

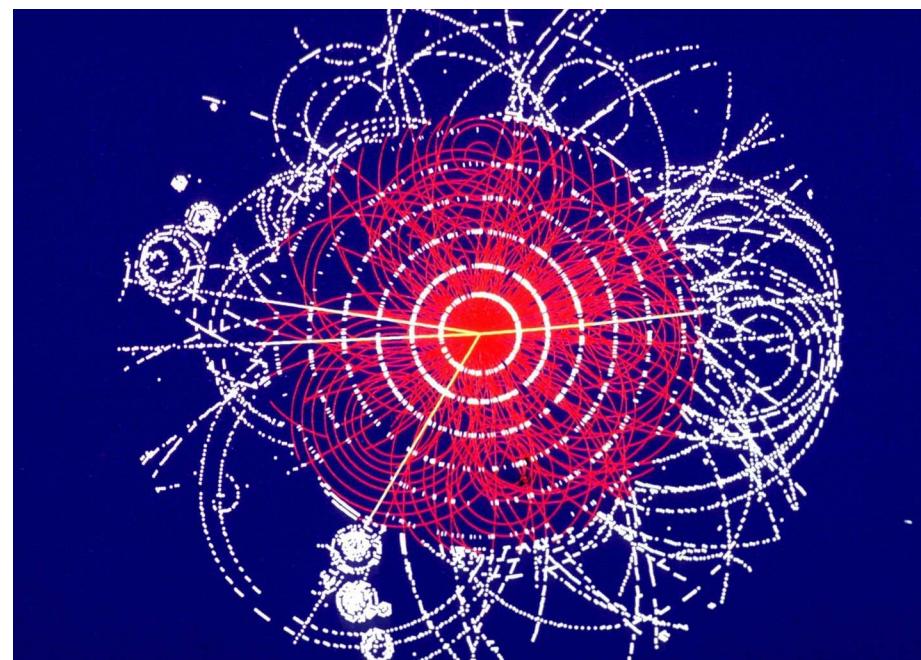
# HIGGS PHYSICS AT THE LHC

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Discoveries of Higgs and Supersymmetry to Pioneer the particle physics in 21st Century

University of Tokyo, Nov. 24–25, 2005

- Goals of Higgs Physics
- SM Channels
- MSSM:  $H/A$  and  $H^\pm$
- Coupling measurements
- QCD Corrections
- $HVV$  vertex structure
- $HHH$  coupling
- Conclusions



## Goals of Higgs Physics

Higgs Search = search for dynamics of  $SU(2) \times U(1)$  breaking

- Discover the Higgs boson
- Measure its couplings and probe mass generation for gauge bosons and fermions

Fermion masses arise from Yukawa couplings via  $\Phi^\dagger \rightarrow (0, \frac{v+H}{\sqrt{2}})$

$$\begin{aligned}\mathcal{L}_{\text{Yukawa}} &= -\Gamma_d^{ij} \bar{Q}'^i_L \Phi d'^j_R - \Gamma_d^{ij*} \bar{d}'^i_R \Phi^\dagger Q'_L + \dots &= -\Gamma_d^{ij} \frac{v+H}{\sqrt{2}} \bar{d}'^i_L d'^j_R + \dots \\ &= -\sum_f m_f \bar{f} f \left( 1 + \frac{H}{v} \right)\end{aligned}$$

- Test SM prediction:  $\bar{f} f H$  Higgs coupling strength  $= m_f/v$
- Observation of  $H f \bar{f}$  Yukawa coupling is no proof that v.e.v exists

## Higgs coupling to gauge bosons

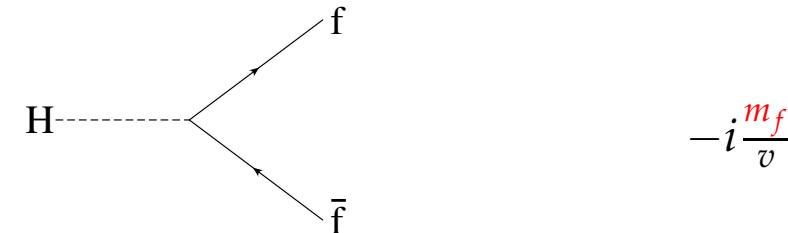
Kinetic energy term of Higgs doublet field:

$$(D^\mu \Phi)^\dagger (D_\mu \Phi) = \frac{1}{2} \partial^\mu H \partial_\mu H + \left[ \left( \frac{gv}{2} \right)^2 W^{\mu+} W_\mu^- + \frac{1}{2} \frac{(g^2 + g'^2)}{4} v^2 Z^\mu Z_\mu \right] \left( 1 + \frac{H}{v} \right)^2$$

- $W, Z$  mass generation:  $m_W^2 = \left( \frac{gv}{2} \right)^2$ ,  $m_Z^2 = \frac{(g^2 + g'^2)v^2}{4}$
- $WWH$  and  $ZZH$  couplings are generated
- Higgs couples proportional to mass: coupling strength =  $2 m_V^2/v$  within SM

Measurement of  $WWH$  and  $ZZH$  couplings is essential for identification of  $H$  as agent of symmetry breaking: Without a v.e.v. such a trilinear coupling is impossible at tree level

## Feynman rules



Verify tensor structure of  $HVV$  couplings. Loop induced couplings lead to  $HV_{\mu\nu}V^{\mu\nu}$  effective coupling and different tensor structure:  $g_{\mu\nu} \rightarrow q_1 \cdot q_2 g_{\mu\nu} - q_{1\nu}q_{2\mu}$

## The MSSM Higgs sector

The SM uses the conjugate field  $\Phi_c = i\sigma_2\Phi^*$  to generate down quark and lepton masses. In supersymmetric models this must be an independent field

$$\begin{aligned}\mathcal{L}_{\text{Yukawa}} = & -\Gamma_d \bar{Q}_L \Phi_1 d_R - \Gamma_e \bar{L}_L \Phi_1 e_R + \text{h.c.} \\ & -\Gamma_u \bar{Q}_L \Phi_2 u_R + \text{h.c.}\end{aligned}$$

Two complex Higgs doublet fields  $\Phi_1$  and  $\Phi_2$  receive mass and v.e.v.s  $v_1, v_2$  from generalized Higgs potential. Mass eigenstates constructed out of these 8 real fields are

### Neutral sector:

2 CP even Higgs bosons:  $h$  and  $H$

1 CP odd Higgs boson:  $A$

1 Goldstone boson:  $\chi_0$

### Charged sector:

charged Higgs bosons:  $H^\pm$

charged Goldstone boson:  $\chi^\pm$

Goldstone bosons absorbed as longitudinal degrees of freedom of  $Z, W^\pm$

## Couplings of the MSSM Higgses

### Fermions

Two doublet fields mix, two v.e.v's  $v_1 = v \cos \beta, v_2 = v \sin \beta$ :

$$\begin{aligned}\mathcal{L}_{\text{Yuk.}} &= -\Gamma_b \bar{b}_L \Phi_1^0 b_R - \Gamma_t \bar{t}_L \Phi_2^0 t_R + \text{h.c.} \\ &= -\Gamma_b \bar{b}_L \frac{v_1 + H \cos \alpha - h \sin \alpha + iA \sin \beta}{\sqrt{2}} b_R - \Gamma_t \bar{t}_L \frac{v_2 + H \sin \alpha + h \cos \alpha + iA \cos \beta}{\sqrt{2}} t_R + \dots\end{aligned}$$

Expressed in terms of masses the Yukawa Lagrangian is

$$\mathcal{L}_{\text{Yuk.}} = -\frac{m_b}{v} \bar{b} \left( v + H \frac{\cos \alpha}{\cos \beta} - h \frac{\sin \alpha}{\cos \beta} - i\gamma_5 A \tan \beta \right) b - \frac{m_t}{v} \bar{t} \left( v + H \frac{\sin \alpha}{\sin \beta} + h \frac{\cos \alpha}{\sin \beta} - i\gamma_5 A \cot \beta \right) t$$

$\implies$  coupling factors compared to SM  $hff$  coupling  $-i m_f/v$

### Gauge Bosons

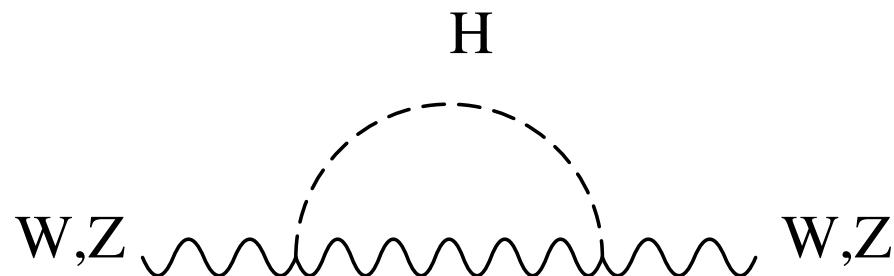
extra coupling factors for  $hVV$  and  $HVV$  couplings as compared to SM

$$hVV \sim \sin(\beta - \alpha) \quad HVV \sim \cos(\beta - \alpha)$$

## Clues to the Higgs boson mass: SM case

Higgs mass is largely unconstrained by theory  $\Rightarrow$  need experimental input

Electroweak precision data from LEP, SLC,  $m_W, m_t, \dots$



SM predictions for observables depend logarithmically on Higgs mass

$$\sim \frac{\alpha}{\pi} \log \frac{m_H^2}{m_W^2}$$

Data require small such contribution

$$\Rightarrow m_H \approx \text{order } m_Z$$

## SM Higgs mass fit to EW precision data

$$m_H = 91^{+45}_{-32} \text{ GeV}$$

Including theory uncertainty

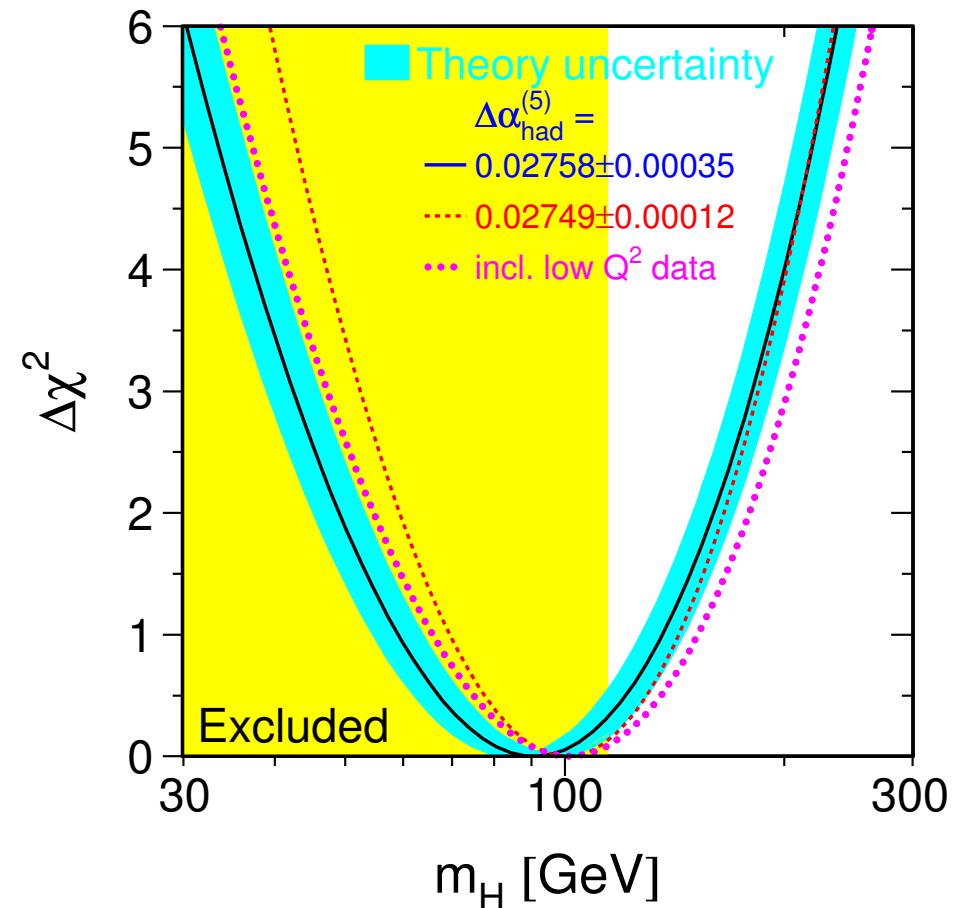
$$m_H < 186 \text{ GeV} \quad (95\% \text{ CL})$$

Does not include  
Direct search limit from LEP

$$m_H > 114 \text{ GeV} \quad (95\% \text{ CL})$$

Renormalize probability for  
 $m_H > 114 \text{ GeV}$  to 100%:

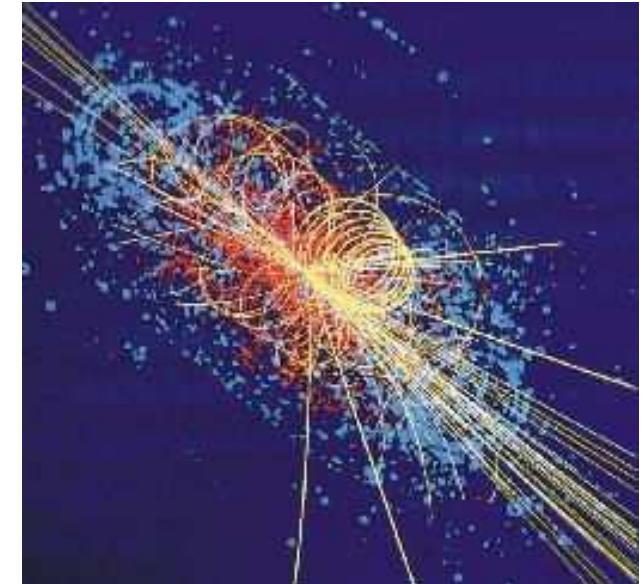
$$m_H < 219 \text{ GeV} \quad (95\% \text{ CL})$$



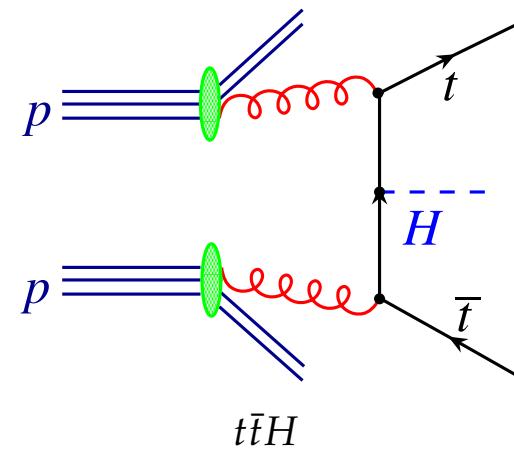
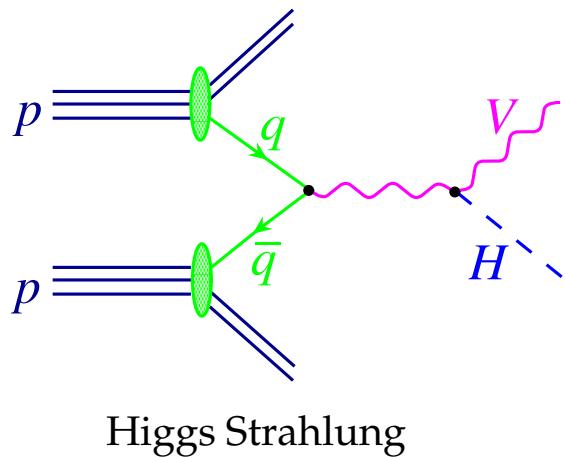
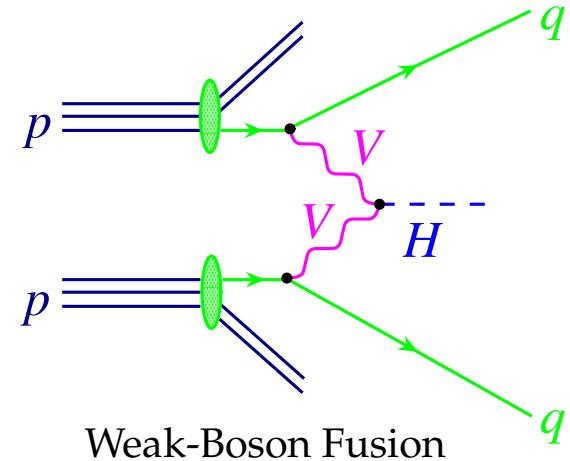
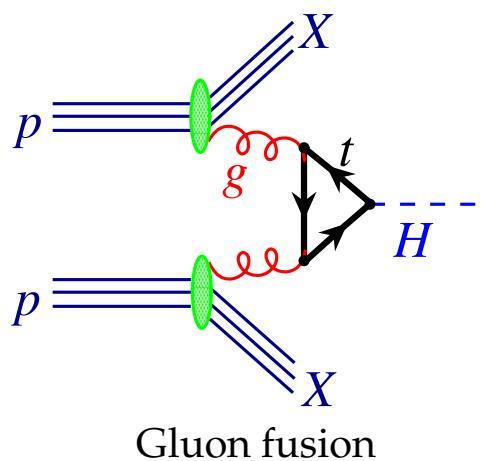
## Higgs boson channels at LHC

Two steps

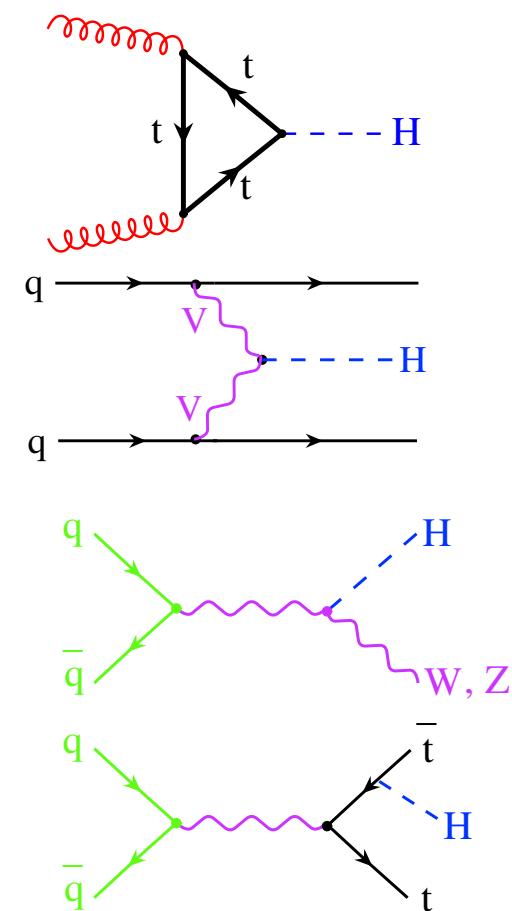
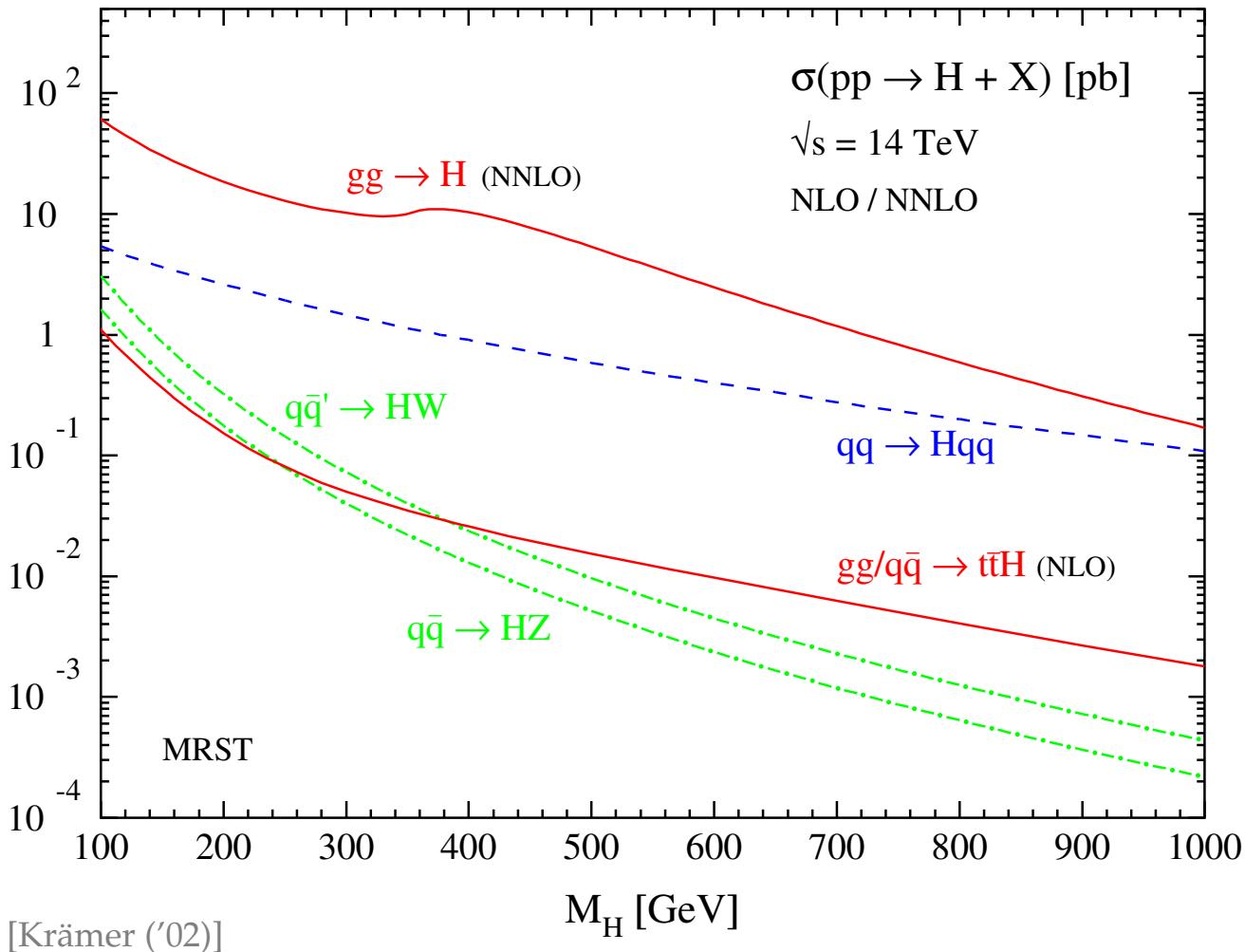
- Production of the Higgs boson
- Detection of the decay products of the Higgs boson and identification of the events



## Production Modes

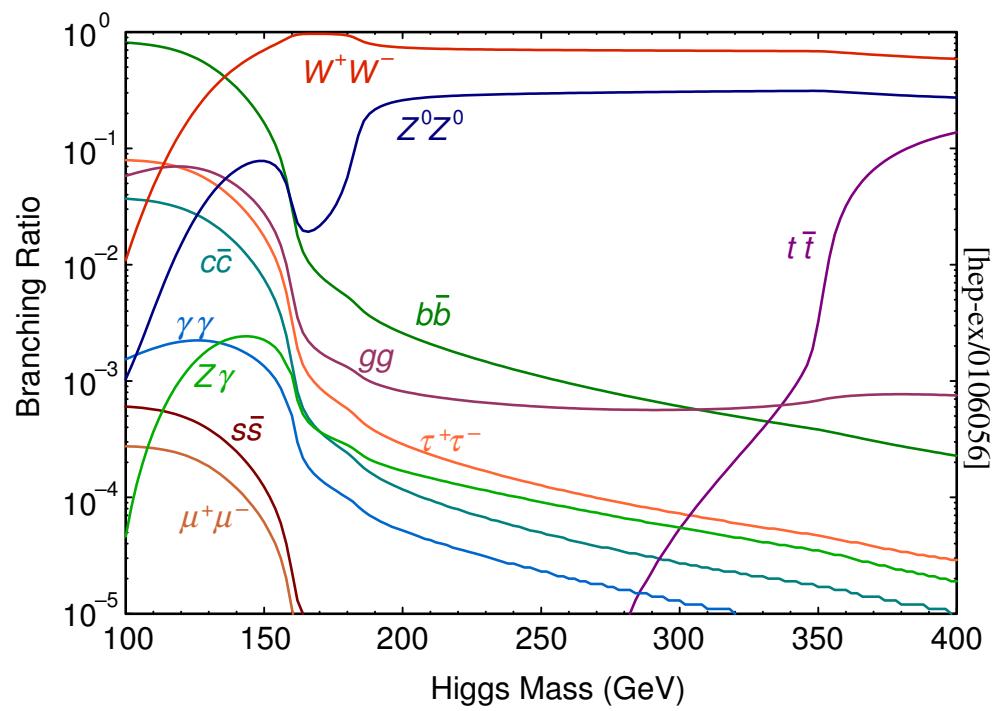
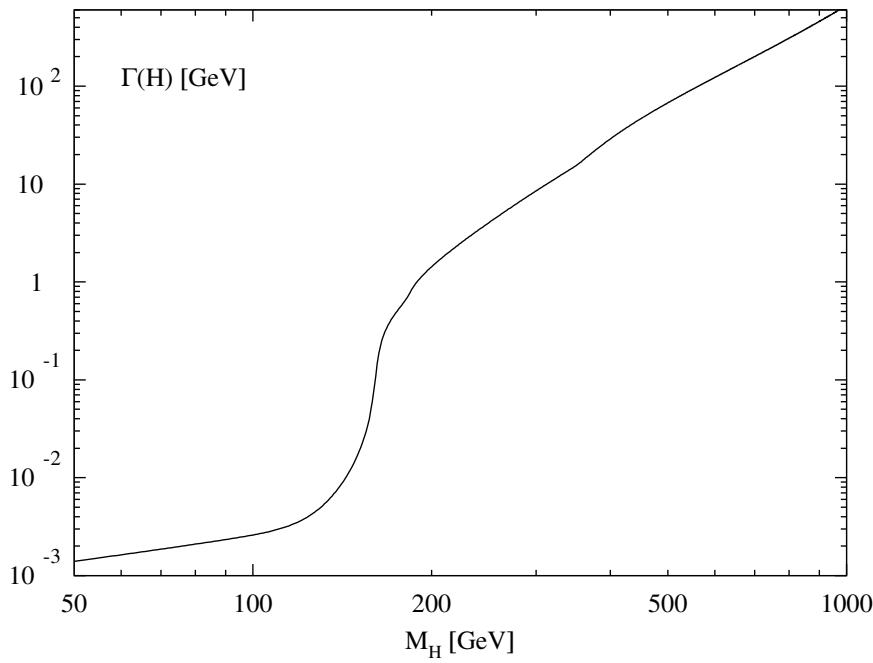


## Total cross sections at the LHC

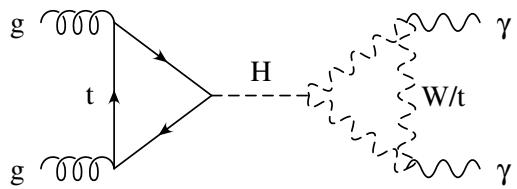


## Decay of the SM Higgs

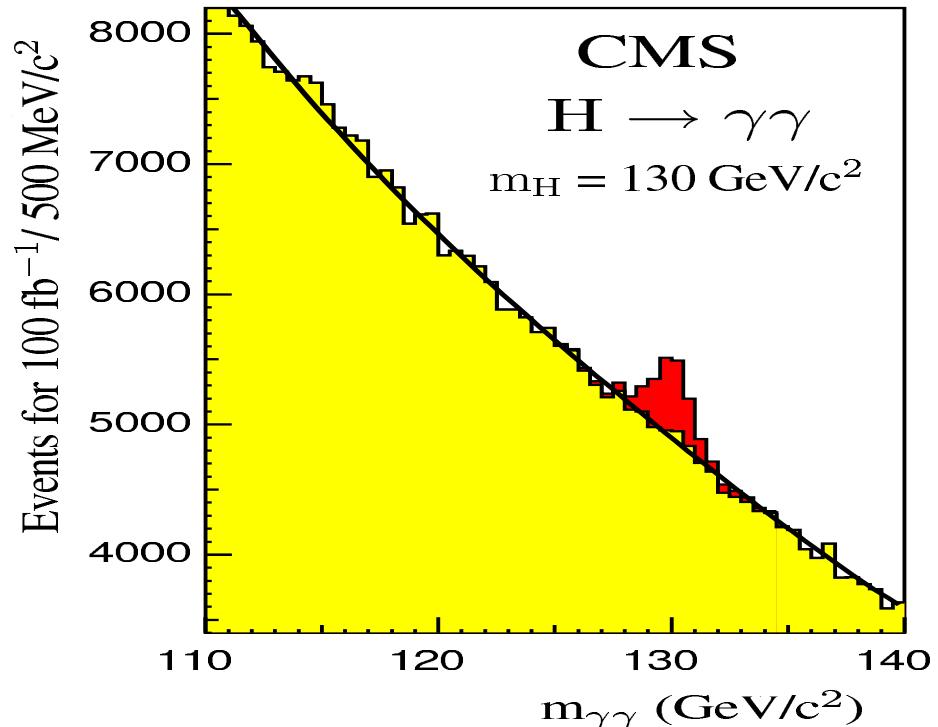
Higgs decay width and branching fractions within the SM



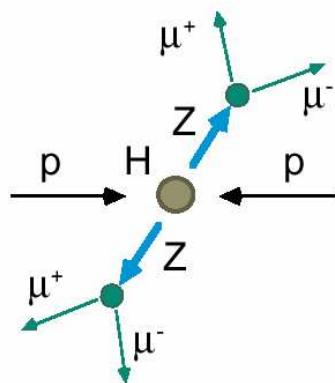
## $H \rightarrow \gamma\gamma$



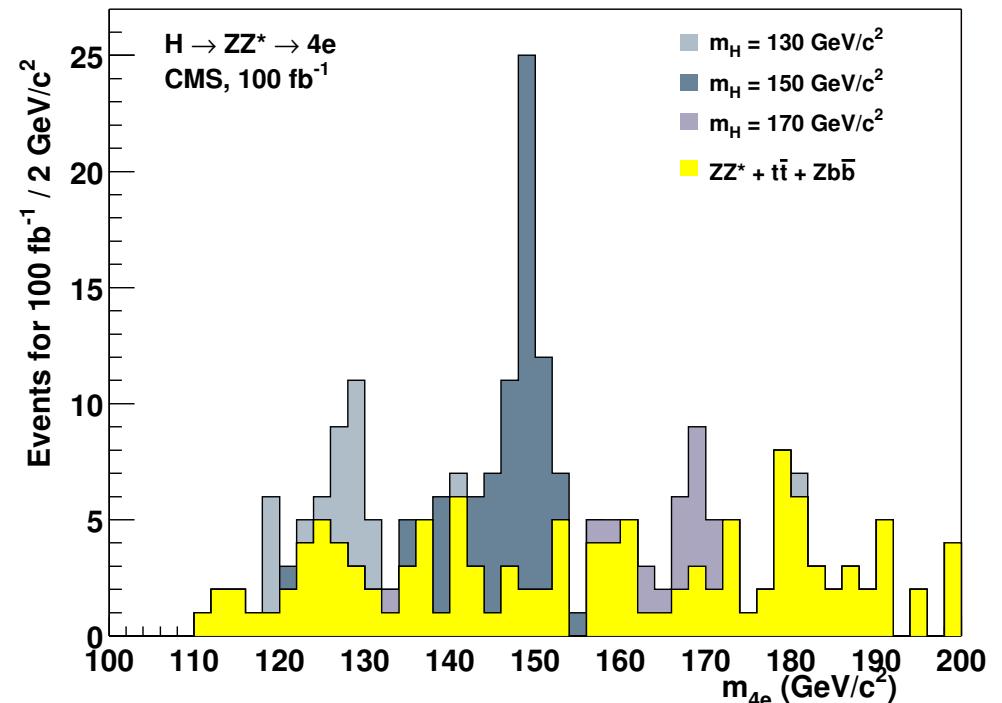
- ✗  $\text{BR}(H \rightarrow \gamma\gamma) \approx 10^{-3}$
- ✗ large backgrounds from  $q\bar{q} \rightarrow \gamma\gamma$  and  $gg \rightarrow \gamma\gamma$
- ✓ but CMS and ATLAS will have excellent photon-energy resolution (order of 1%)
- ✓ Look for a narrow  $\gamma\gamma$  invariant mass peak
- ✓ extrapolate background into the signal region from sidebands.



$$H \rightarrow ZZ \rightarrow \ell^+ \ell^- \ell^+ \ell^-$$



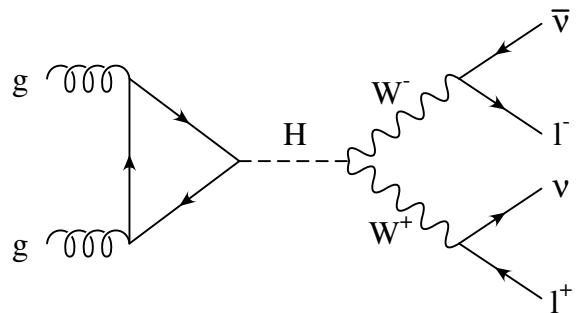
- ✓ invariant mass of the charged leptons fully reconstructed



For  $m_H \approx 0.6\text{--}1 \text{ TeV}$ , use the “silver-plated” mode  $H \rightarrow ZZ \rightarrow \nu\bar{\nu}\ell^+\ell^-$

- ✓  $\text{BR}(H \rightarrow \nu\bar{\nu}\ell^+\ell^-) = 6 \text{ BR}(H \rightarrow \ell^+\ell^-\ell^+\ell^-)$
- ✓ the large missing  $E_T$  allows a measurement of the transverse mass

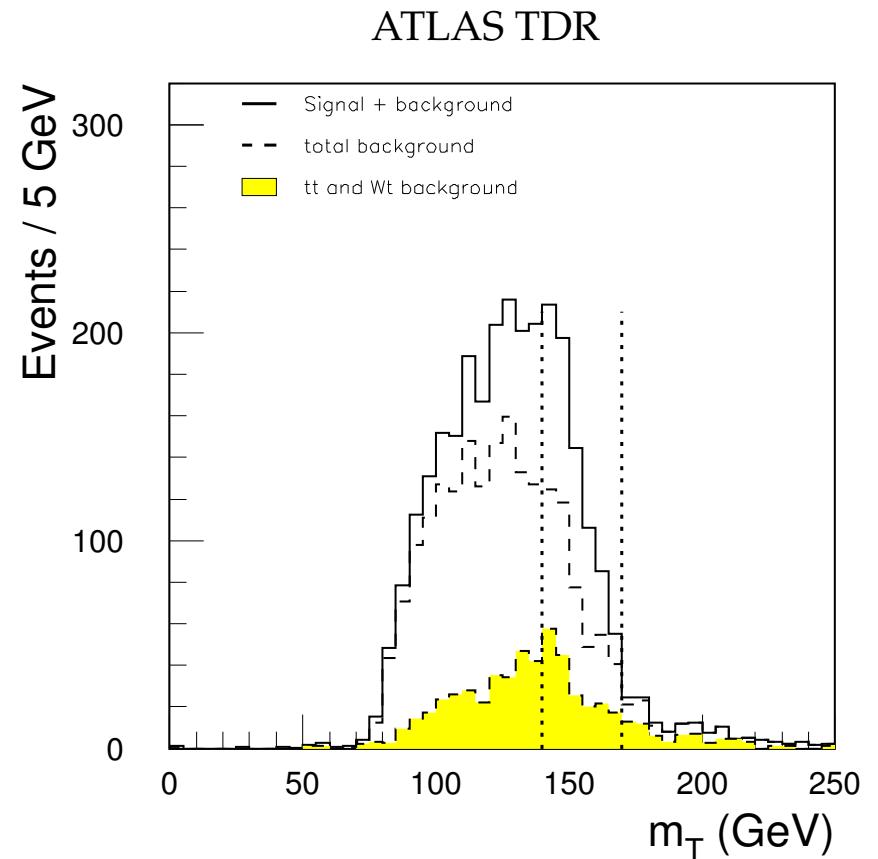
$$H \rightarrow WW \rightarrow \ell^+ \bar{\nu} \ell^- \nu$$



- ✓ Exploit  $\ell^+ \ell^-$  angular correlations
- ✓ measure the transverse mass with a Jacobian peak at  $m_H$

$$m_T = \sqrt{2 p_T^{\ell\ell} E_T (1 - \cos(\Delta\Phi))}$$

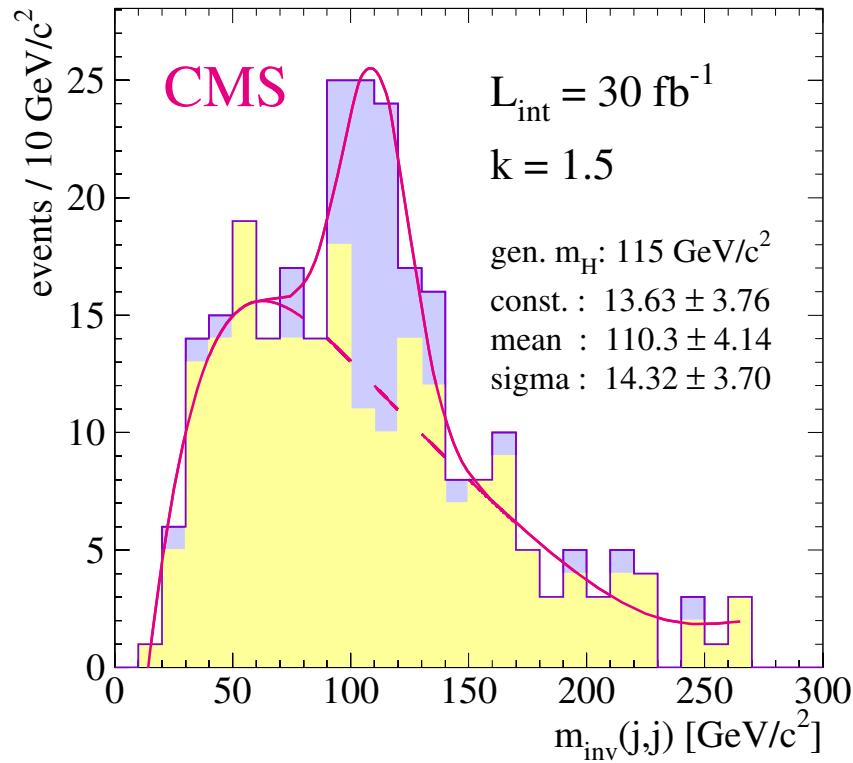
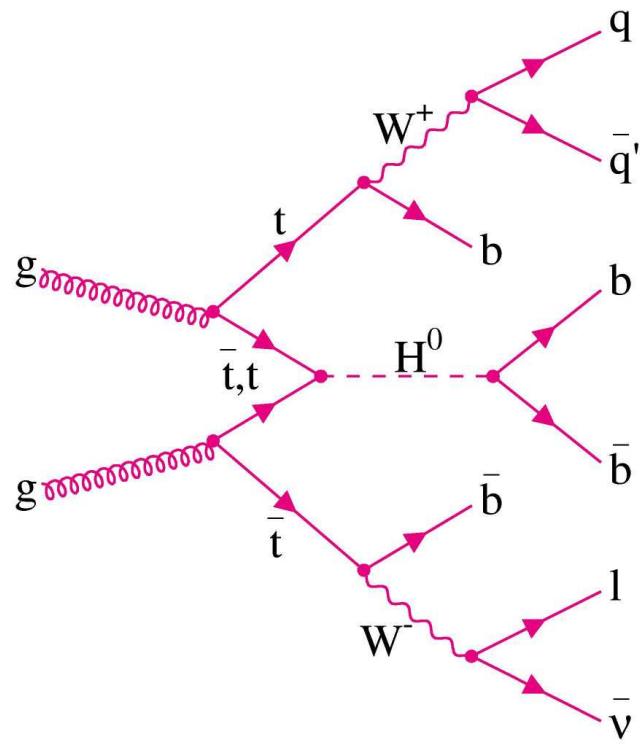
✗ background and signal have similar shape  $\Rightarrow$  must know the background normalization precisely



$$m_H = 170 \text{ GeV}$$

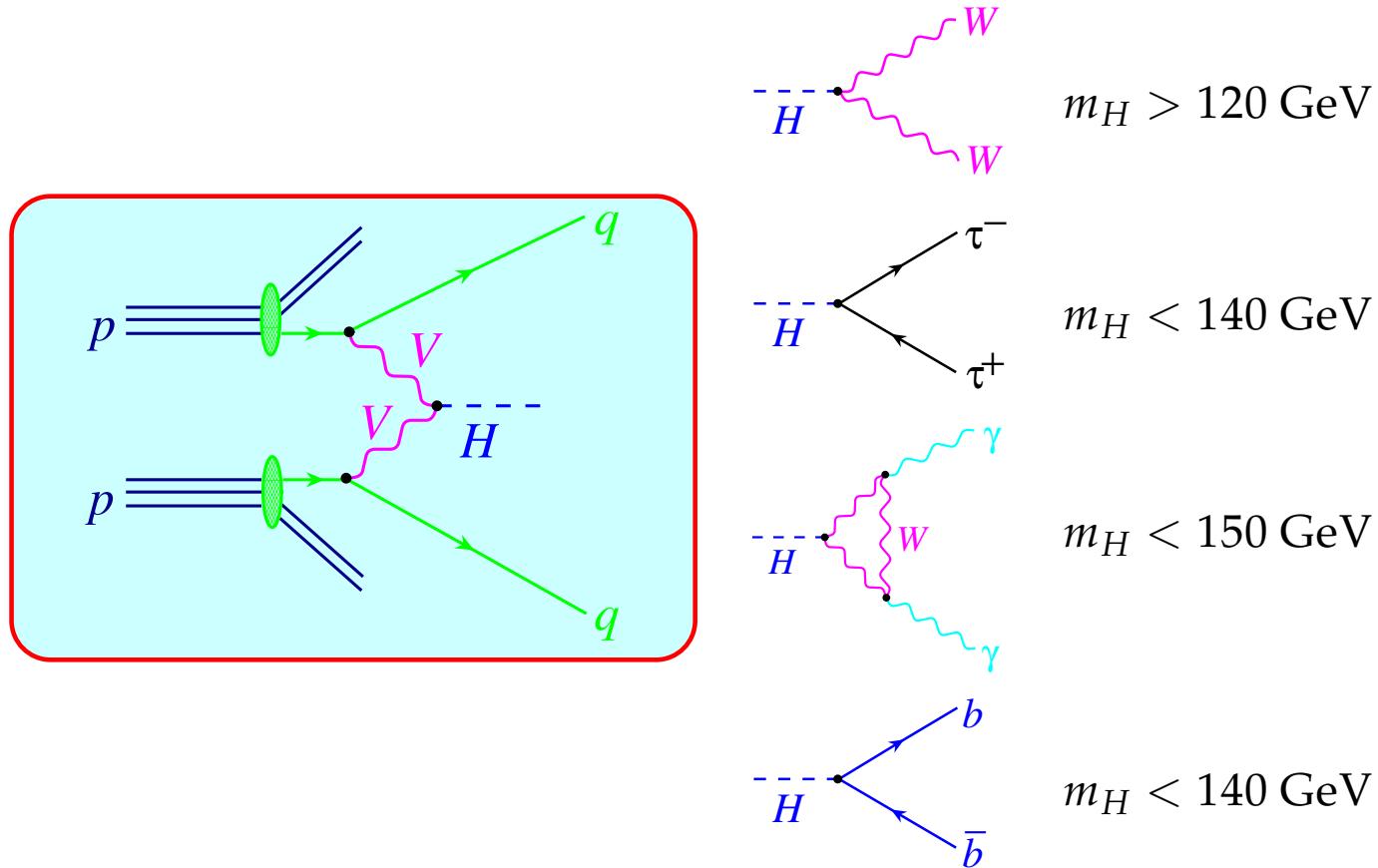
$$\text{integrated luminosity} = 20 \text{ fb}^{-1}$$

## $t\bar{t}H \rightarrow t\bar{t}b\bar{b}$



- ✓  $h_t = t\bar{t}H$  Yukawa coupling  $\Rightarrow$  measure  $h_t^2 \text{ BR}(H \rightarrow b\bar{b})$
- ✗ must know the background normalization precisely

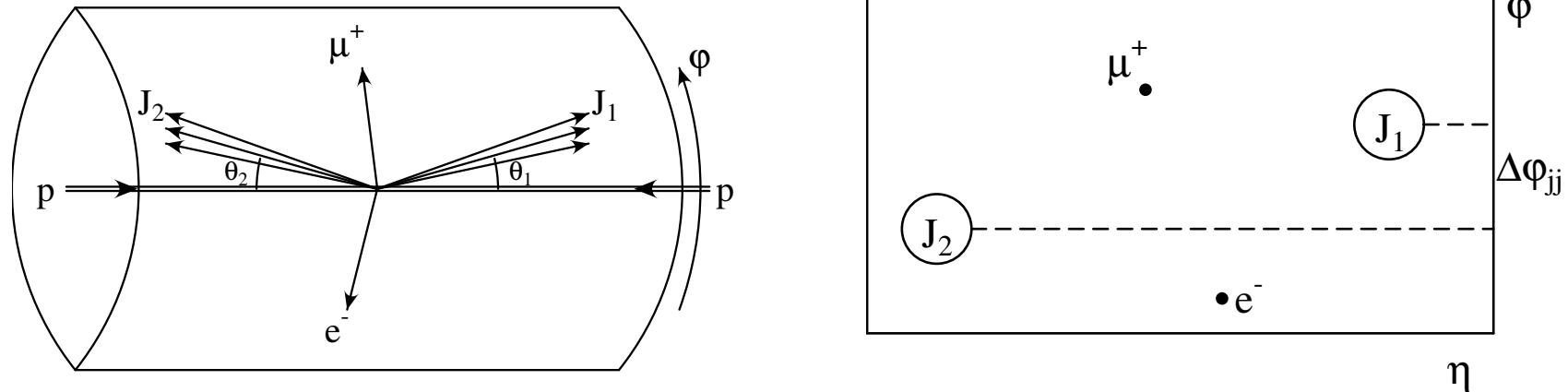
## Weak Boson Fusion



[Eboli, Hagiwara, Kauer, Plehn, Rainwater, D.Z. ...] [Mangano, Moretti, Piccinini, Pittau, Polosa ('03)]

Most measurements can be performed at the LHC with **statistical accuracies** on the measured cross sections times decay branching ratios,  $\sigma \times \text{BR}$ , of **order 10%** (sometimes even better).

## WBF signature



$$\eta = \frac{1}{2} \log \frac{1 + \cos \theta}{1 - \cos \theta}$$

### Characteristics:

- energetic jets in the **forward** and **backward** directions ( $p_T > 20$  GeV)
- Higgs decay products **between** tagging jets
- Little gluon radiation in the central-rapidity region, due to **colorless**  $W/Z$  exchange  
(**central jet veto**: no extra jets with  $p_T > 20$  GeV and  $|\eta| < 2.5$ )

## Example: Parton level analysis of $H \rightarrow WW$

Near threshold:  $W$  and  $W^*$  almost at rest in Higgs rest frame  $\Rightarrow$  use  $m_{ll} \approx m_{\nu\nu}$  for improved transverse mass calculation:

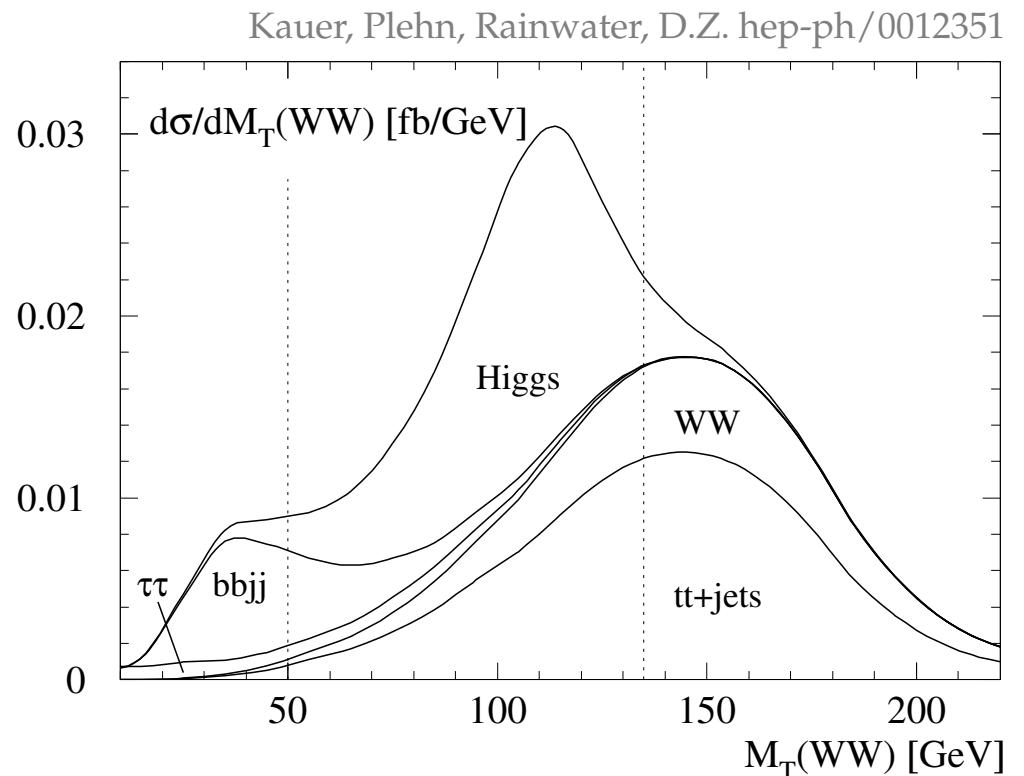
$$E_{T,ll} = \sqrt{\mathbf{p}_{T,ll}^2 + m_{ll}^2}$$

$$E_T = \sqrt{\mathbf{p}_T^2 + m_{\nu\nu}^2} \approx \sqrt{\mathbf{p}_T^2 + m_{ll}^2}$$

$$M_T = \sqrt{(E_T + E_{T,ll})^2 - (\mathbf{p}_{T,ll} + \mathbf{p}_T)^2}$$

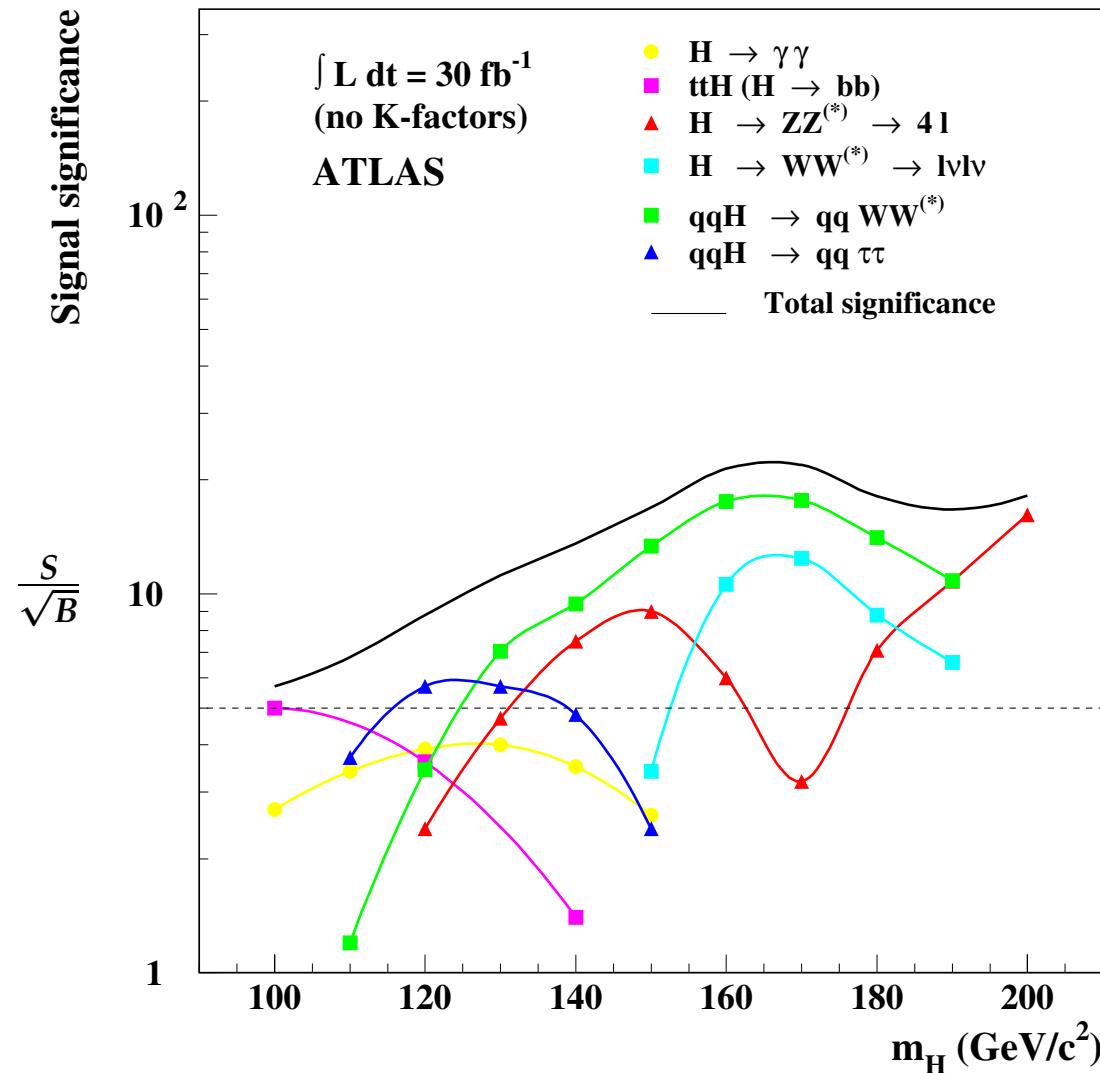
Observe Jacobian peak below

$$M_T = m_H$$



Transverse mass distribution for  $m_H = 115$  GeV and  $H \rightarrow WW^* \rightarrow e^\pm \mu^\mp p_T$

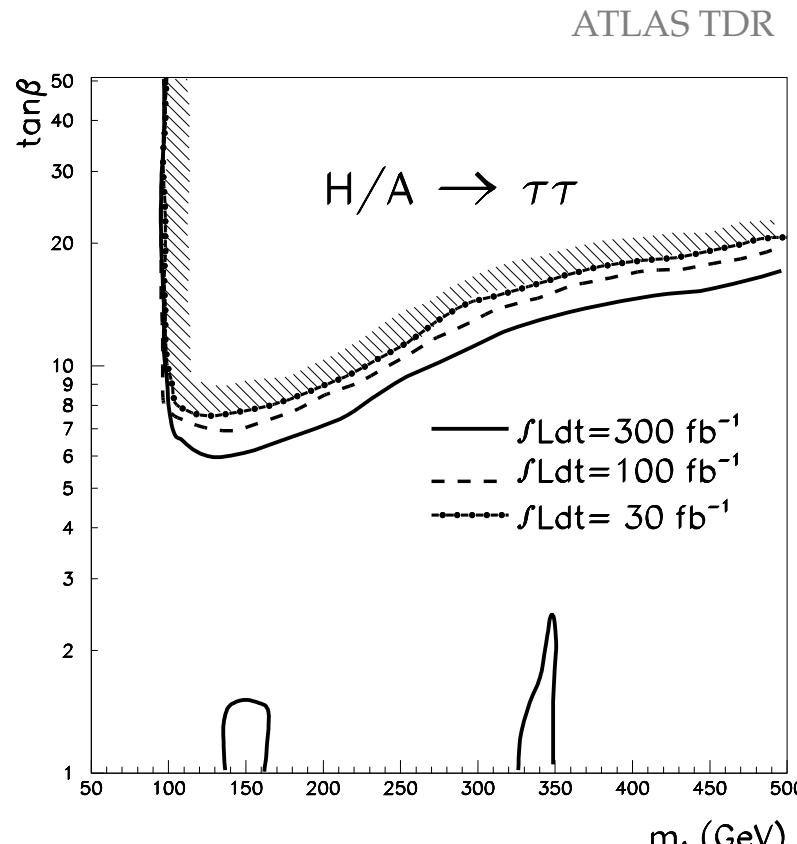
## Higgs discovery potential



## Reach for H/A discovery within MSSM

Enhancement of  
*Hbb* and *Abb* coupling  
by factor  $\tan\beta$   
compared to SM Higgs

- ⇒ large production cross section for  $p p \rightarrow \bar{b}bH/A$
- ⇒ decay dominated by  $H/A \rightarrow \bar{b}b, \tau^+\tau^-$



5 $\sigma$  discovery contours

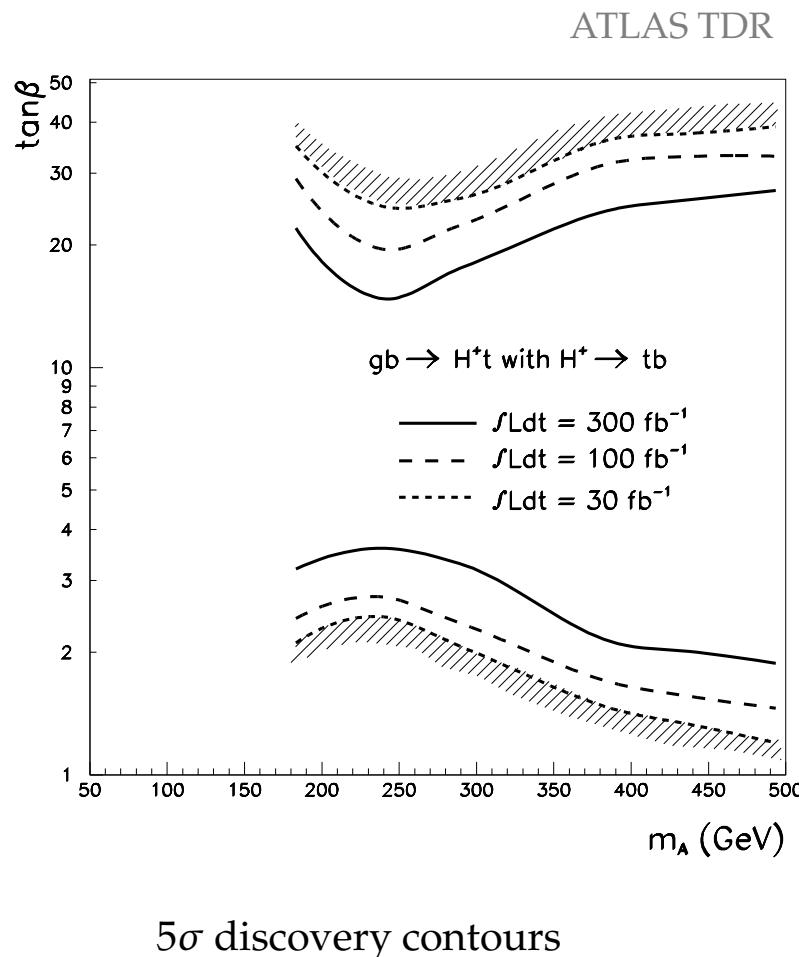
## Reach for $H^\pm$ discovery within MSSM

- For  $m_{H^\pm} > m_t + m_b$  expect  $H^\pm \rightarrow tb$  decay
- Dominant production process

$$gg \rightarrow H^\pm tb$$

b-quark has low  $p_T$ :  
 $gb \rightarrow H^\pm t$  is dominant subprocess

- Main background from  $t\bar{t}(+jets)$  production



## Measuring Higgs couplings at LHC

LHC rates for partonic process  $pp \rightarrow H \rightarrow xx$  given by  $\sigma(pp \rightarrow H) \cdot BR(H \rightarrow xx)$

$$\sigma(H) \times BR(H \rightarrow xx) = \frac{\sigma(H)^{\text{SM}}}{\Gamma_p^{\text{SM}}} \cdot \frac{\Gamma_p \Gamma_x}{\Gamma},$$

Measure products  $\Gamma_p \Gamma_x / \Gamma$  for combination of processes ( $\Gamma_p = \Gamma(H \rightarrow pp)$ )

**Problem:** rescaling fit results by common factor  $f$

$$\Gamma_i \rightarrow f \cdot \Gamma_i, \quad \Gamma \rightarrow f^2 \Gamma = \sum_{\text{obs}} f \Gamma_i + \Gamma_{\text{rest}}$$

leaves observable rate invariant  $\Rightarrow$  no model independent results at LHC

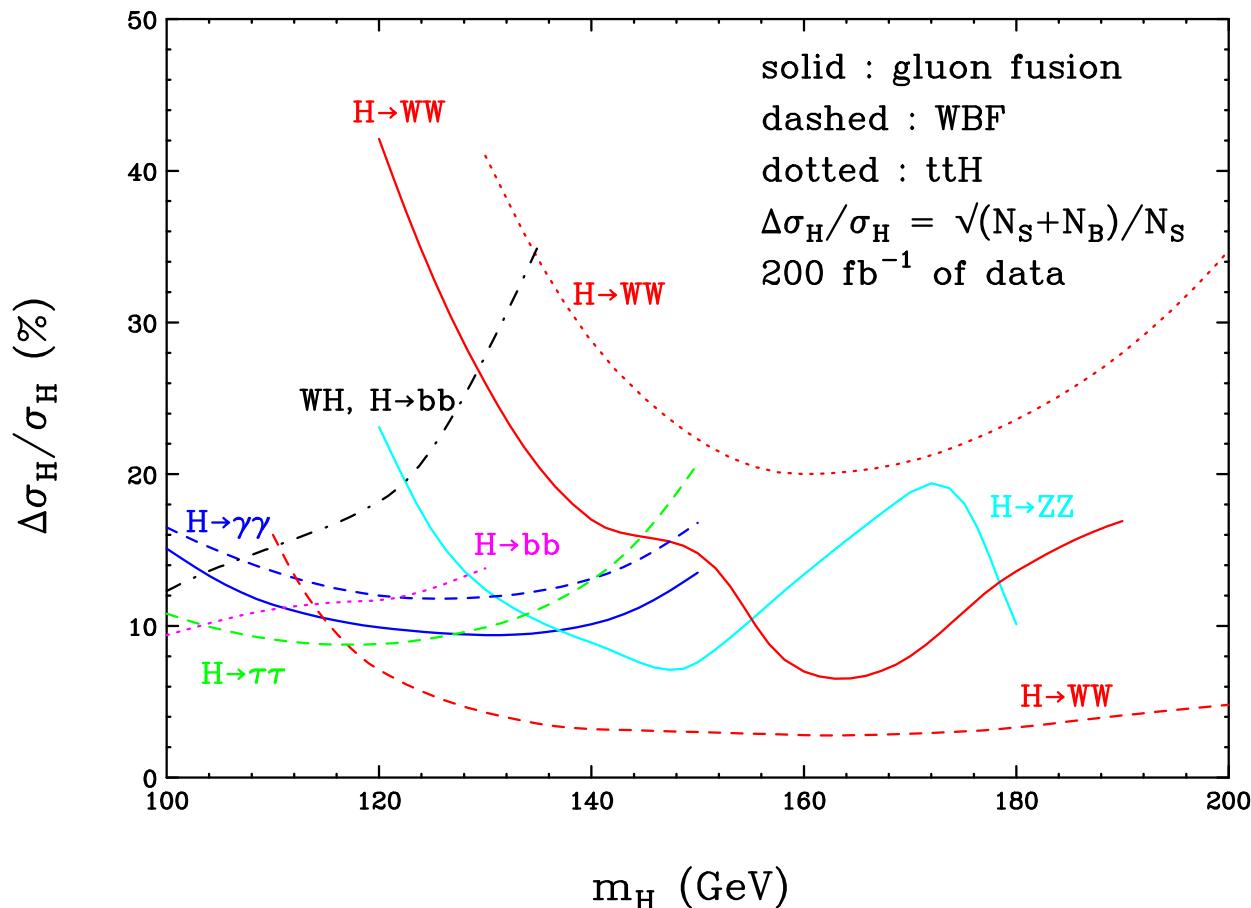
Loose bounds on scaling factor:

$$f^2 \Gamma > \sum_{\text{obs.}} f \Gamma_x \quad \Rightarrow \quad f > \sum_{\text{obs.}} \frac{\Gamma_x}{\Gamma} = \sum_{\text{obs.}} BR(H \rightarrow xx) (= \mathcal{O}(1))$$

Total width below experimental resolution of Higgs mass peak ( $\Delta m = 1 \dots 20 \text{ GeV}$ )

$$f^2 \Gamma < \Delta m \quad \Rightarrow \quad f < \sqrt{\frac{\Delta m}{\Gamma}} < \mathcal{O}(10 - 40)$$

## Statistical and systematic errors at LHC

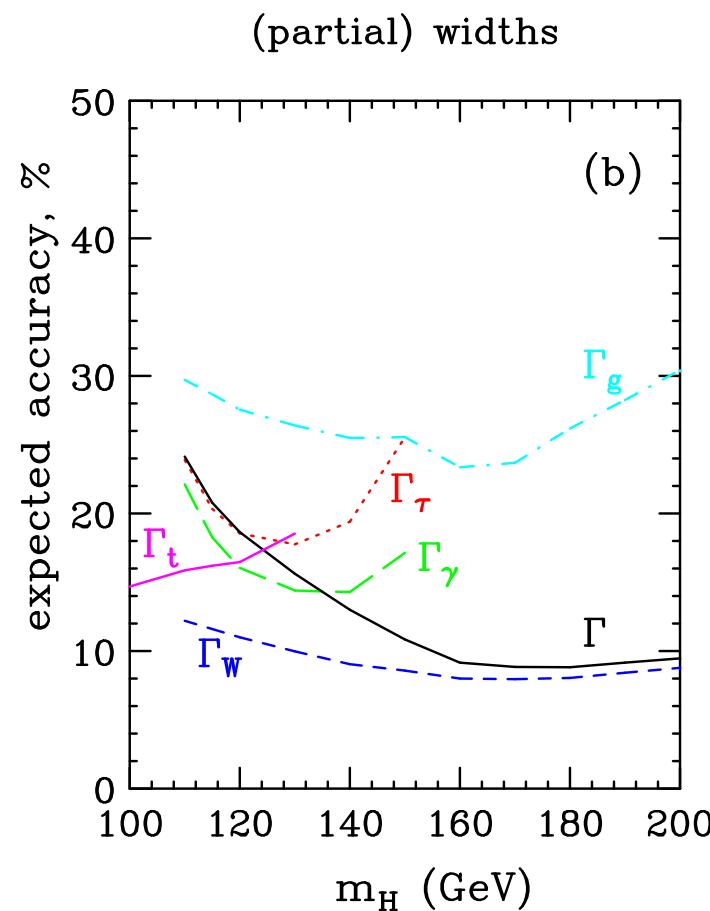
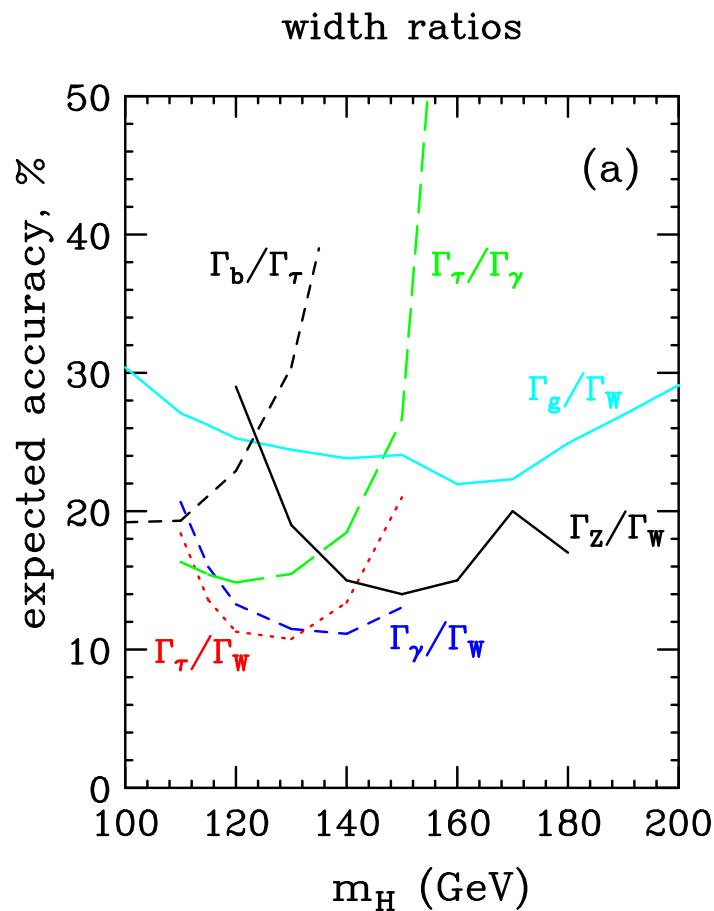


Assumed errors in fits to  
couplings:

- QCD/PDF uncertainties
  - $\pm 5\%$  for WBF
  - $\pm 20\%$  for gluon fusion
- luminosity/acceptance uncertainties
  - $\pm 5\%$

# Fit LHC data within constrained models

- $\frac{g_{H\tau\tau}}{g_{Hbb}} = \text{SM value}$
- $\frac{g_{HWW}}{g_{HZZ}} = \text{SM value}$
- no exotic channels



With  $200 \text{ fb}^{-1}$  measure partial width with 10–30% errors, couplings with 5–15% errors

## Distinguishing the MSSM Higgs sector from the SM

Alternative: compare data to predictions of specific models

Example:  $m_H^{\max}$  scenario of LEP analyses

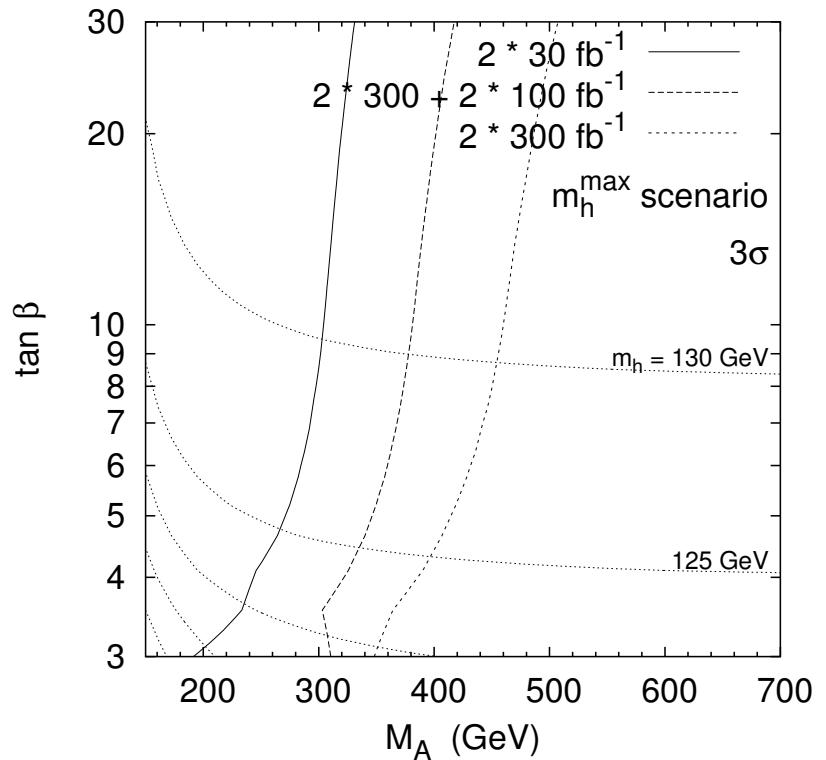
Consider modest  $m_A$ :

- decoupling almost complete for  $hWW$  and  $h\gamma\gamma$  (effective) vertices
- enhanced  $hbb$  and  $h\tau\tau$  couplings compared to SM increases total width of  $h$



- $\approx$  SM rates for  $h \rightarrow \tau\tau$  in WBF
- suppressed  $h \rightarrow \gamma\gamma$  and  $h \rightarrow WW$  rates in WBF

$3\sigma$ -effects or more at small  $m_A$



## QCD corrections for Higgs production

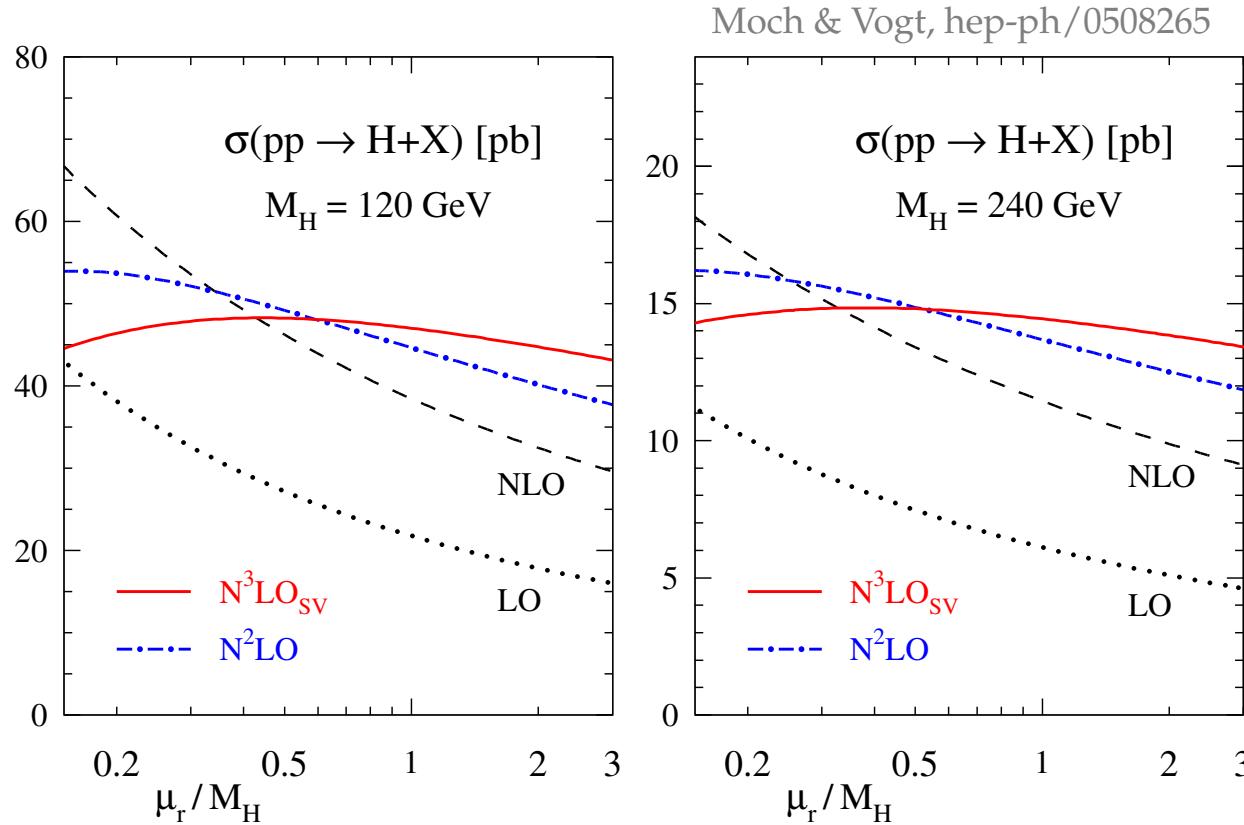
Measurement of **partial widths** at **10–20% level** or **couplings** at **5–10% level** requires predictions of SM production cross sections at **10% level or better**

⇒ need QCD corrections to production cross sections

Much work in recent years

- $gg \rightarrow H$  (all but NLO in  $m_t \rightarrow \infty$  limit)
  - NLO for finite  $m_t$ : Graudenz, Spira, Zerwas (1993)
  - NNLO: Harlander, Kilgore (2001); Anastasiou, Melnikov (2002); Ravindran, Smith, van Neerven (2003)
  - NNLL: Catani, de Florian, Grazzini, Nason (2003)
  - $N^3LO$  in soft approximation: Moch, Vogt (2005)
- weak boson fusion
  - total cross section at NLO: Han, Willenbrock (1991)
  - distributions at NLO: Figy, Oleari, D.Z (2003); Campbell, Ellis, Berger (2004)
- $t\bar{t}H$  associated production at NLO: Beenakker et al.; Dawson, Orr, Reina, Wackerlo (2002)
- $b\bar{b}H$  associated production at NLO: Dittmaier, Krämer, Spira; Dawson et al. (2003)

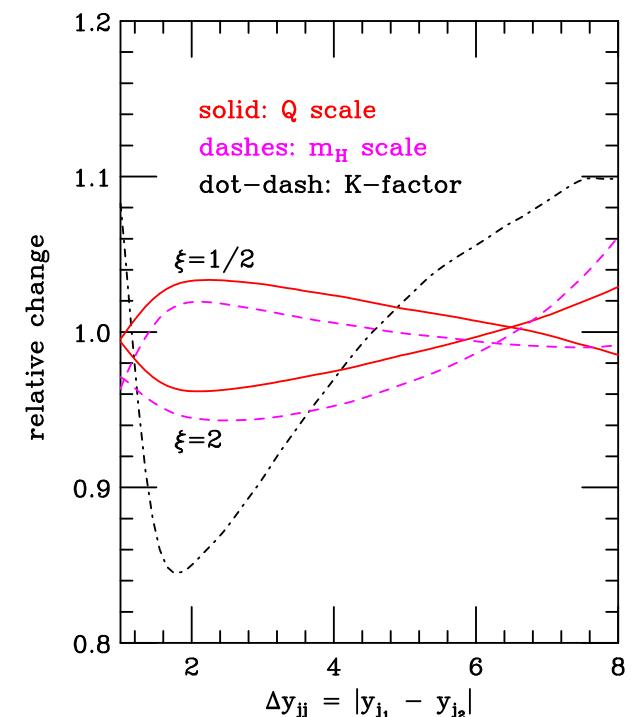
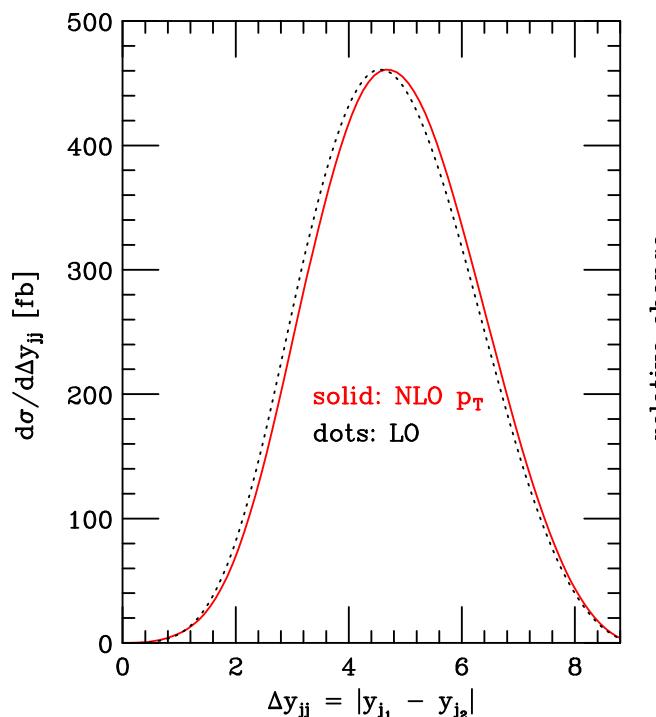
## QCD corrections to $gg \rightarrow H$



- ✓ Huge improvement in recent years
- ✓ Remaining scale uncertainty **below 10%**
- ✓ Uncertainty from gluon pdf  $\approx 4 - 7\%$
- ✗ What is K-factor for cross section with cuts?  
Most problematic: central jet veto against  $t\bar{t}$  background for  $H \rightarrow WW$  search

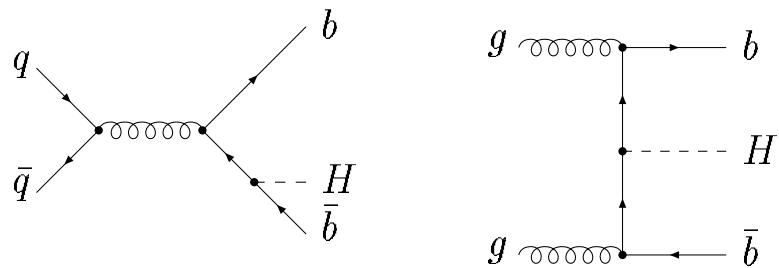
## NLO QCD corrections to WBF

- ✓ Small QCD corrections of order 10%
- ✓ Tiny scale dependence of NLO result
  - $\pm 5\%$  for distributions
  - $< 2\%$  for  $\sigma_{\text{total}}$
- ✓ K-factor is phase space dependent
- ✓ QCD corrections under excellent control
- ✗ Need electroweak corrections for 5% uncertainty

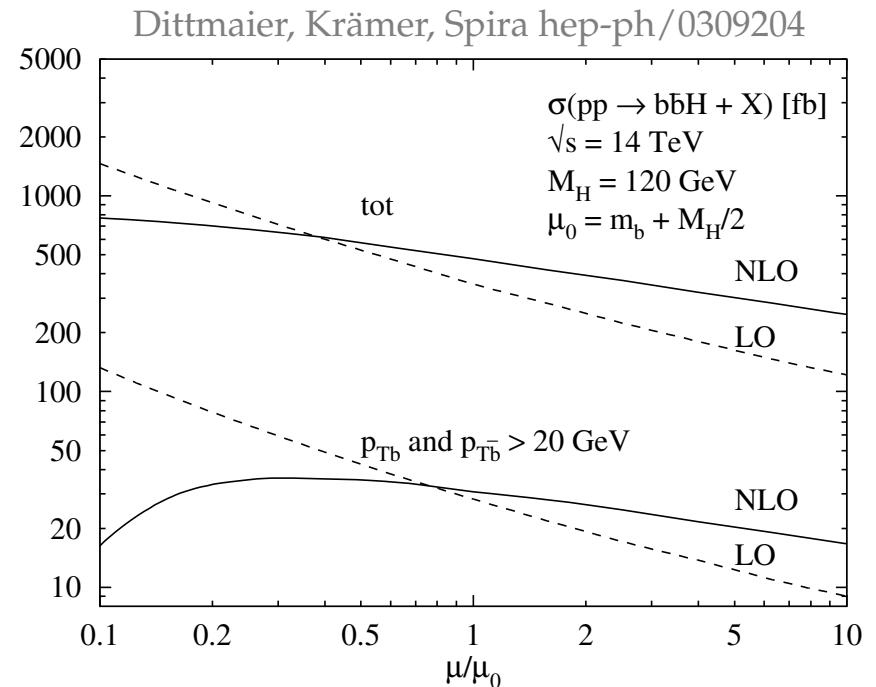


$m_H = 120 \text{ GeV}$ , typical WBF cuts

## NLO QCD corrections to $b\bar{b}H$ production



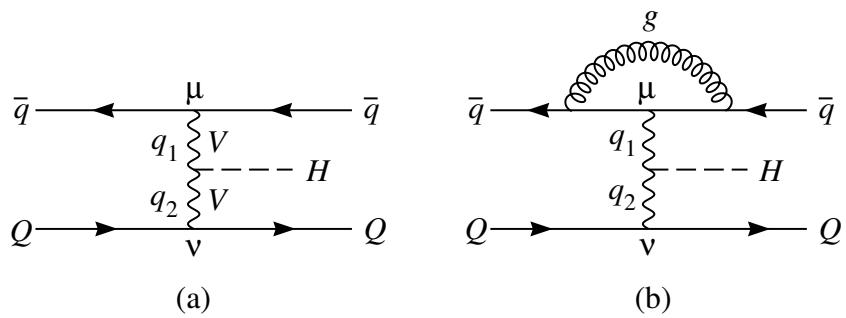
- Discovery channel for H/A in the MSSM at sizeable  $\tan \beta$
- NLO corrections known for  $\bar{b}bH$  final state
- b-quarks at low  $p_T$ : effective process is  $\bar{b}b \rightarrow H$ : cross section known at NNLO  
**Harlander, Kilgore (2003)**



scale dependence of inclusive vs.  
double b-tagged cross section

## Tensor structure of the $HVV$ coupling

Most general  $HVV$  vertex  $T^{\mu\nu}(q_1, q_2)$



$$T^{\mu\nu} = a_1 g^{\mu\nu} + \\ a_2 (q_1 \cdot q_2 g^{\mu\nu} - q_1^\nu q_2^\mu) + \\ a_3 \epsilon^{\mu\nu\rho\sigma} q_{1\rho} q_{2\sigma}$$

The  $a_i = a_i(q_1, q_2)$  are scalar form factors

Physical interpretation of terms:

**SM Higgs**       $\mathcal{L}_I \sim HV_\mu V^\mu \longrightarrow a_1$

loop induced couplings for neutral scalar

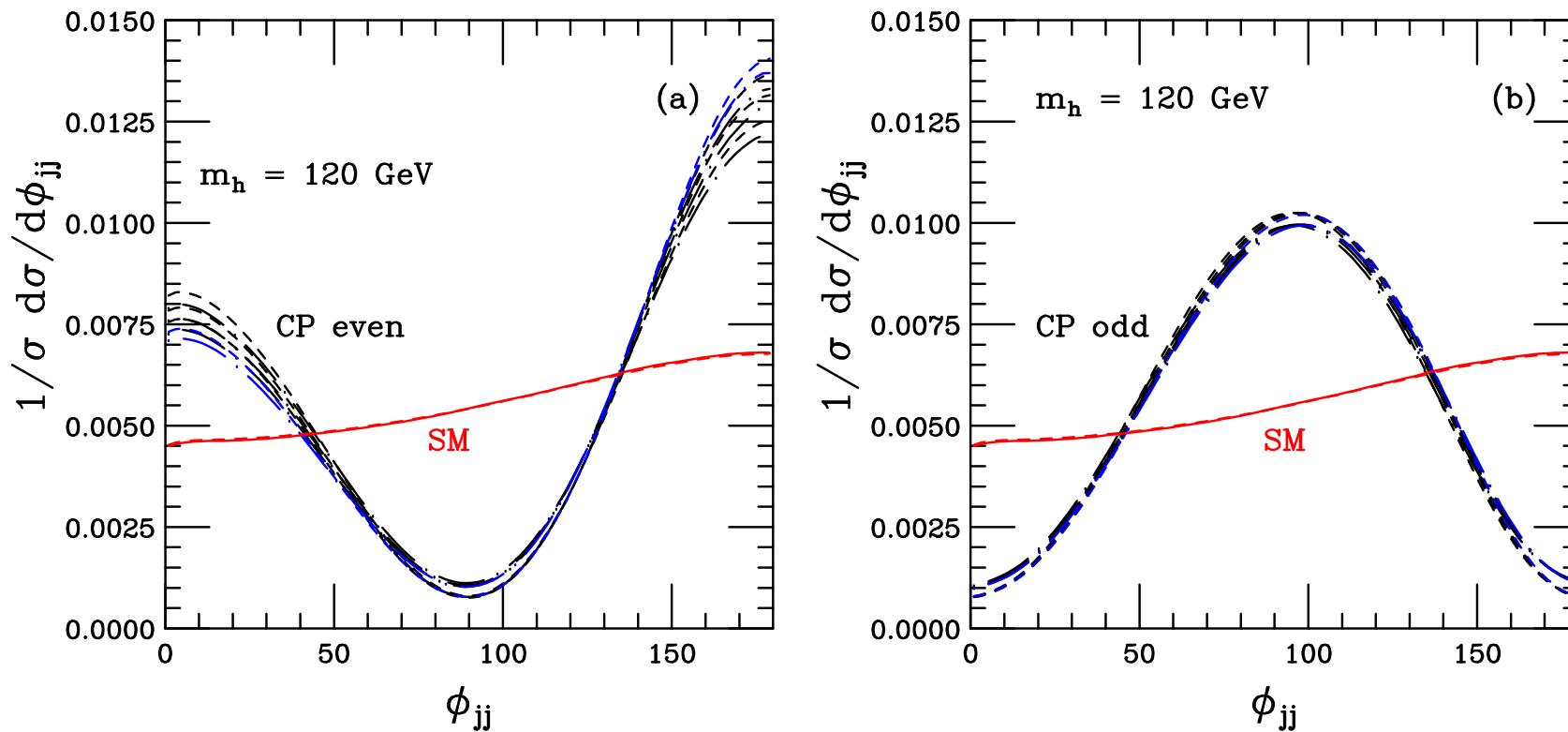
**CP even**       $\mathcal{L}_{eff} \sim HV_{\mu\nu} V^{\mu\nu} \longrightarrow a_2$

**CP odd**       $\mathcal{L}_{eff} \sim HV_{\mu\nu} \tilde{V}^{\mu\nu} \longrightarrow a_3$

Must distinguish  $a_1, a_2, a_3$  experimentally

## Azimuthal angle correlations

Tell-tale signal for non-SM coupling is azimuthal angle between tagging jets



Dip structure at  $90^\circ$  (CP even) or  $0/180^\circ$  (CP odd) only depends on tensor structure of  $HVV$  vertex. Very little dependence on form factor, LO vs. NLO, Higgs mass etc.

## Probing the Higgs potential

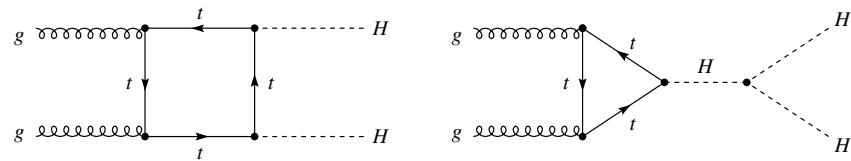
$$V(\Phi) = \lambda \left( \Phi^\dagger \Phi - \frac{v^2}{2} \right)^2$$

$\sigma(gg \rightarrow HH) \approx 20 - 30 \text{ fb at } 14 \text{ TeV}$   
 Gianotti et al., hep-ph/0204087

$\Rightarrow$  Higgs mass:  $m_H^2 = 2\lambda v^2$

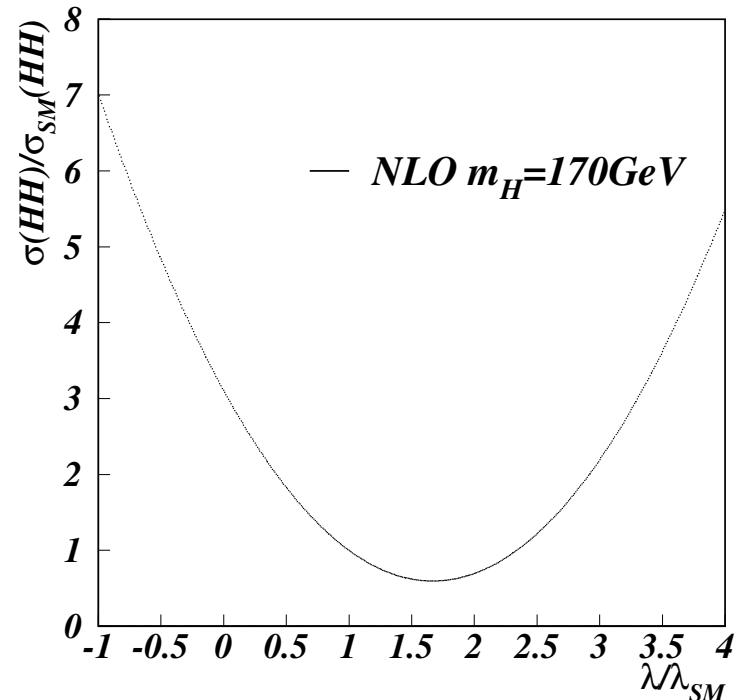
HHH coupling:  $6\lambda v = 3m_H^2/v$

Probe this relation in  $gg \rightarrow HH$



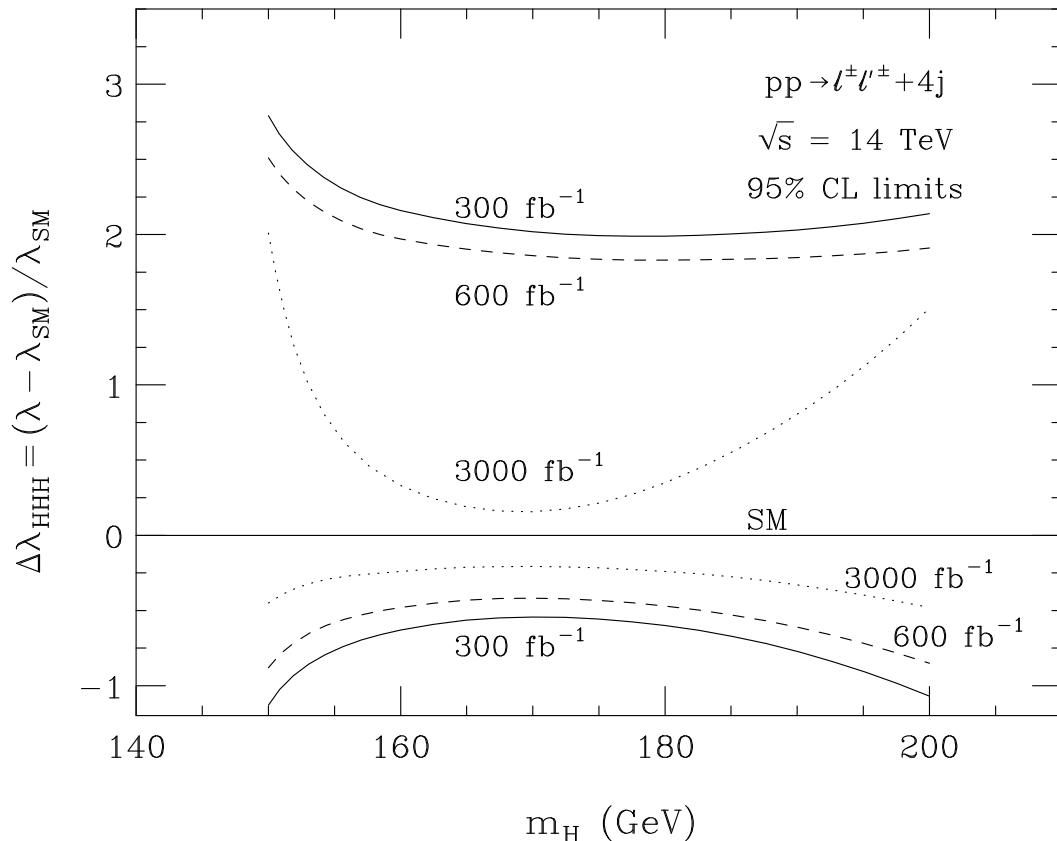
Most sensitive decay channel:

$$\begin{aligned} HH &\rightarrow W^+W^-W^+W^- \\ &\rightarrow l^\pm l'^\pm + 4j + p_T \end{aligned}$$



## LHC sensitivity to $HHH$ coupling

Baur, Plehn, Rainwater: hep-ph/0211224



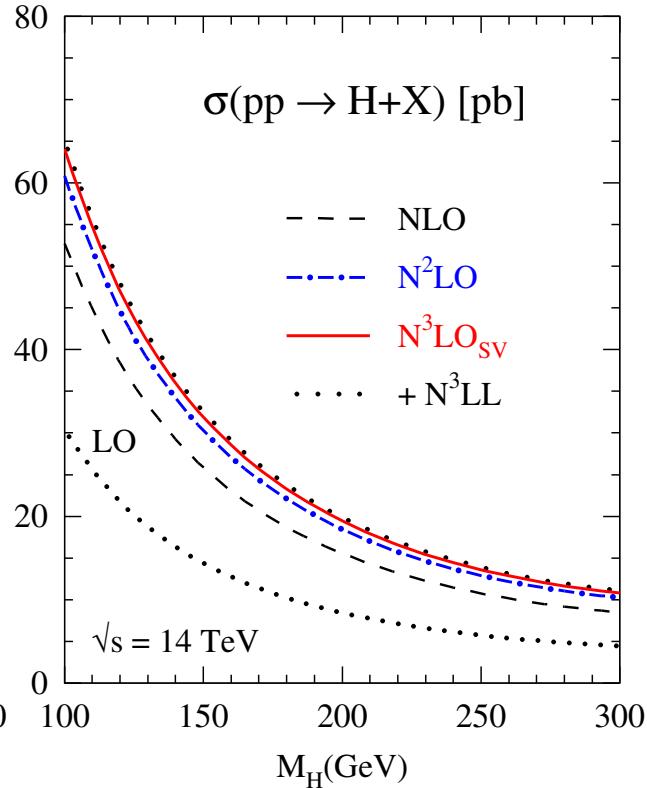
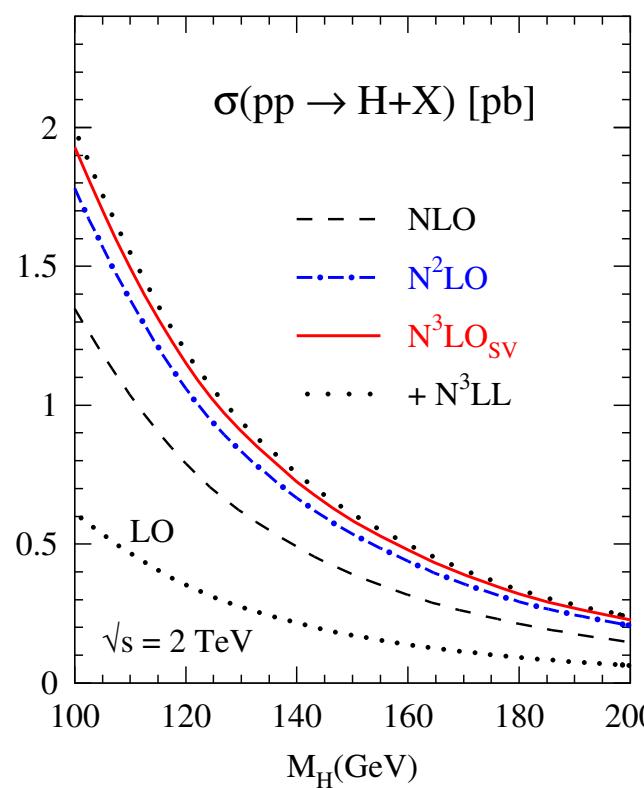
- Need very high luminosity for serious measurement of self coupling
- SLHC sensitivity: up to  $\pm 20\%$

## Conclusions

- LHC will observe a SM-like Higgs boson in multiple channels, with 5 ... 20% statistical errors  
     $\Rightarrow$  great source of information on Higgs couplings
- Extraction of couplings at the LHC requires knowledge of NLO QCD corrections for signal and important backgrounds
- Absence of  $HVV$  and  $AVV$  couplings for the heavy  $H/A$  of supersymmetry make their observation more challenging  
     $\Rightarrow$  Need large  $\tan \beta$  rate enhancement for discovery
- Higgs boson CP properties from jet-angular correlations in WBF and gluon fusion
- Higgs boson self couplings are big challenge: SLHC may give information for favorable Higgs mass range ( $m_H > 160$  GeV) in which  $HH \rightarrow WWW$  observation is possible

## QCD corrections to $gg \rightarrow H$

Moch & Vogt, hep-ph/0508265



Cross section as function  
of  $m_H$  for Tevatron and  
LHC