~ 10 k $B^0_s \rightarrow K^+ K^-$

\rightarrow angle γ to $\sim 10^\circ$.

$B_{(s)}^U \rightarrow \pi\pi, \pi K, KK$ samples

- Problem: we measure $\mathcal{A}_{dir}, \mathcal{A}_{mix}$ for time dependence $x_d = 0.7, x_s = 26$
- Observed asymmetries are diluted by:

$$\mathcal{A}_{obs} = \mathcal{A}_{\pi^+\pi^-} \times f_{\pi\pi}$$

$$\mathcal{A}_{obs} = \mathcal{A}_{K^+K^-} \times f_{KK},$$

$f_{\pi\pi}, f_{KK}$ = respective fractions in mass window

- First determine signal rates *before* flavor tagging

Use dEdx with Mass \Rightarrow

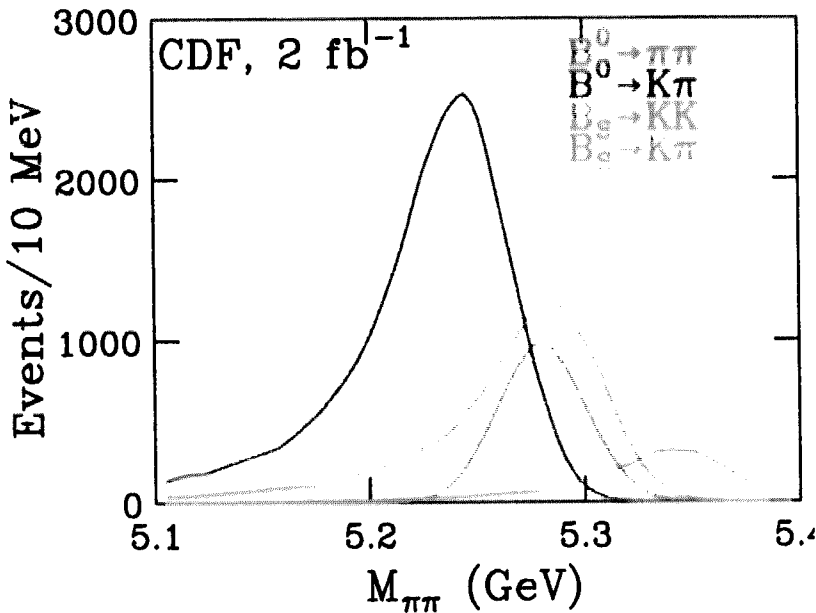
\Rightarrow Fitted errors on $f_{\pi\pi}, f_{KK}, f_{K\pi} \sim 1 \div 4\%$ on each signal

Higher math $\Rightarrow 1\sigma$ dEdx separation on $K\pi$ gives

$\times 2.3$ larger error on f_{π} than perfect separation . still just a few %

$f_{\pi\pi}, f_{KK}$ are same for tagged/untagged samples

\Rightarrow negligible errors on measured \mathcal{A}_{CP}



- Nominal BR's. $\sigma(B^0), \sigma(B_s^0)$
 - 20000 $B^0 \rightarrow K^+\pi^-$
 - 10000 $B_s^0 \rightarrow K^+K^-$
 - 5000 $B^0 \rightarrow \pi^+\pi^-$
 - 2500 $B_s^0 \rightarrow K^-\pi^+$
- Also QCD combinatorics (flat)
 - $B^0 + B_s^0$: QCD $\sim 1:1$

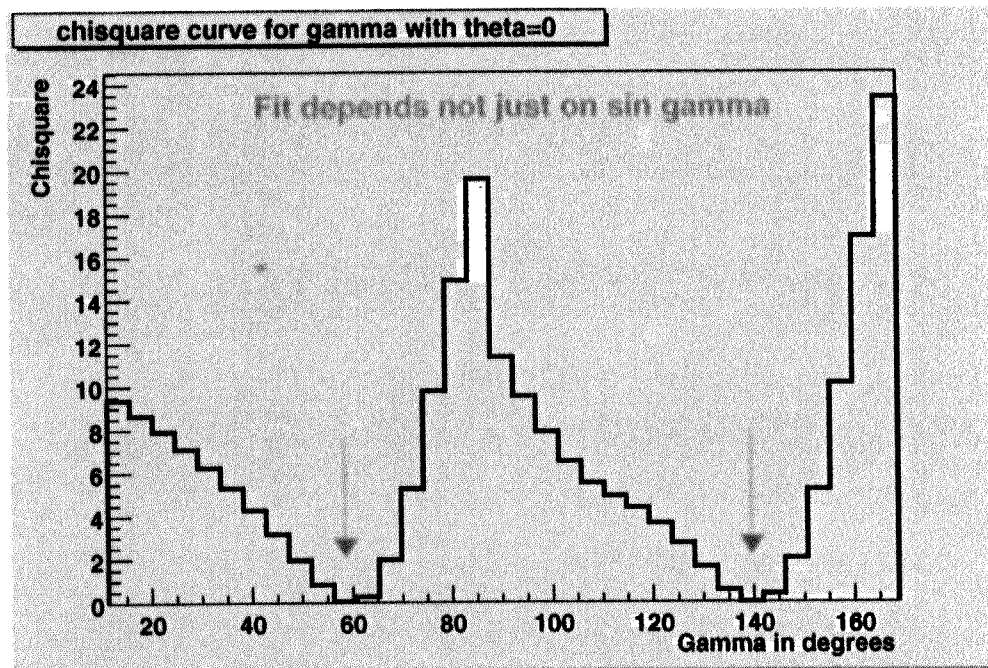
Measuring γ — the Result

Experimental Errors for “nominal assumptions”:

$$\sigma_{ACP} \sim 0.08 \text{ for } B_s \rightarrow K^+ K^-$$

$$\sigma_{ACP} \sim 0.11 \text{ for } B_d \rightarrow \pi^+ \pi^-$$

χ^2 fit for σ_γ

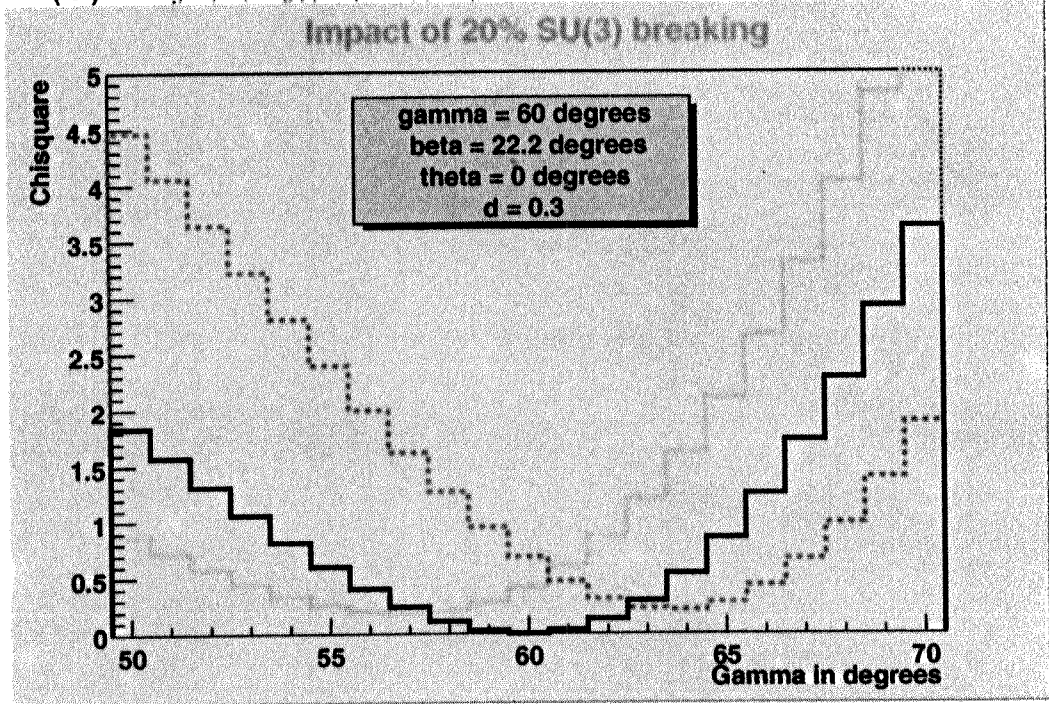


$$\sigma_\gamma = \frac{0.4}{6.8} \pm 3 \text{ degrees}$$

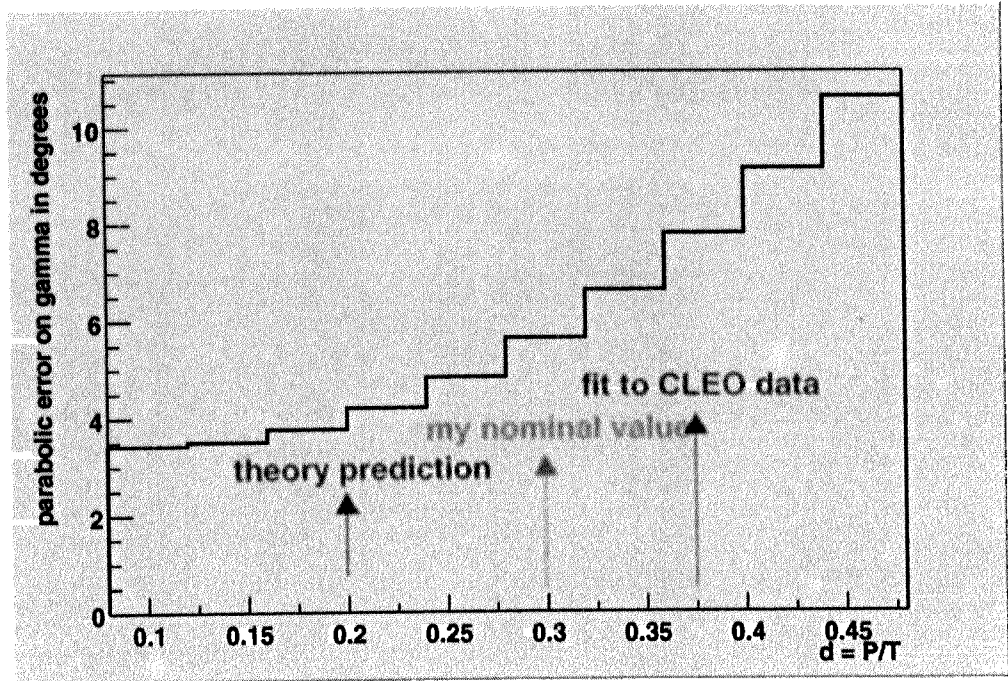
Systematic Error due to SU(3) breaking of 20%:
 $\sim 1/2$ the expected experimental error !!!

Stability of Errors on γ

(1) Vary $|d(B_s)/d(B^0)|$ by 20%, $\theta(B_s) - \theta(B^0)$ by $\pm 10^\circ$



(2) Vary central value of $|d|$ used in fits



Other Topics

- Search for CP -violation in $B_s^0/\bar{B}_s^0 \rightarrow J/\psi\phi$
 A_{CP} to $\sim \pm 0.1$. Expect ~ 0 in SM, new physics if substantial.
- Width difference $\Delta\Gamma$ in $B_s^0\bar{B}_s^0$ system
Potential for CP studies with untagged B_s^0 decays.
 $\sigma(\Delta\Gamma/\Gamma) \simeq 0.024$ from $J/\psi\phi$ vs. $D_s^+\pi^-$.
Also, direct check with $D_s^{(*)+}D_s^{(*)-}$.
- Rare decays:
 $B \rightarrow \mu^+\mu^-K^{(*)}$, ~ 60 events in 2 fb^{-1} .
Need more data for forward/backward asymmetry.
Also $(B^0 \rightarrow K^{*0}\gamma) / (B^0 \rightarrow \rho^0\gamma)$
and $(B_s^0 \rightarrow \phi\gamma) / (B_s^0 \rightarrow K^{*0}\gamma) \Rightarrow |V_{ts}/V_{td}|$.
- Angle γ from $B_s^0 \rightarrow D_s^\mp K^\pm$?
Theoretically clean, but BG from $D_s^-\pi^+$ tough.
Hope to see signal in 2 fb^{-1} .
- Precision lifetime ratios : B_s^0/B^0 , B_c^+/B^0 , Λ_b/B^0
- Full reconstruction of $B_c^+ \rightarrow J/\psi\pi^+$, $B_s^0\pi^+$...
- QCD b and c production, onium polarization.

Much of them pretty complementary to $\Upsilon(4S)$.

Lifetime Difference, $\frac{\Delta\Gamma}{\Gamma}$

- Full Mass and Decay Matrix

$$H_{eff} = \begin{pmatrix} M & M_{12} \\ M_{12}^* & M \end{pmatrix} - \frac{i}{2} \begin{pmatrix} \Gamma & \Gamma_{12} \\ \Gamma_{12}^* & \Gamma \end{pmatrix}$$

- Eigenstates have masses $M \pm \frac{\Delta M}{2}$, widths $\Gamma \pm \frac{\Delta\Gamma}{2}$
 M_{12} due to virtual intermediate states (tt)
 Γ_{12} due to real intermediate states ($D\bar{D}$)
 $\Delta\Gamma = 2 \cos \Delta\Phi |\Gamma_{12}|$ ($\Delta\Phi = \arg[M_{12}^* \Gamma_{12}]$)
 CP impurity in eigenstates, $\Re(\epsilon) = \sin \Delta\Phi \left| \frac{\Gamma_{12}}{4M_{12}} \right|$

- For K_L K_S system

$\Delta\Gamma \simeq 100\%$ due to common $K \rightarrow 2\pi$ intermediate state
 Also, phase difference is large, so $\Re(\epsilon)$ is "large"

- In B^0 and B_s^0 systems

$\Delta\Gamma$ small (random mix of intermediate states)

$\Delta\Phi$ is small- $6.4^\circ (B^0)$, $-0.2^\circ (B_s)$ by CKM unitarity,
 so $\Re(\epsilon) \simeq 2 \cdot 10^{-4} (B^0)$, $5 \cdot 10^{-6} (B_s)$

- For B^0 , B_s^0 mesons, we have

$$B_s^0, \quad b \rightarrow s \rightarrow ccs - s \sim 1$$

$$B_d^0, \quad b \rightarrow d \rightarrow ccd + d \sim \sin^2 \theta_c$$

$$\frac{\Delta\Gamma}{\Gamma}(B^0) = 15 \pm 5\% \text{ (Hashimoto, '99)}$$

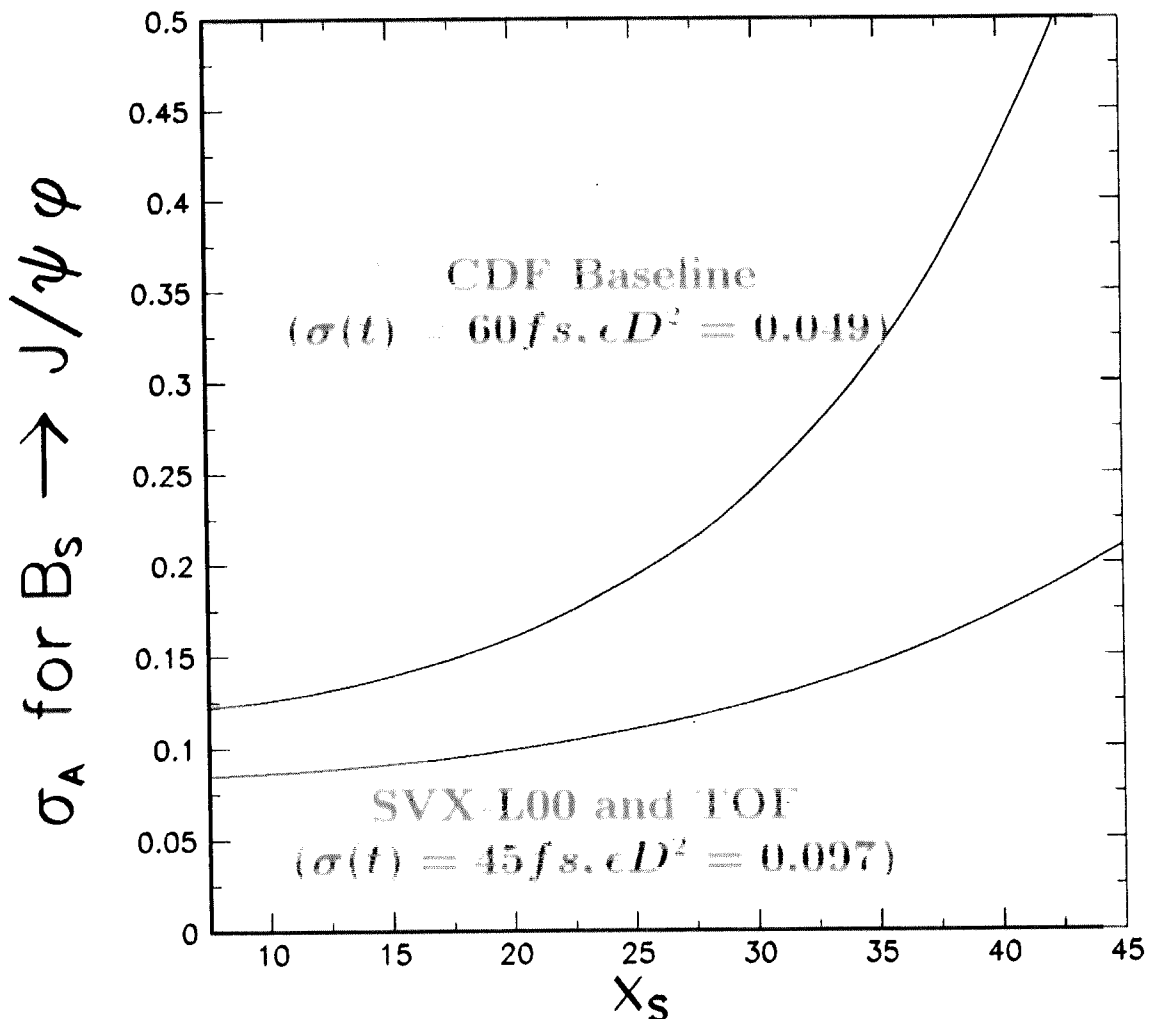
$$\frac{\Delta\Gamma}{\Gamma}(B_d^0) \lesssim 1\%$$

$$\text{Numerically, } \frac{\Delta\Gamma}{\Delta M} \simeq (5.6 \pm 2.6) 10^{-3}$$

Conclusion: $\Delta\Gamma(B_s^0)$ should be detectable ($\sim 15\%$)
 but $\Delta\Gamma(B_d^0)$, also $\Re(\epsilon)$, probably not

CP Violation in $B_s^0/\overline{B}_s^0 \rightarrow J/\psi\phi$

- Expect $\sim 6000 B_s^0/\overline{B}_s^0 \rightarrow J/\psi\phi$ events in 2 fb^{-1} (CDF)
- Expect small asymmetry: $\text{Arg}[M_{12}(B_s^0)] \sim -2^\circ$ in S.M.
- Assumes prior determination of ΔM_s
- CP asymmetry ($\text{Arg}[M_{12}(B_s^0)]$)
 \Rightarrow input to determination of γ via $B^0 \rightarrow \pi^+\pi^-$, $B_s^0 \rightarrow K^+K^-$



Measurements of $\Delta\Gamma(B_s)$

Ignore CP violation in B_s mixing (negligible in S.M.)

$\Rightarrow B_{sH}, B_{sL}$ are (heavy, light) $CP = \pm 1$ eigenstates

[1]Decays $B_s \rightarrow D_s^- \ell^+ \nu$ are 50:50 mix of B_{sH}, B_{sL}

Fit to $(\exp^{-\Gamma_L t} + \exp^{-\Gamma_H t})$

Not very sensitive:

[2]Isolate $CP = +1$ B_{sL} decays with modes

$B_{sL}^0 \rightarrow J/\psi\phi, B_{sL}^0 \rightarrow D_s^{+(*)}D^{-(*)}, J/\psi\eta\dots$

$\Rightarrow \Delta\Gamma_s = 2[\bar{\Gamma} - \Gamma(B_{sL})], \bar{\Gamma} = \Gamma(B_s^0)$ from $B_s \rightarrow D_s\pi$

[3]Directly evaluate the Γ_{12} term in the mixing matrix

$\Gamma_{12} \sim [\sum_f A(B_s^0 \rightarrow f)A^*(\bar{B}_s^0 \rightarrow f)]$

Final state $f = D_s^{-(*)}D_s^{+(*)}$ should dominate sum

Direct measurement of $|\Gamma_{12}|$ if sample pure $CP = +1$

CERN-EP-2000-096 (lepbose.web.cern.ch/LEPBOSC/)

R. Aleksan *et al.*, Phys. Lett. B316 (1993) 567

[4]New Physics Scenarios

New physics possible in M_{12} , not Γ_{12}

Large $\Delta\Phi \Rightarrow \Delta\Gamma$ "too small"

Any anomalous phase in M_{12} will show up in $B_s \rightarrow J/\psi\phi$ CP asymmetry

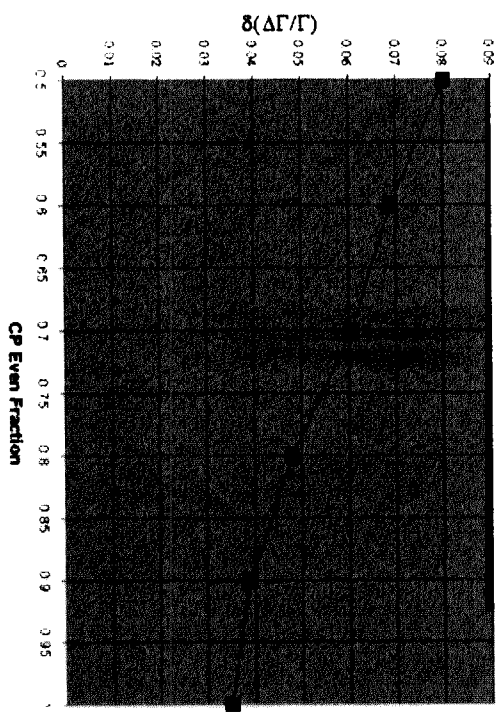
Measured $|\Gamma_{12}| \gg \Delta\Gamma/2$

$\Delta M_s \gg$ Standard model, $\Delta\Gamma$ "normal"

i.e. Phase of M_{12} OK, but not magnitude

CDF Run II $\Delta\Gamma(B_s)$ Projections

$\delta(\Delta\Gamma/\Gamma)$ as a function of CP Even fraction in $B_s \rightarrow J/\psi \phi$



$\delta(\Delta\Gamma/\Gamma) = \frac{\delta(\text{CP Even Fraction})}{\text{CP Even Fraction}}$
 $\delta(\text{CP Even Fraction}) = \frac{\delta(\text{CP Odd Fraction})}{\text{CP Even Fraction}}$

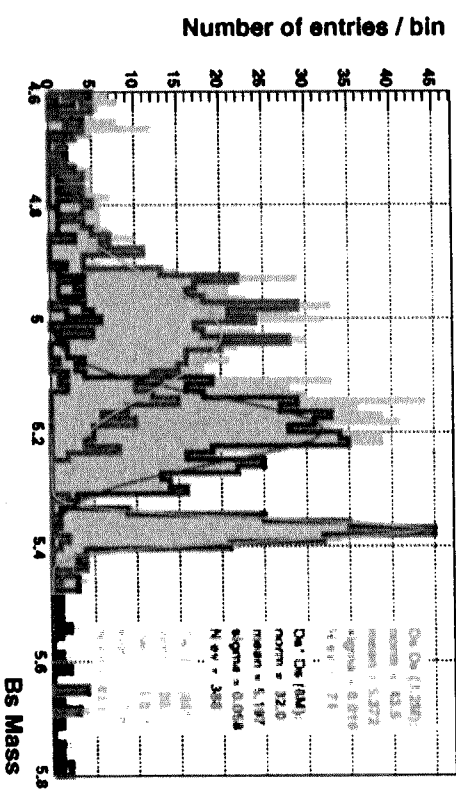
Angular distribution \Rightarrow

$CP = +1$ $J/\psi\phi$ fraction

Run I: $83 \pm 19\%$ ($J/\psi\phi$)

Run I: $87 \pm 13\%$ ($J/\psi K^{*0}$)

$\delta(\text{CP Even Fraction}) = \frac{\delta(\text{CP Odd Fraction})}{\text{CP Even Fraction}}$
 $\delta(\text{CP Even Fraction}) = \frac{\delta(\text{CP Odd Fraction})}{1 - \text{CP Even Fraction}}$



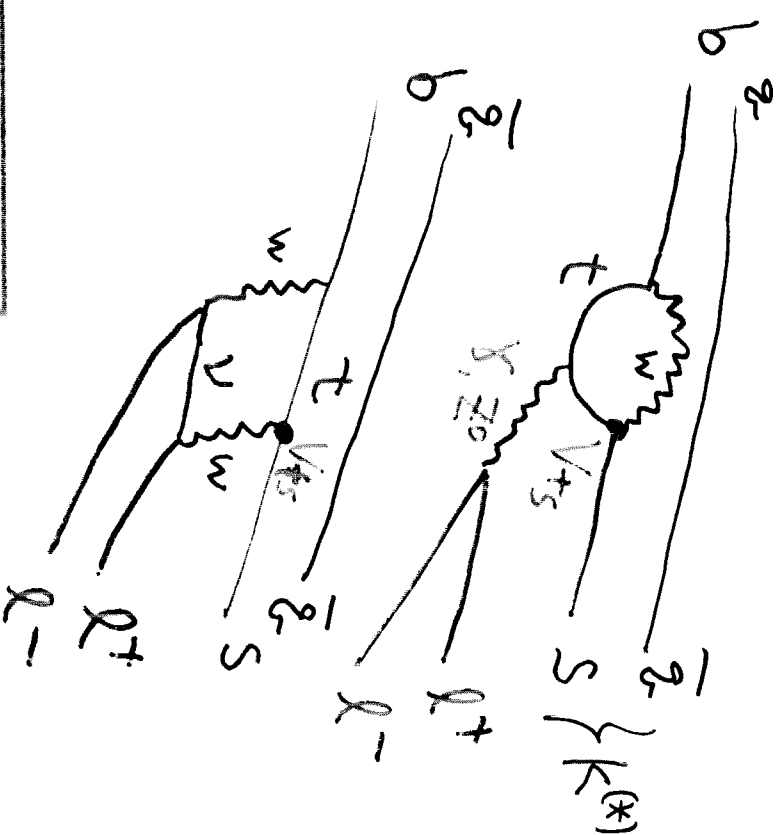
PYTHIA simulation of signal
 $B_s \rightarrow J/\psi\phi$
 $B_s \rightarrow J/\psi K^{*0}$
 $B_s \rightarrow J/\psi\psi(2S)$

\Rightarrow Direct check of $|\Gamma_{12}(B_s)|$

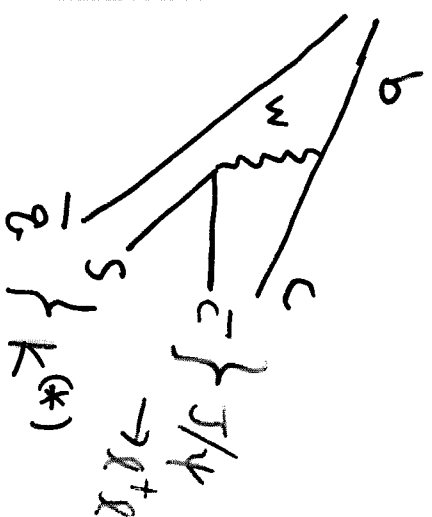
Rare Decays $B \rightarrow K^{(*)} l^+ l^-$

- $b \rightarrow s$ FCNC transition
- Z^0 penguin and box diagram in addition to EM penguin.
- $|V_{ts}|$
- SM predicts B.R. $\sim 10^{-7}$ to 10^{-6} .
- New physics could enhance it.
- Has yet to be observed.

PRL 83, 3378 (1999)

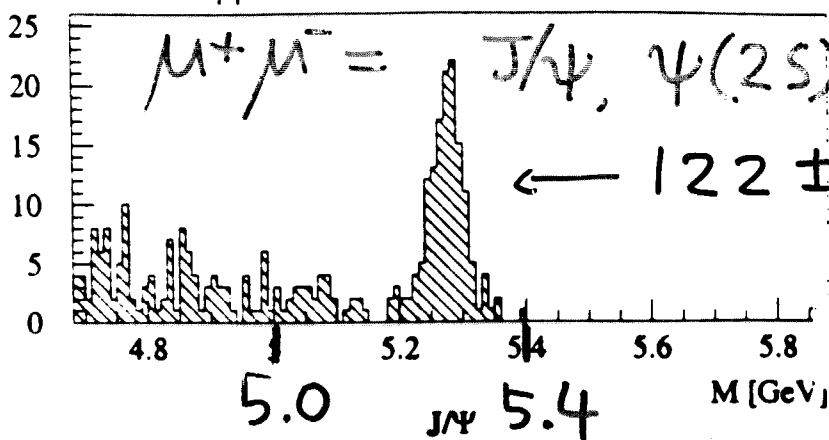


$l^+ l^-$ can be resonant, e.g. $J/\psi, \psi(2S)$.
 \rightarrow Indistinguishable from $b \rightarrow c\bar{c}s$
 Look at non-resonant mass region.



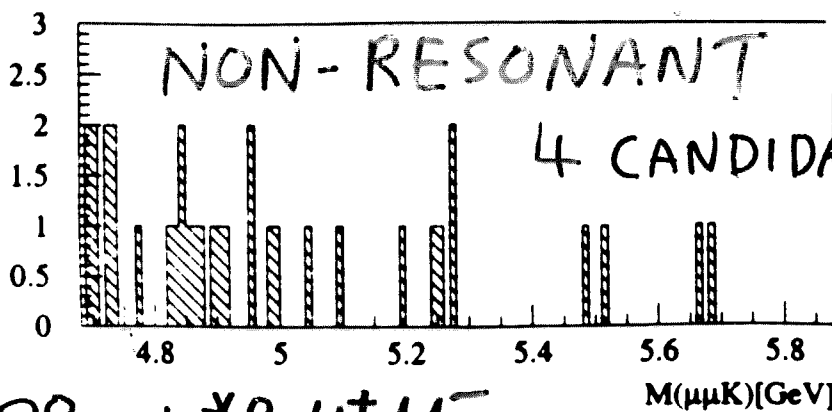
$B^+ \rightarrow K^+ \mu^+ \mu^-$
 $\mu\mu K$ Run I CDF PRELIMINARY

110 pb⁻¹



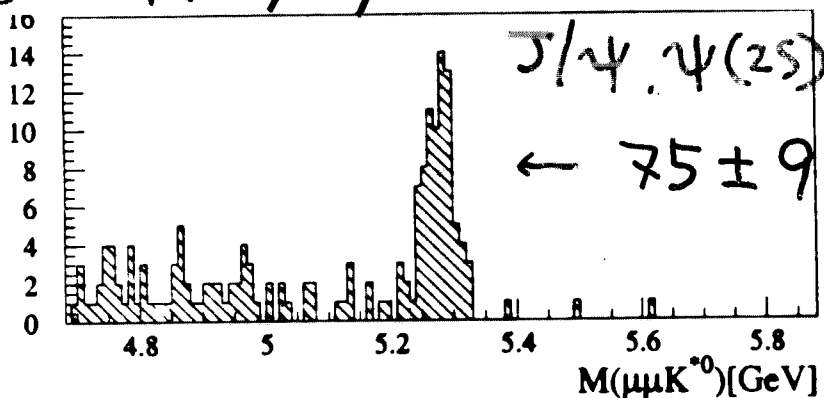
1999
 SIGNAL
 FOR NORMALIZATION

SM: $(5.9 \pm 2.1) \times 10^{-7}$

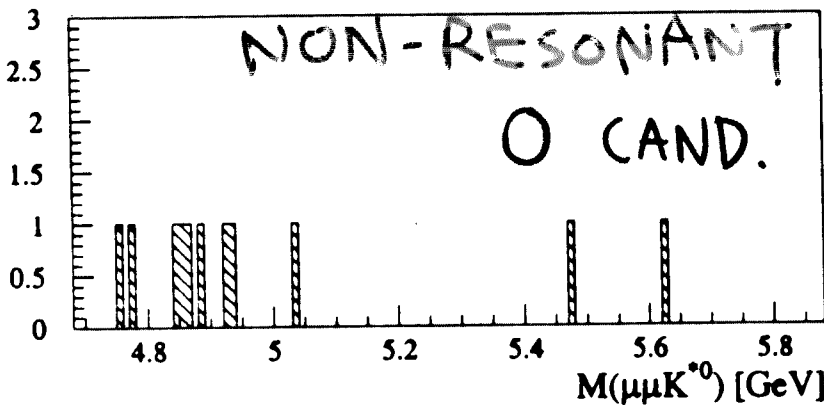


BF < 5.2×10^{-6}
 (90% CL)

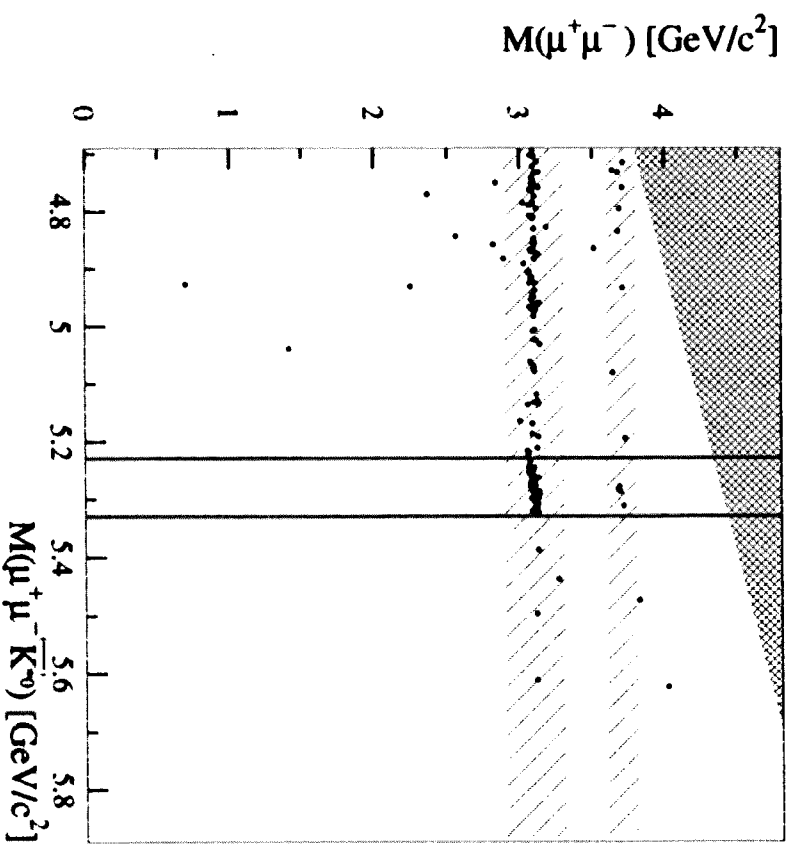
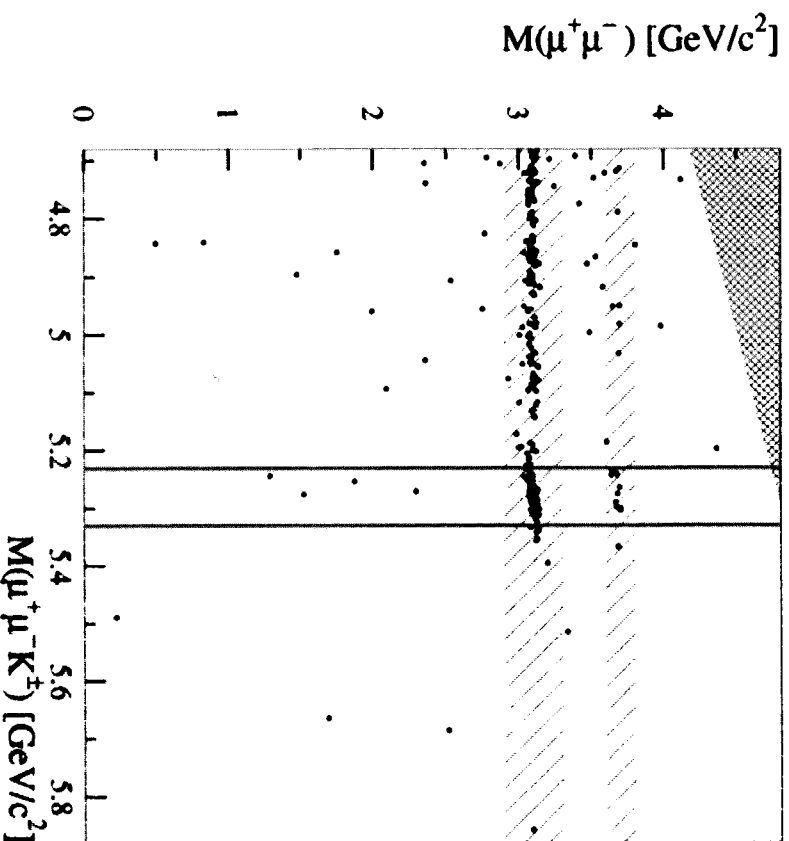
$B^0 \rightarrow K^{*0} \mu^+ \mu^-$
 nonresonant



SIGNAL
 FOR NORMALIZATION



BF < 4.0×10^{-6}
 (90% CL)
 SM: $(2.0 \pm 0.7) \times 10^{-6}$



- 4 candidates
- BR $< 5.2 \times 10^{-6}$ @90% CL
- SM: $(5.9 \pm 2.1) \times 10^{-7}$
- 0 candidate
- BR $< 4.0 \times 10^{-6}$ @90% CL
- SM: $(2.0 \pm 0.7) \times 10^{-6}$

Expected signal ~ 0.5 event each.

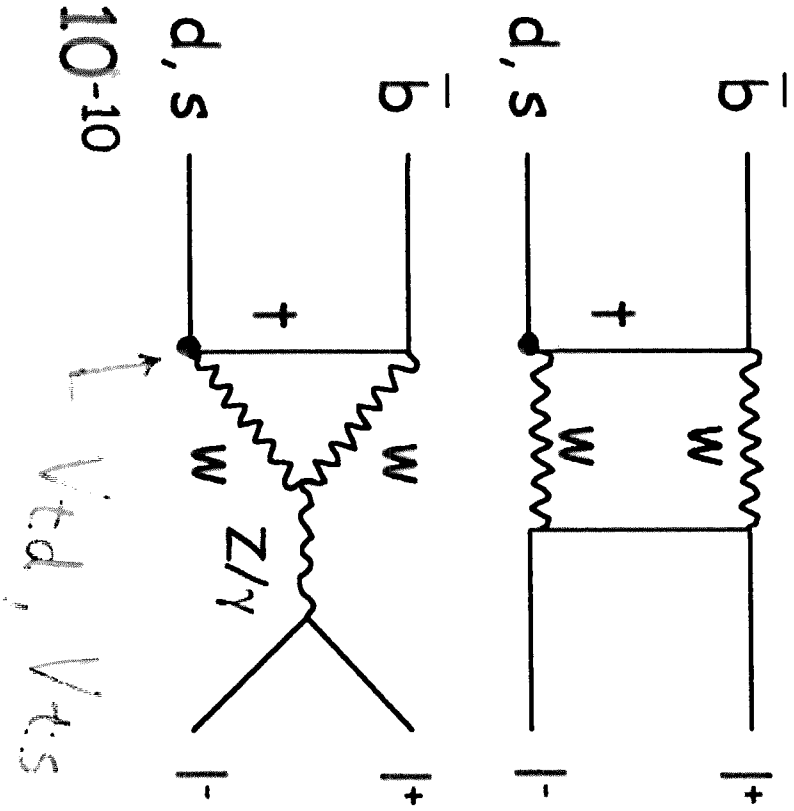
Should see a handful of signal events in Run II.

Even Rarer Decays: $B^0, B^0_s \rightarrow l^+l^-$

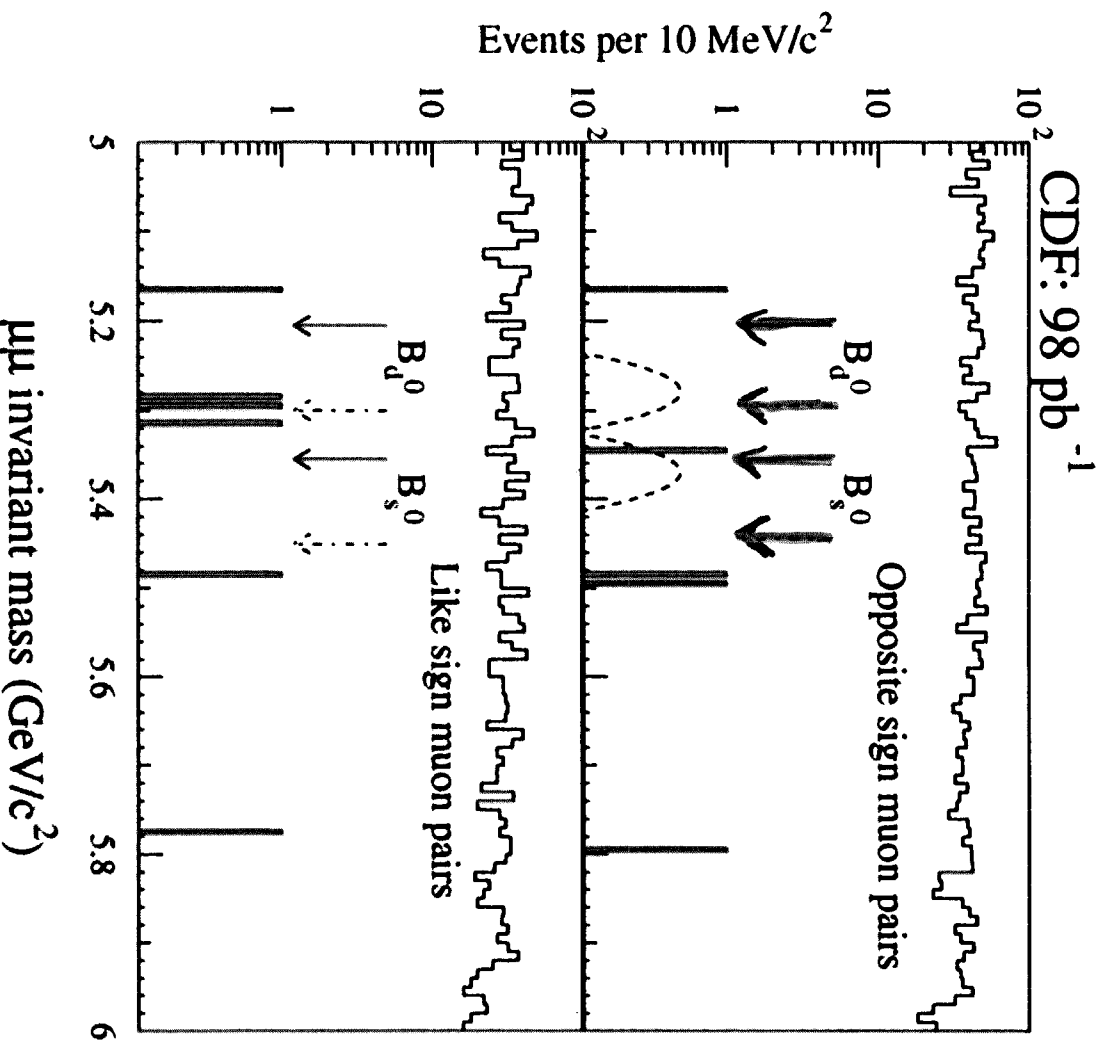
- V_{td} for B^0 , V_{ts} for B^0_s
- Helicity suppressed.
- B.R. very small.

SM predictions:

- $B^0 \rightarrow \mu^+\mu^-$ $(1.5 \pm 1.4) \times 10^{-10}$
- $B^0_s \rightarrow \mu^+\mu^-$ $(3.5 \pm 1.0) \times 10^{-9}$
- $B^0 \rightarrow e^+e^-$ $(3.4 \pm 3.1) \times 10^{-15}$
- $B^0_s \rightarrow e^+e^-$ $(8.0 \pm 3.5) \times 10^{-14}$



Rare Decays $B^0, B_s^0 \rightarrow \mu^+\mu^-$ PRD 57, 3811 (1998)



Still long way to go...

One candidate

in the overlap region

of B^0 and B_s^0 mass

windows.

B.R. $< 8.6 \times 10^{-7}$ for B^0

B.R. $< 2.6 \times 10^{-6}$ for B_s^0

@ 95% C.L.

Also looked for

decays to $e^+\mu^-$, $e^-\mu^+$

B.R. $< 4.5 \times 10^{-6}$ for B^0

B.R. $< 8.2 \times 10^{-6}$ for B_s^0

PRL 81, 5742 (1998)

Summary

- Major upgrades complete for Run-II CDF.
Has just started taking data.
Vastly improved B physics potential :
Integrated luminosity $\times 20$ ~~in~~ ^{by} 2003-2004.
CDF : better vertexing, impact parameter track trigger.
- Two major measurements of the CKM triangle, perhaps well before 2 fb^{-1} .
 $\sin 2\beta$ to ± 0.043 .
 Δm_s up to 40 ps^{-1} (expect $\sim 17 \text{ ps}^{-1}$ in SM).
- Some optimism for third major measurement.
Angle γ to $\sim 10^\circ$ from $B^0 \rightarrow \pi^+\pi^-$ plus $B_s^0 \rightarrow K^+K^-$
(modulo SU(3) breaking effects).
- B_s^0 measurements unique to CDF, and play important roles.
- Many other measurements expected.
Some benefit from (or require) more than 2 fb^{-1} .
Expect 15 fb^{-1} by the end of 2007.
- Then we quit. BTeV starts in 2008.