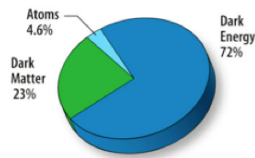
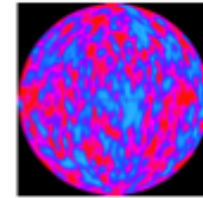


WE HAVE LEARNED

1. The standard cosmological model



$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3c^2}\rho - \frac{c^2 K}{a^2} + \frac{c^2 \Lambda}{3}$$

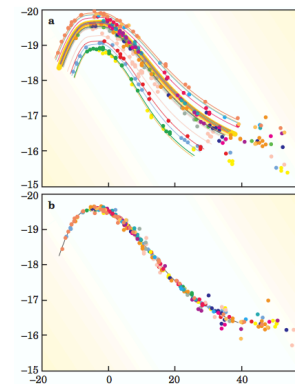
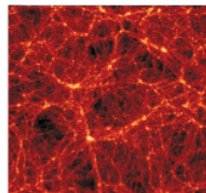


2. Growth of density fluctuations



$$\sigma^2(M) = \frac{1}{2\pi^2} \int P(k)W^2(kR)k^2 dk$$

3. The nature of dark matter



4. Mysterious dark energy

その前に: ダークエネルギーの進化

アインシュタイン方程式にFRW計量を入れると

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3c^2}\rho - \frac{c^2 K}{a^2} + \frac{c^2 \Lambda}{3}$$

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3c^2}(\rho + 3p) + \frac{c^2 \Lambda}{3}$$

上の式を時間部分し、下の式を使うと

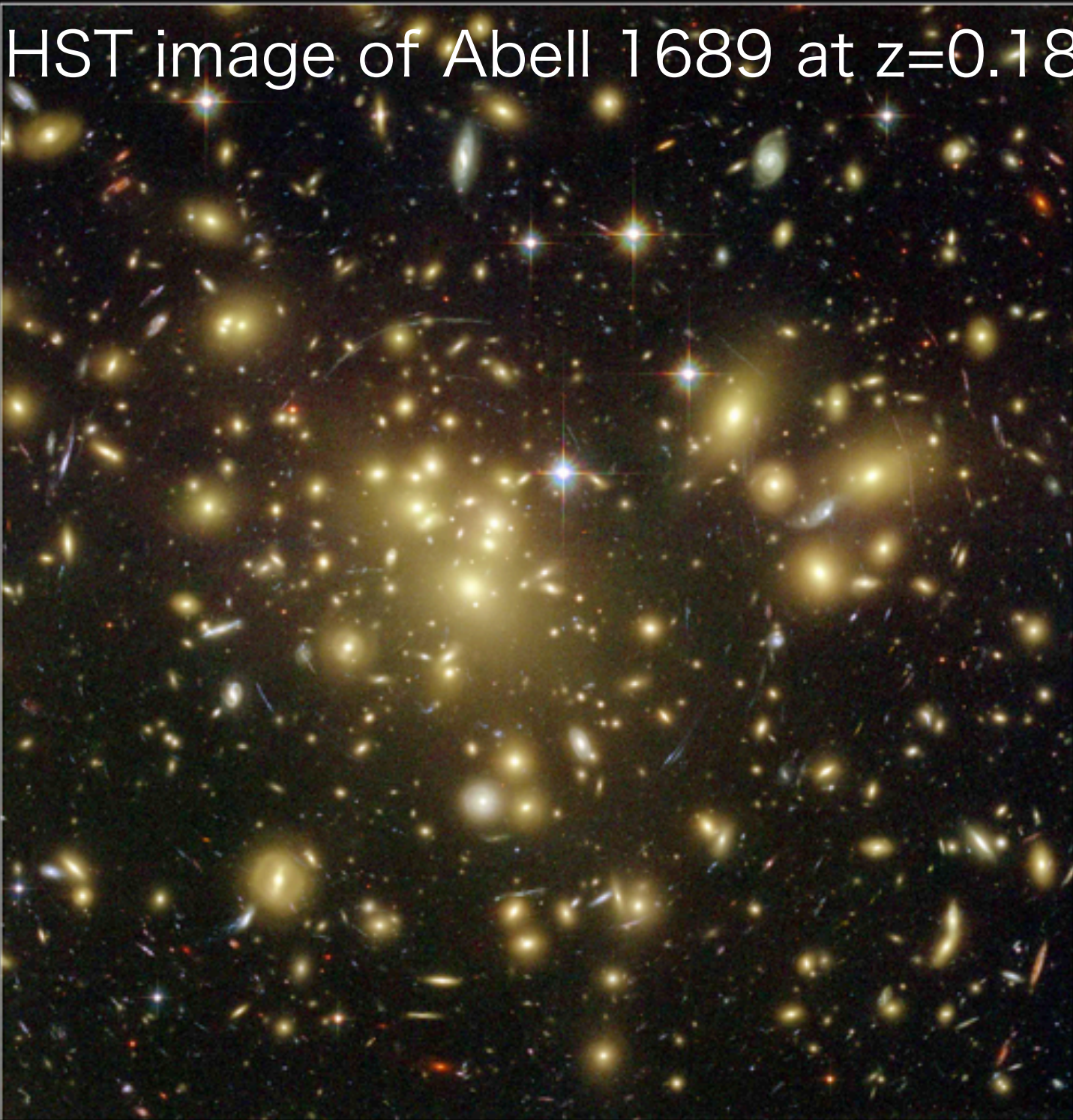
$$\dot{\rho} = -3(\rho + p)\frac{\dot{a}}{a} \quad (\text{密度の進化の式})$$

$p = w\rho$ に対しては

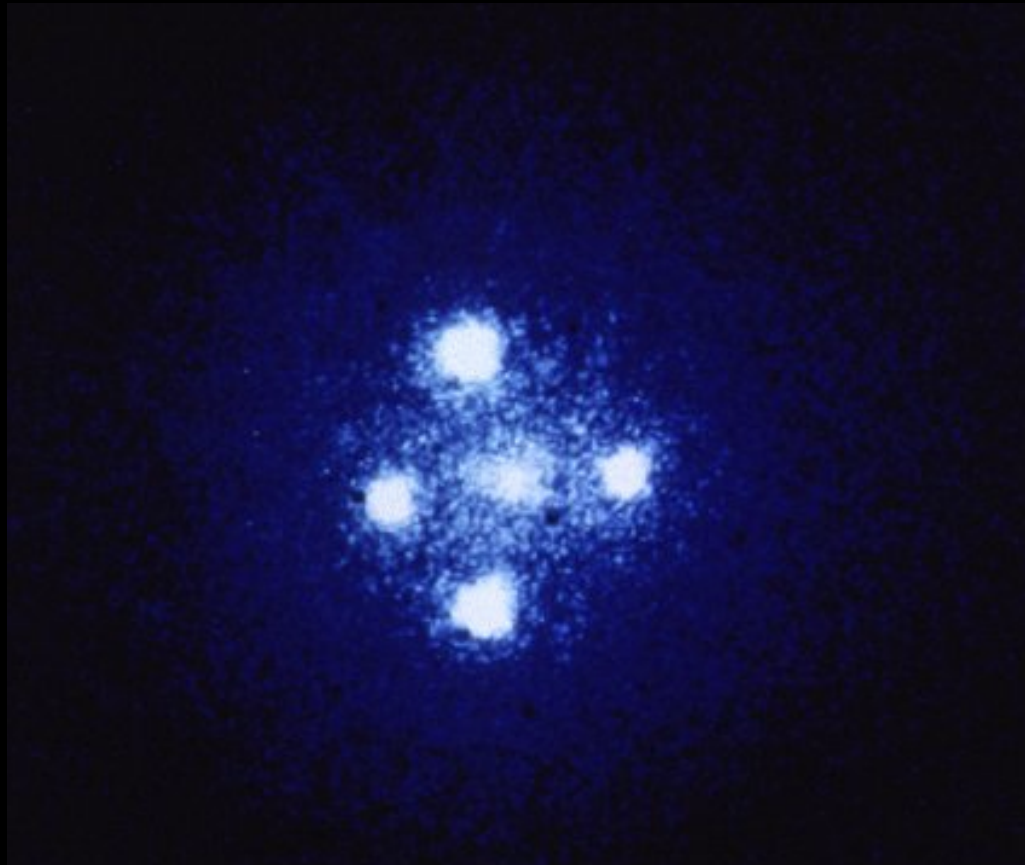
$$\rho \propto \exp\left(-3 \int \frac{da'}{a'}(1 + w(a'))\right)$$

重力レンズ宇宙論

HST image of Abell 1689 at $z=0.18$



QSO-galaxy lens

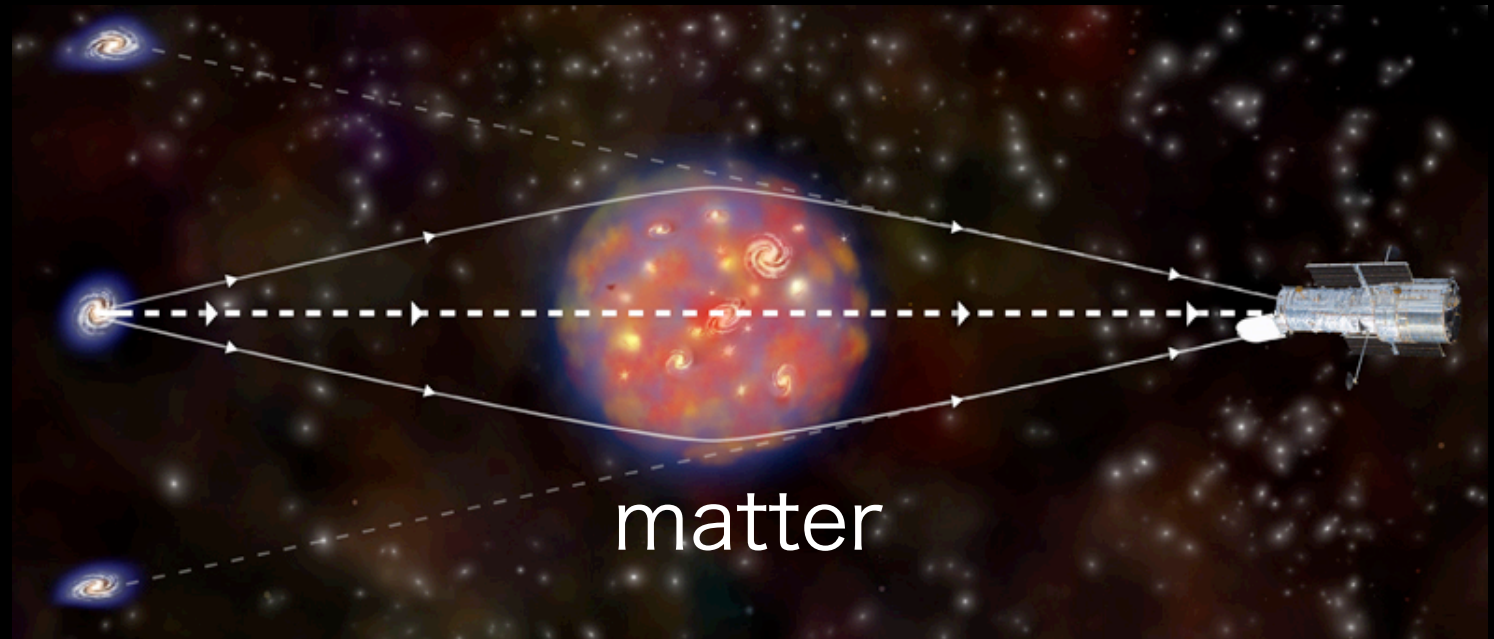
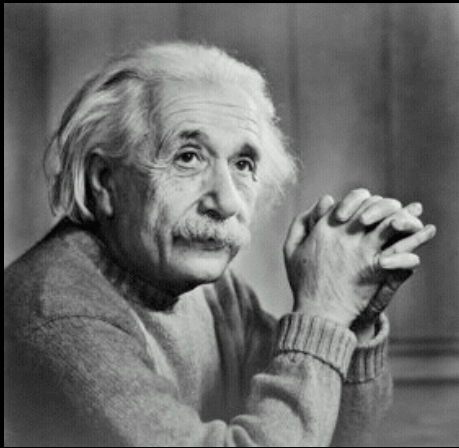


Galaxy-galaxy lens



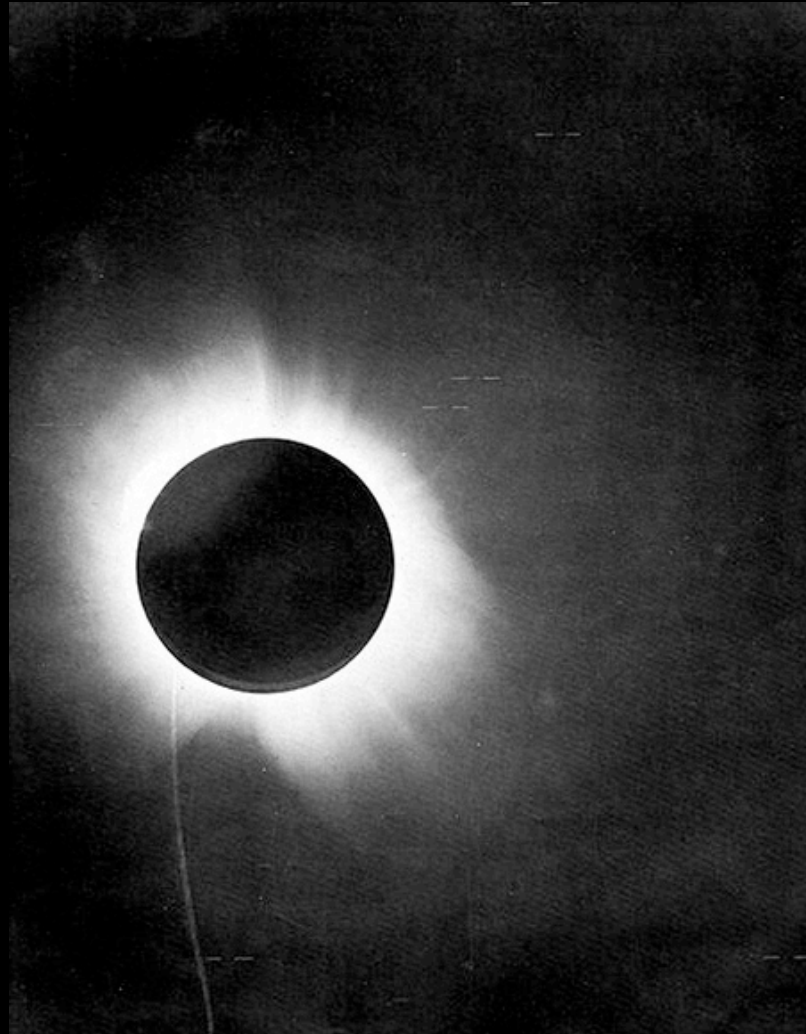
Gravitation lensing

General relativistic effect



Light rays are deflected near a massive object. (It is space-time that is curved.)

May 29, 1919



板書

Quiz 13: Deflection of light

Calculate the deflection angle for a light-ray passing through near the surface of the sun.

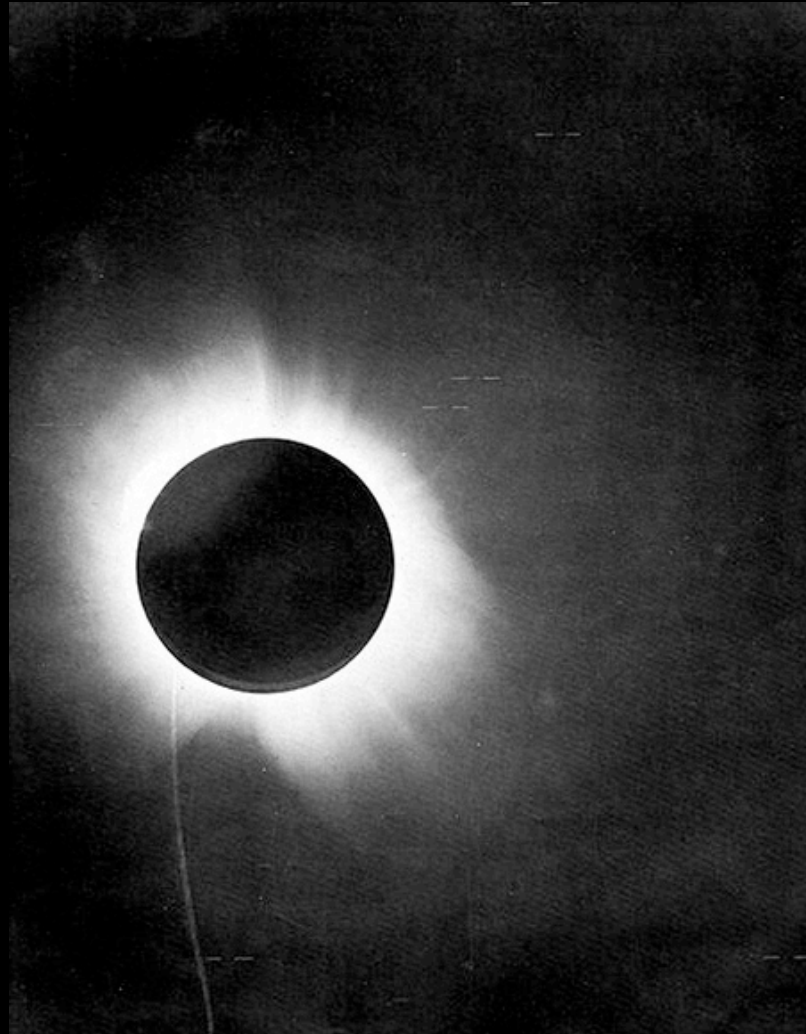
$$M_{\text{sun}} \sim 2 \times 10^{30} \text{ kg}, R_{\text{sun}} \sim 7 \times 10^5 \text{ km}$$

Calculate the typical deflection angle for a galaxy having an isothermal density profile

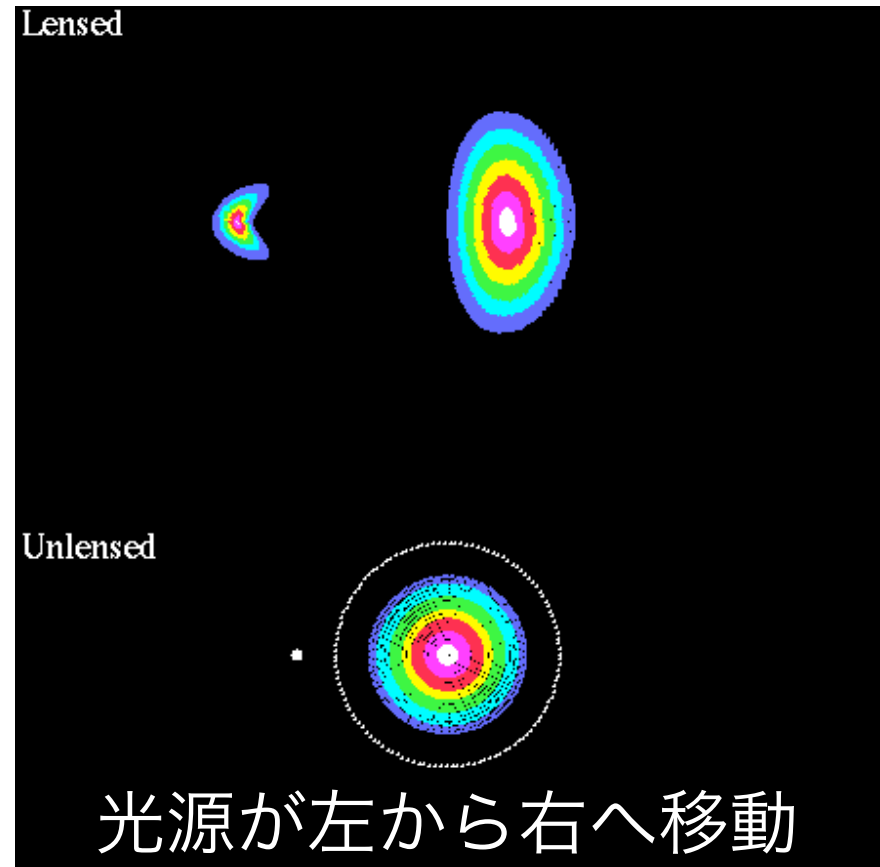
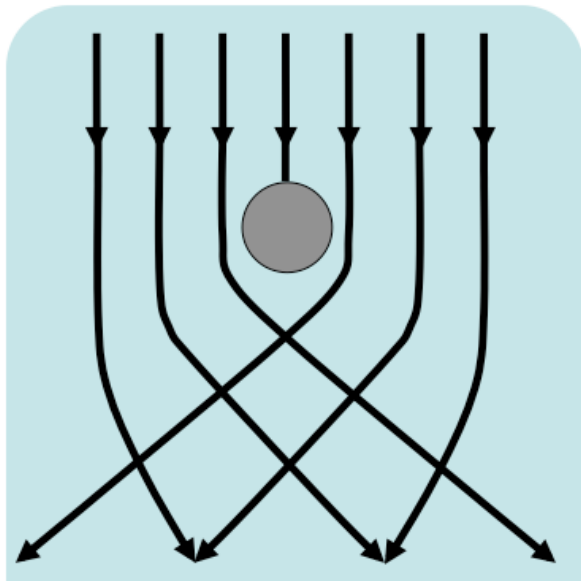
$$\rho(r) = C r^{-2}$$

$$\text{Use } M_{\text{gal}} \sim 10^{12} M_{\text{sun}}, R_{\text{gal}} \sim 100 \text{ kpc}$$

May 29, 1919



Different from optical lens



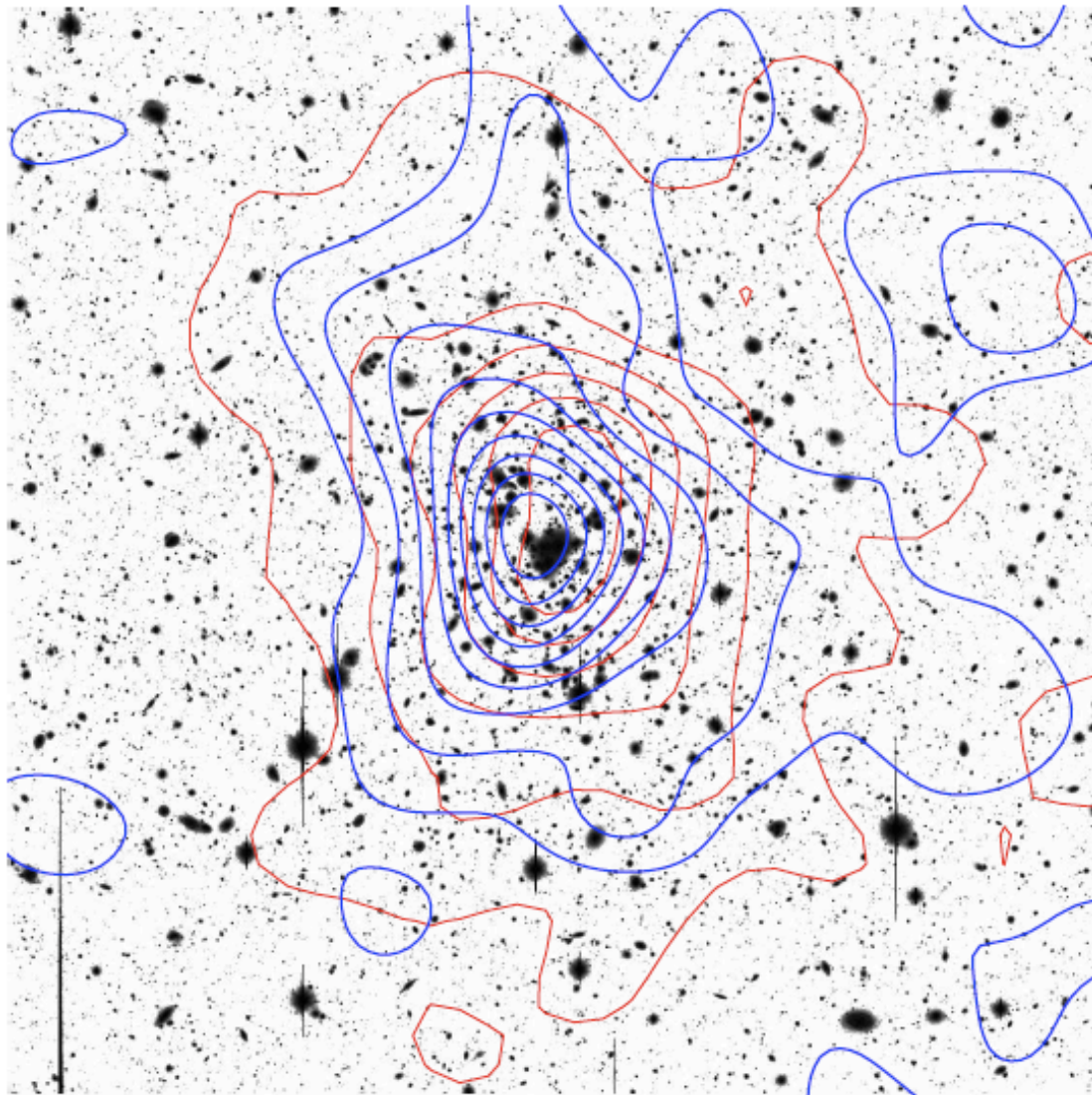
X-ray image of a cluster



Hot intra-cluster
plasma with $T \sim 10^7$ K
($M \sim 10^{14} M_{\text{sun}}$)

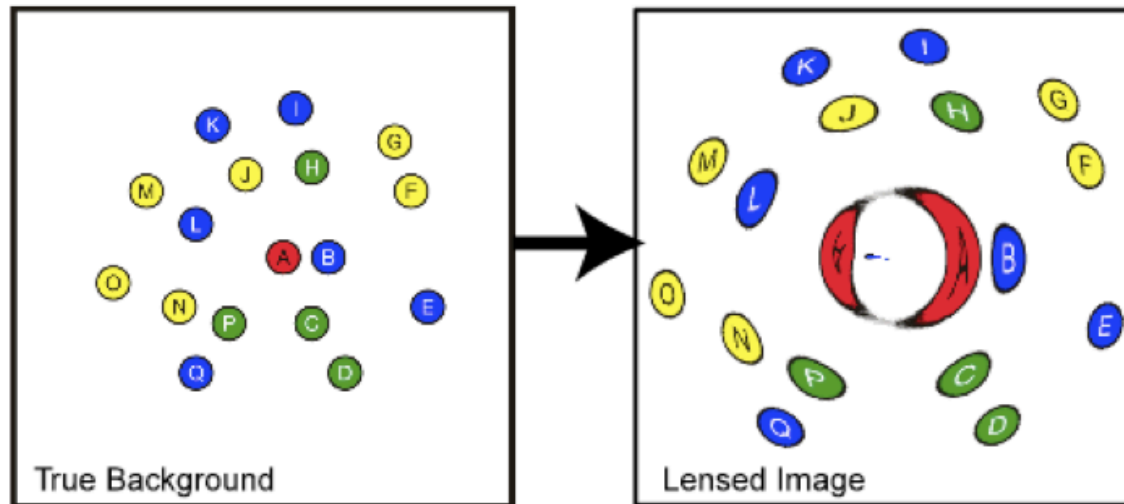
Still not enough to
cause gravitational
lensing.

Mass distribution



Blue contours show the mass distribution around the same cluster.

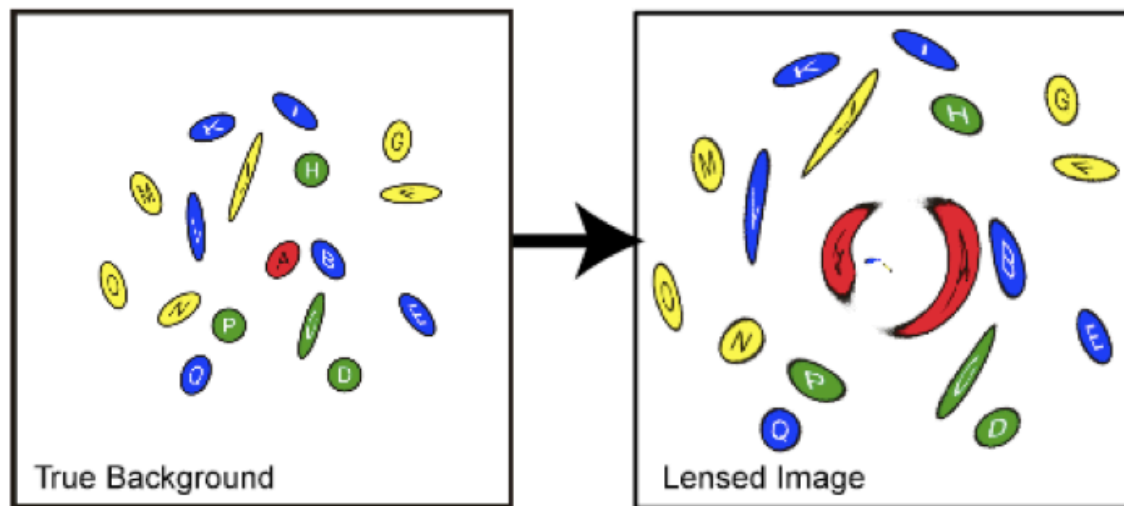
Weak lensing



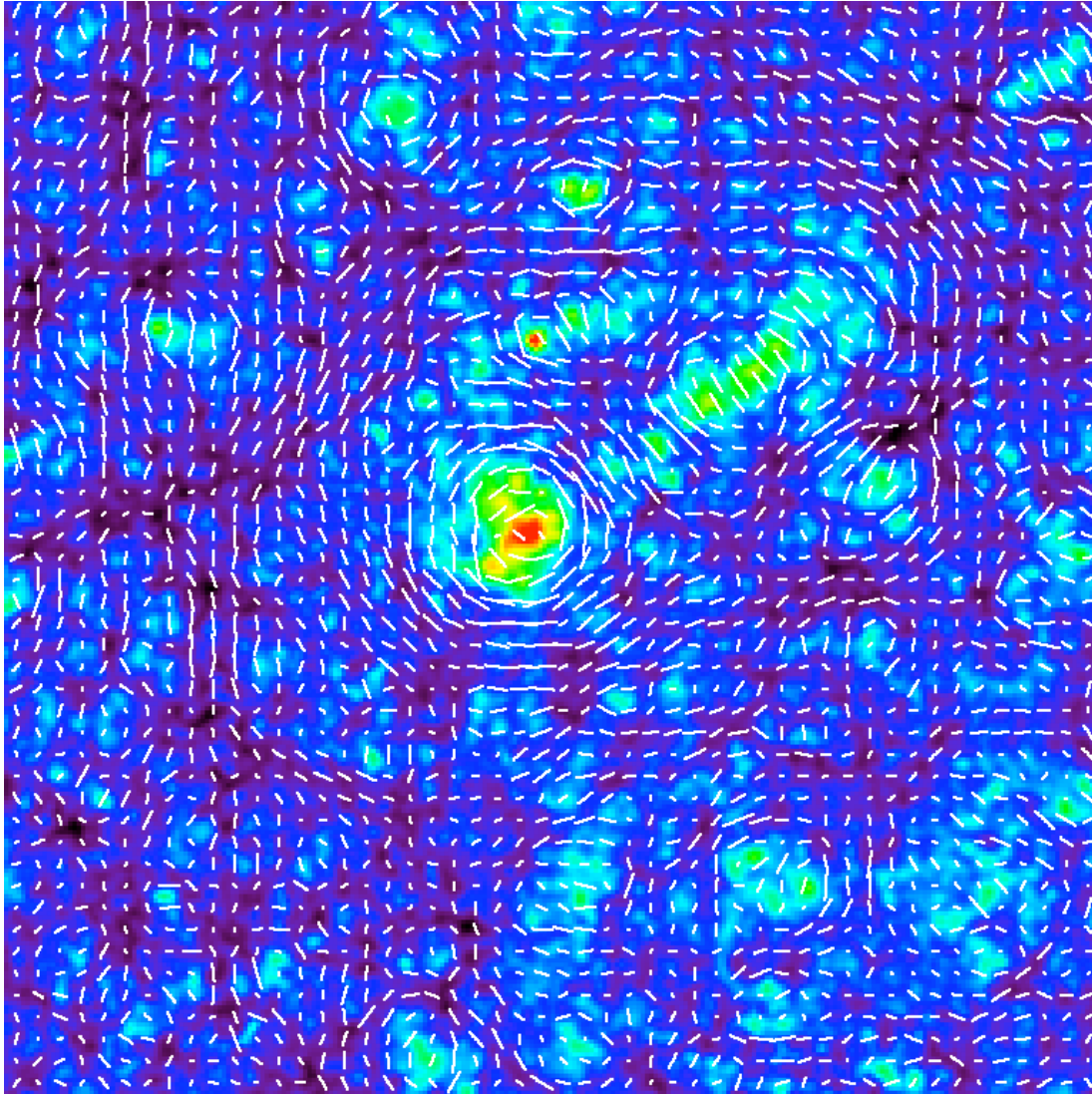
Images of background galaxies are magnified and distorted.

Strong lensing produces multiple lensed-images and large distortion.

Weak lensing causes small stretch and coherent alignment.

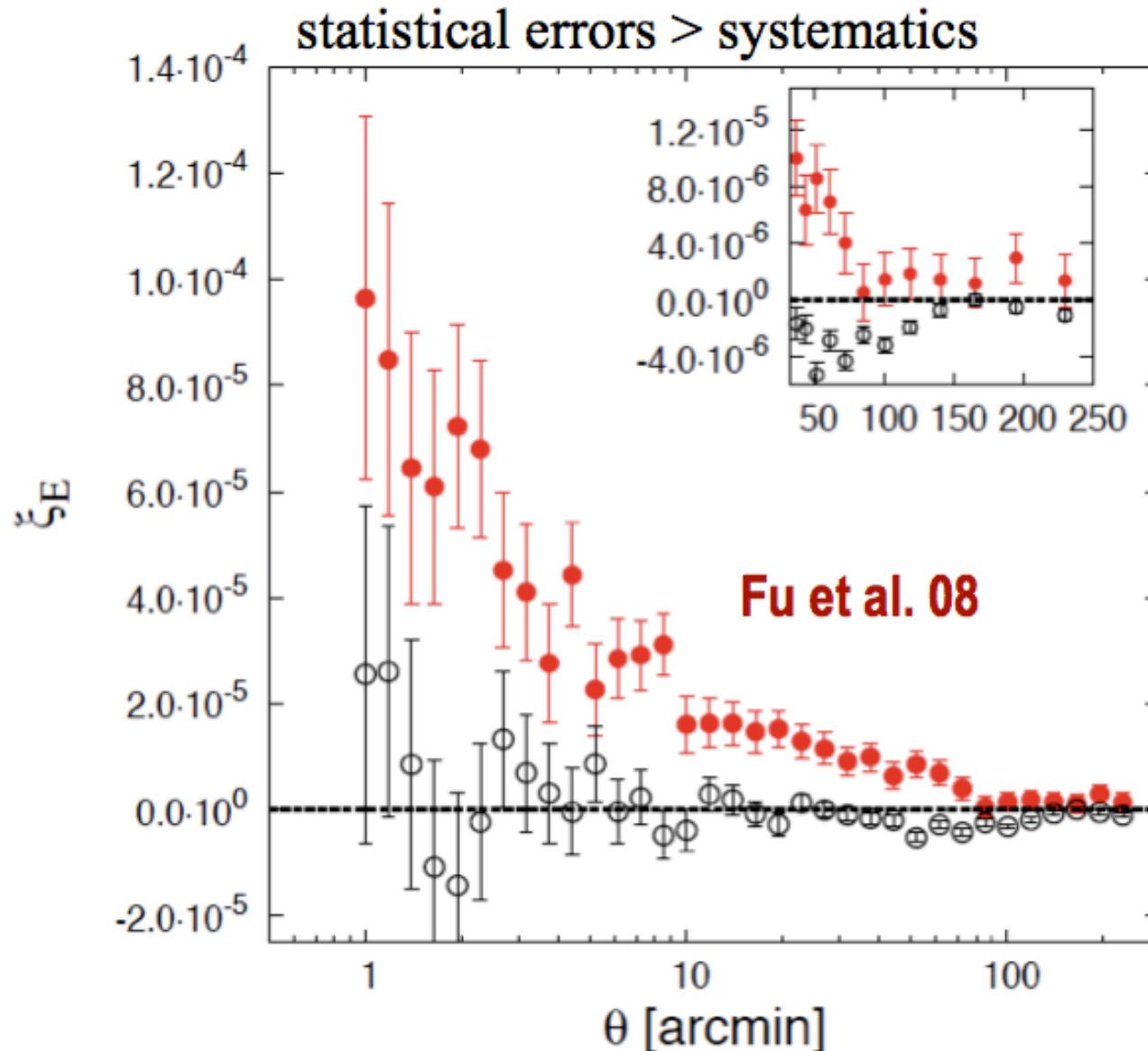


Lensing shear map



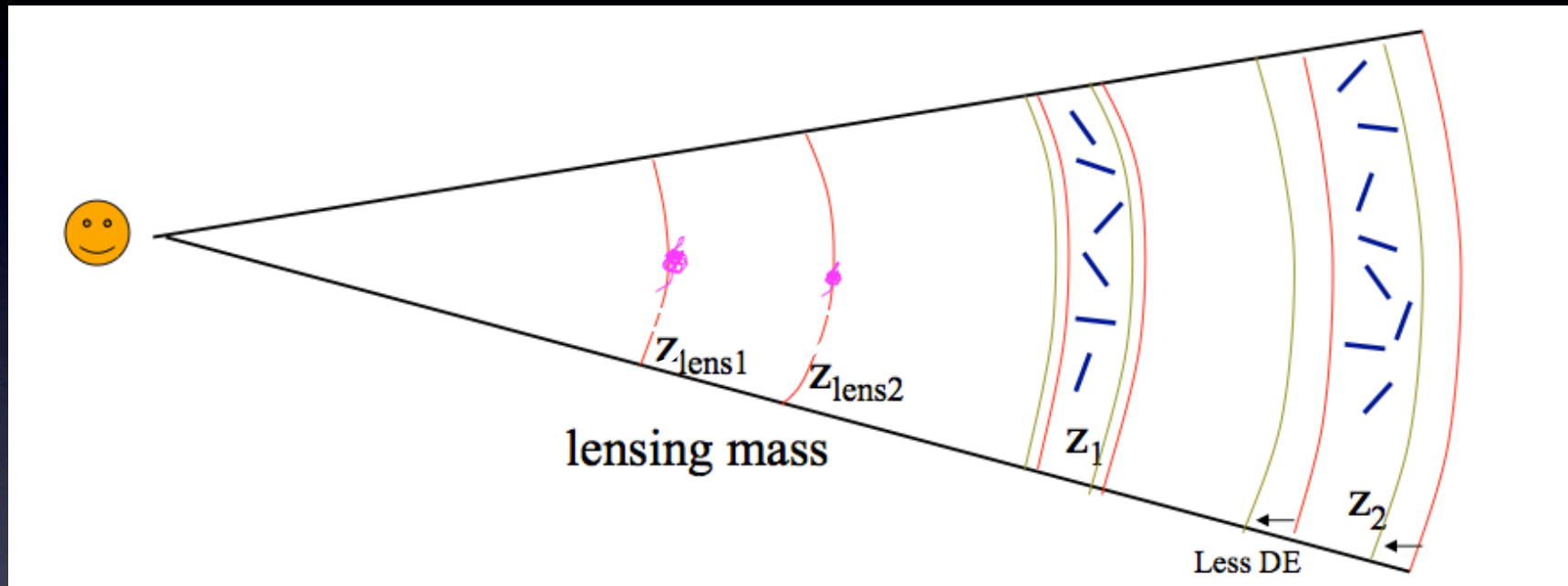
White lines show the amplitude and the direction of local shear
~ the 2nd derivative of the 2D (projected) gravitational pot.

The state-of-art: CFHT WL Survey



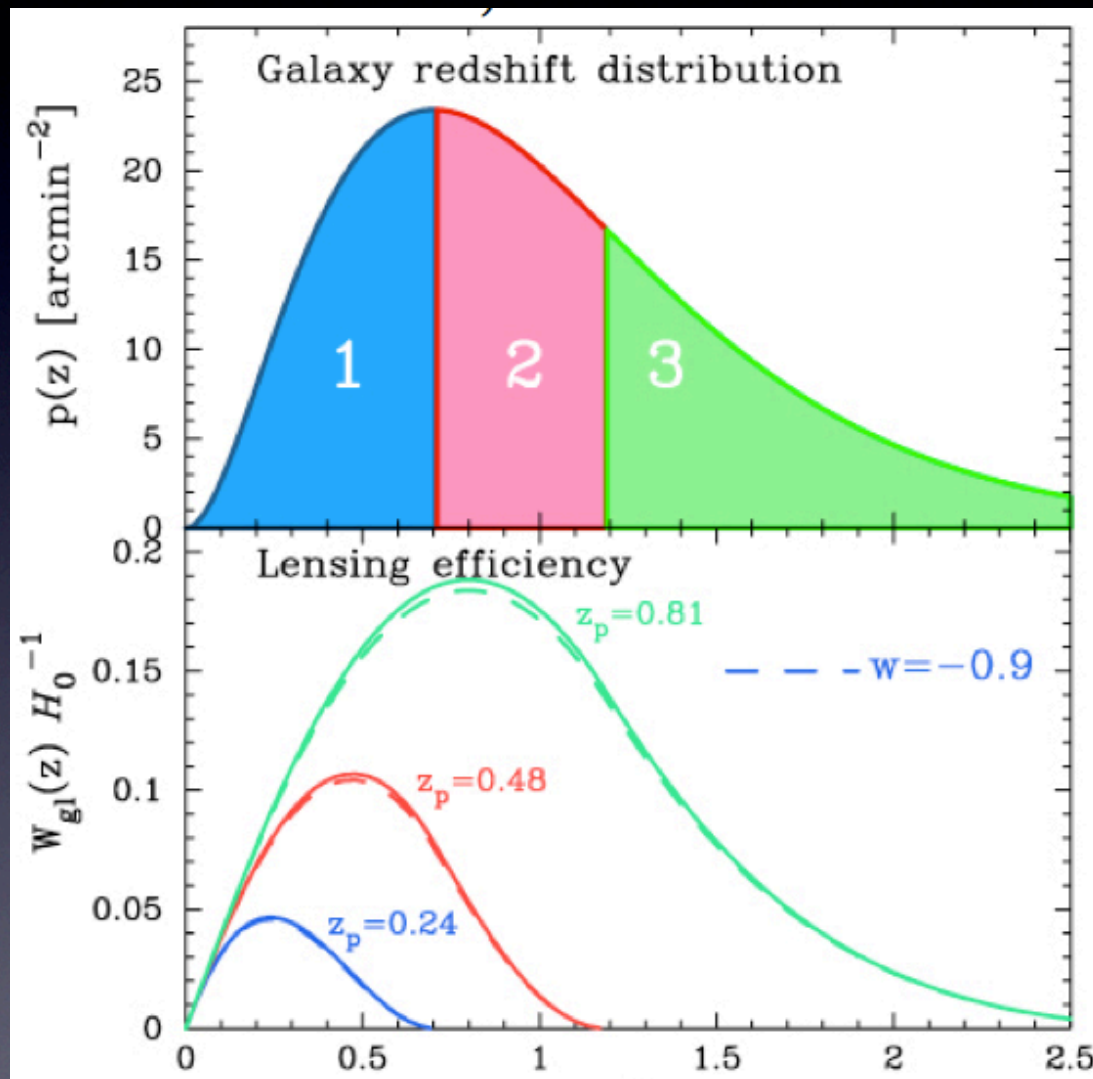
- ~ 60 sq deg²
(effective area: ~ 30 sq. deg²)
- $i'_{AB} \sim 24.5$,
 $\langle z \rangle \sim 0.9$
- Calibrate source redshift with the CFHT deep survey and the VVSD
- **$\sim 20\sigma$ detection**,
over a range of few arcminutes to a few degrees
- 170 deg² results will be released this year?

Lensing tomography



Selecting source galaxies by redshift enables to probe structure at different distances.

Lensing tomography

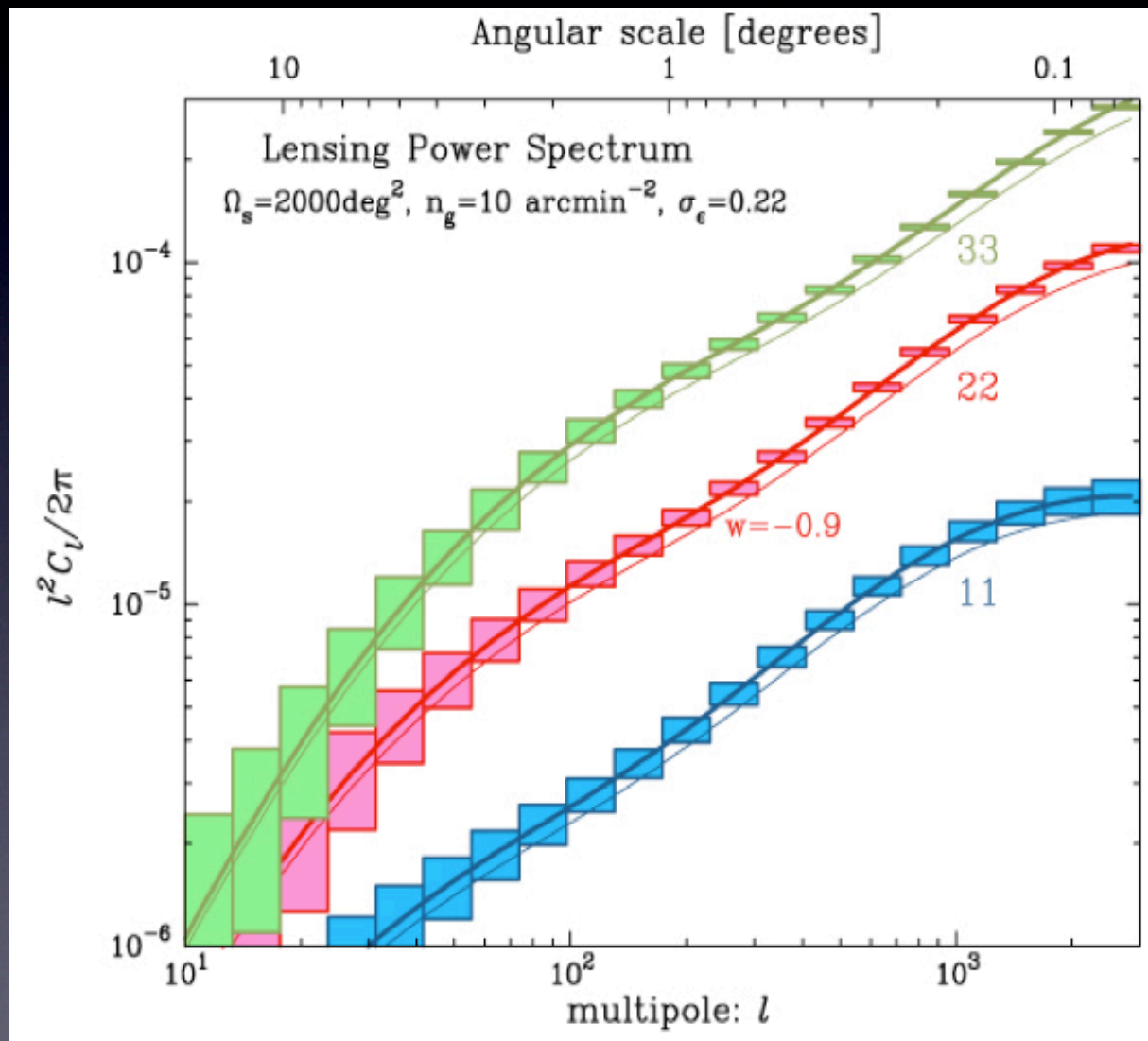


Lensing efficiency has a broad shape even for a single source redshift.



To do “coarse” tomography, one doesn’t need precise redshifts of all the source galaxies.

Power spectrum



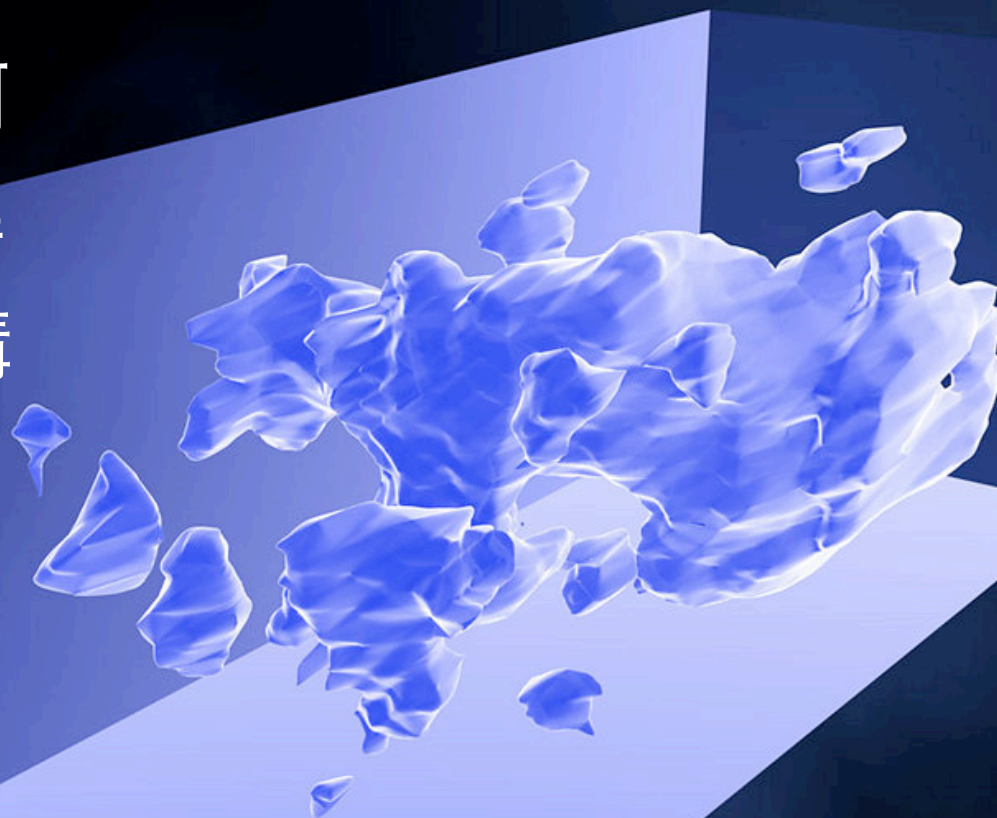
Exact shapes
less important.
(Featureless anyway)

The overall
amplitude and the
evolution
give strong
constraints on
cosmological
parameters.

遠方宇宙の暗黒物質の可視化

国際協同コスモスプロジェクト

120万個の銀河
の重力レンズ解
析から3次元構
造を再構築

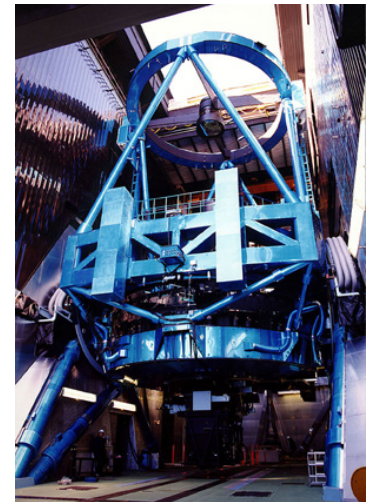
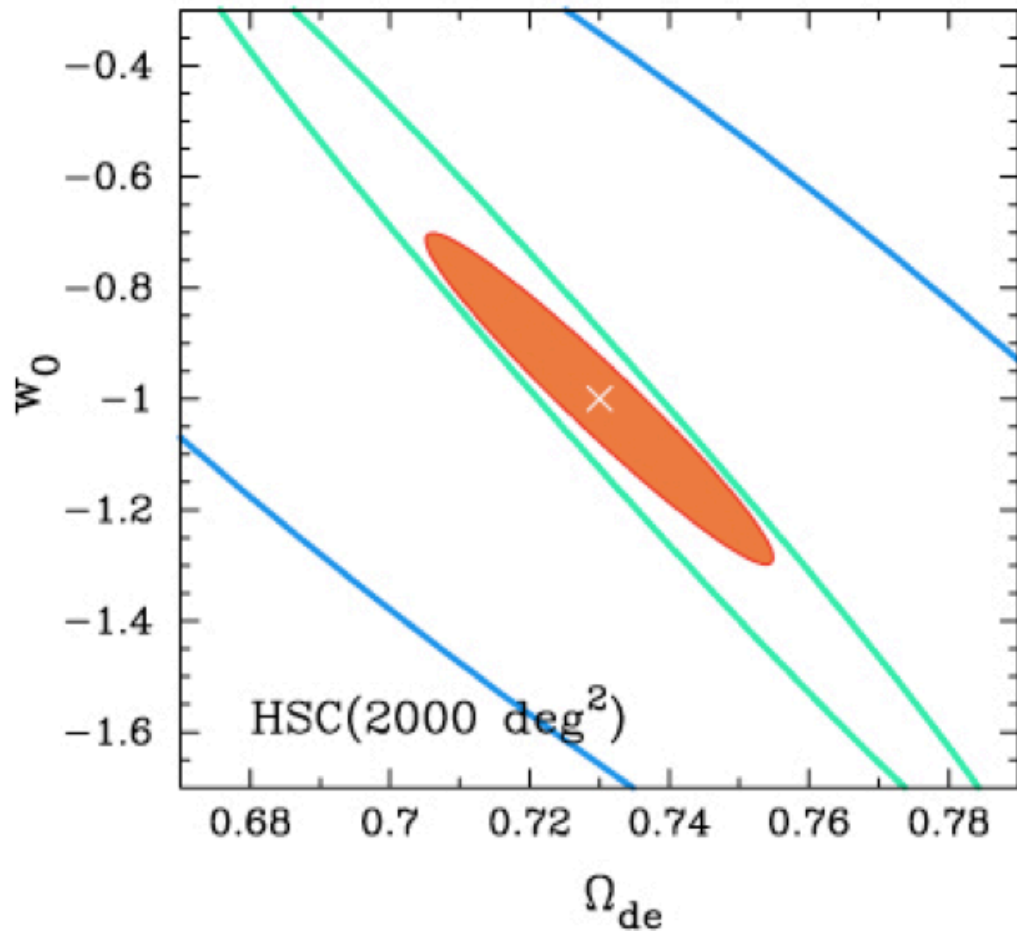


Massey et al. 2007, Nature

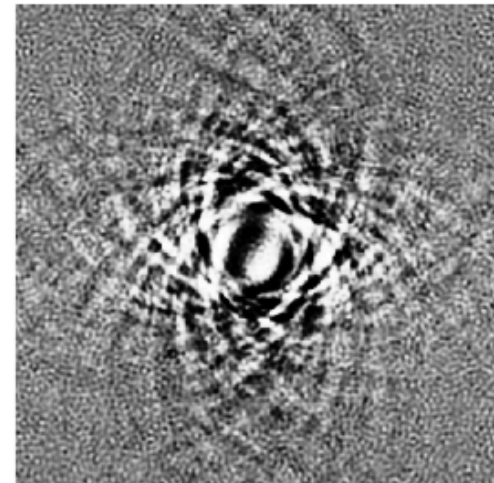
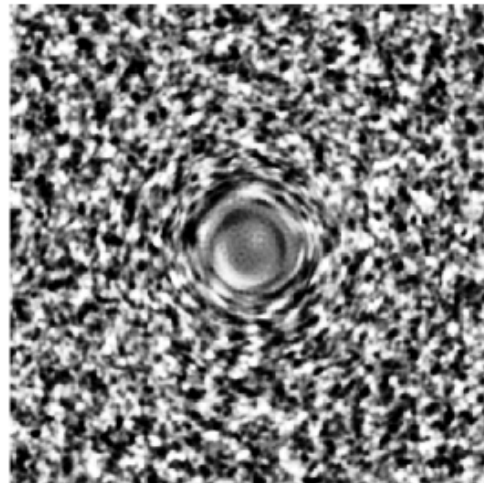
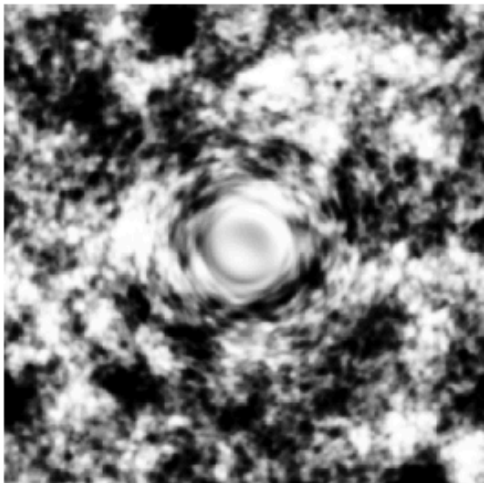
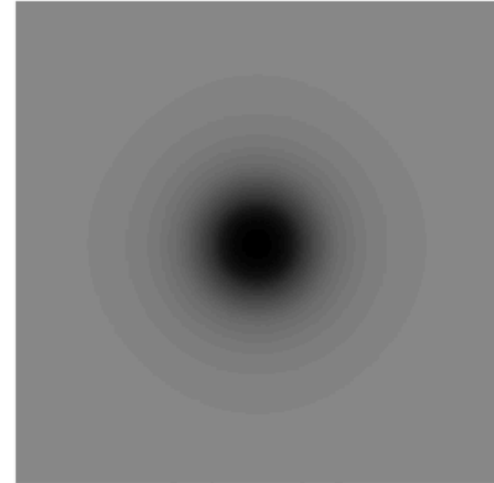
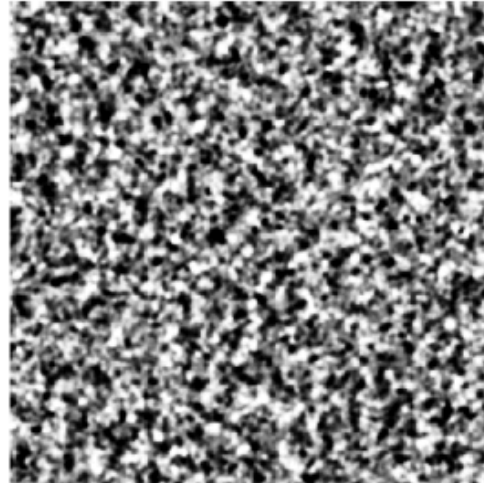
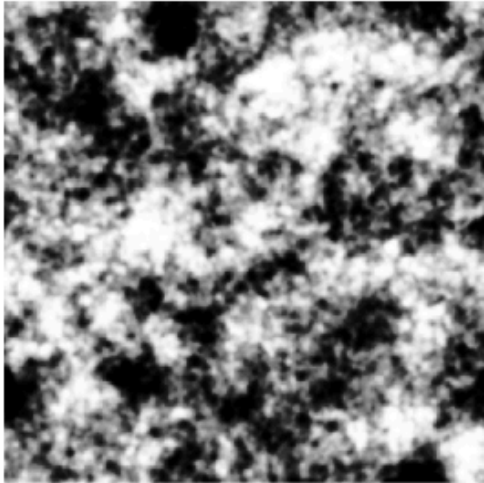
Probing dark energy

Weak lensing tomographic surveys will probe the growth of large-scale structure, which in turn probes the equation of state of dark energy:

$$P = w \rho$$

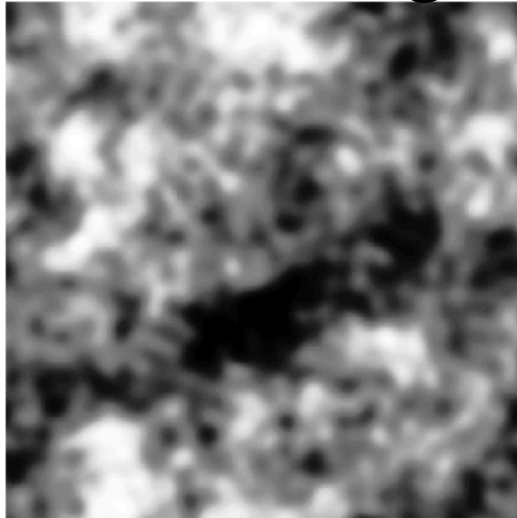


Sources other than galaxies I: CMB lensing

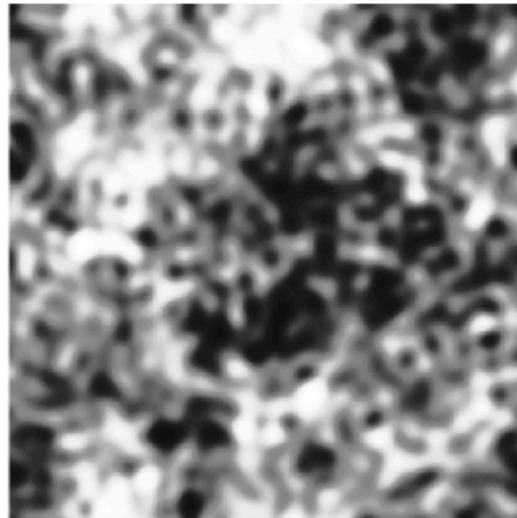


Sources other than galaxies I: CMB lensing

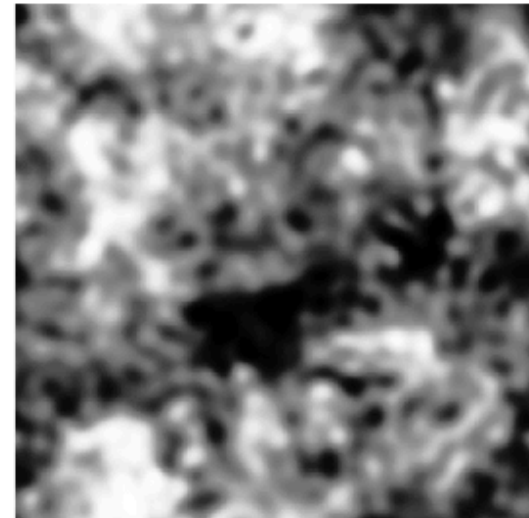
10x10 deg²



QQ reconst.



EB reconst.



Okamoto-Hu02

Sources other than galaxies II: HI 21 cm lensing

Multiple lens planes as a function of frequency (redshift)

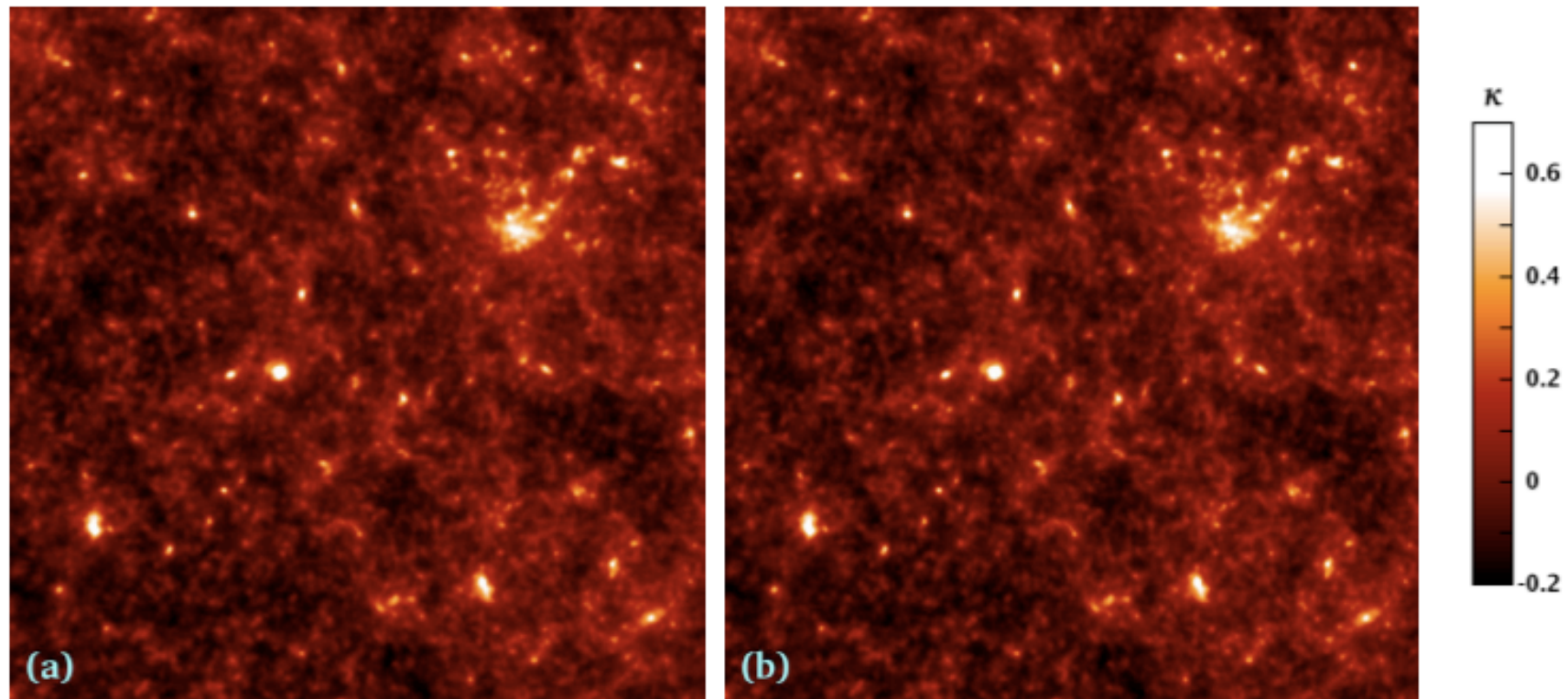


Figure 2. 21-cm-based convergence maps for the $20' \times 20'$ field shown in Fig. 1(a), but smoothed assuming a telescope beam with $\lambda = 6''$. Whereas (a) is noise-free, noise has been added in (b) at the irreducible value for a map of this resolution. The colour scale indicated by the bar at right is the same as in Fig. 1(a).