

ICEPP Symposium in Hakuba 2004/02/15

**Study of CP Violation
in $B^0 \rightarrow K_S^0$ at Belle**

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KEK

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Belle Collaboration



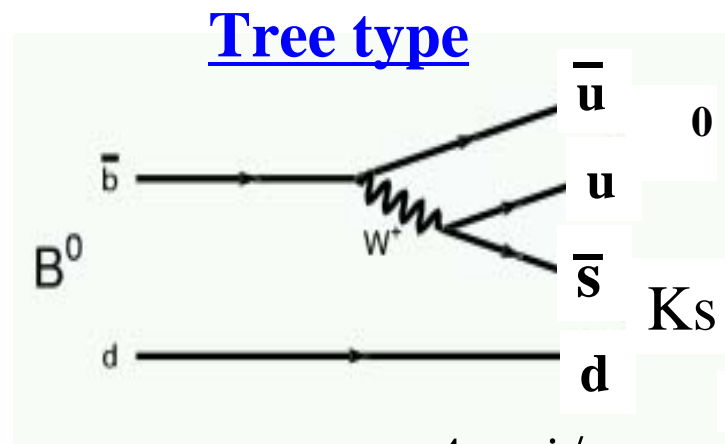
Introduction
to
 K_s^0 Mode



K_S^0 Mixing Indirect CP-Violation Mode likely
J K_S

$$A_{cp}(\Delta t) = \frac{\Gamma(\bar{B}^0 \rightarrow K_S \pi^0) - \Gamma(B^0 \rightarrow K_S \pi^0)}{\Gamma(\bar{B}^0 \rightarrow K_S \pi^0) + \Gamma(B^0 \rightarrow K_S \pi^0)}$$

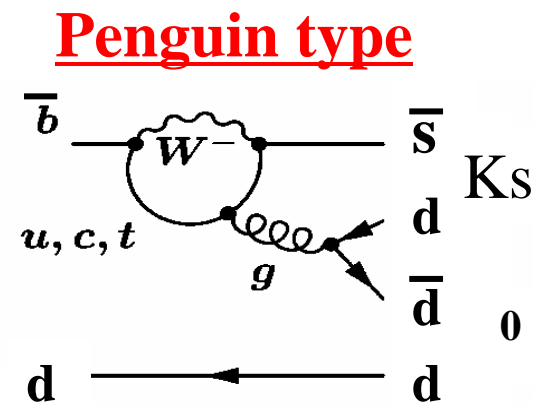
$$= A_{K_S \pi^0} \cdot \cos(\Delta m \Delta t) + S_{K_S \pi^0} \cdot \sin(\Delta m \Delta t)$$



$$\Gamma \propto A \lambda^4 e^{-i\phi_3}$$

$$\lambda = 0.22$$

→ Very Small Effect

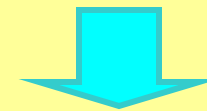


$$\ll \Gamma \propto A \lambda^2$$

(no phase)

→ Dominant!

In
Standard Model

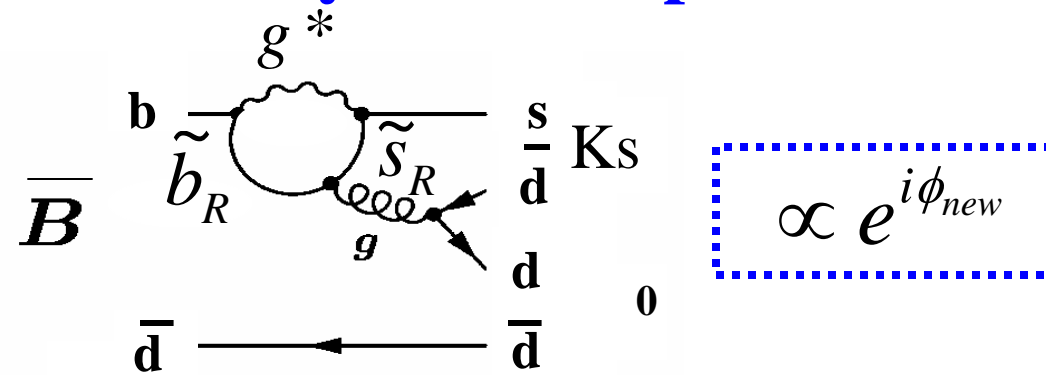


$$A_{K_S \pi^0} = 0$$

$$S_{K_S \pi^0} = \sin 2\phi_1$$

Physical Motivation

If New Physics in loop ...

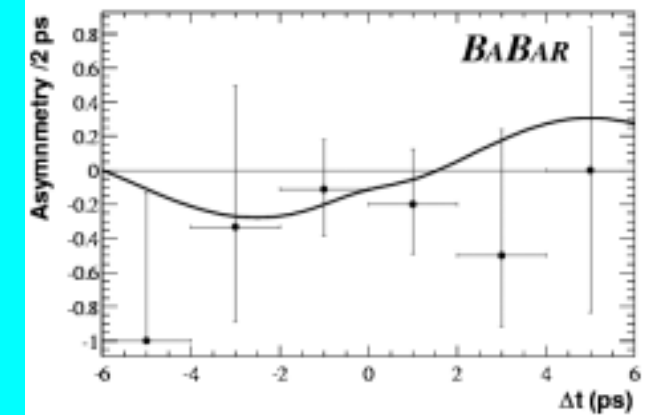
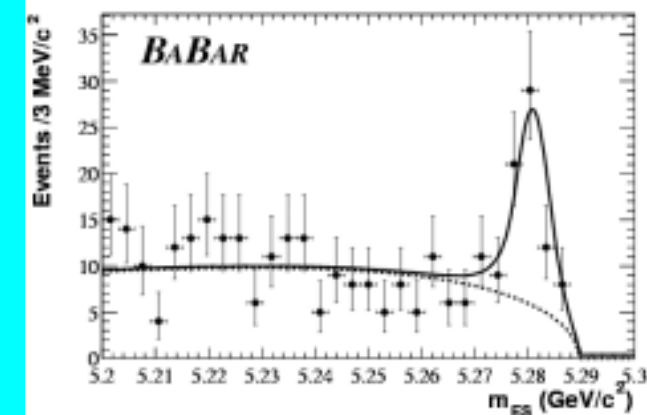


$$S_{Ks\pi^0} \propto \sin 2\phi_1$$

$$\phi_1 \rightarrow \phi_1 + \phi_{\text{new-physics}}$$

Ks 0 is sensitivity for new physics in loop diagram.

BaBar Result of LP03



Events = 122 ± 1

$$A_{Ks\pi^0} = 0.40^{+0.27}_{-0.28} \pm 0.10$$

$$S_{Ks\pi^0} = 0.48^{+0.38}_{-0.47} \pm 0.11$$

Today's Topics

Event Selection & Signal Yield

Analysis process

B⁰ reconstruction

- (1) Event Selection
- (2) Signal & Background Yield Extraction

CP-Fit Analysis

- (1) Define the Resolution of t for K_S^0 mode
- (2) t & CP-Asymmetry Fitting

KEK

Event Selection

**Ks & π^0
Selection**

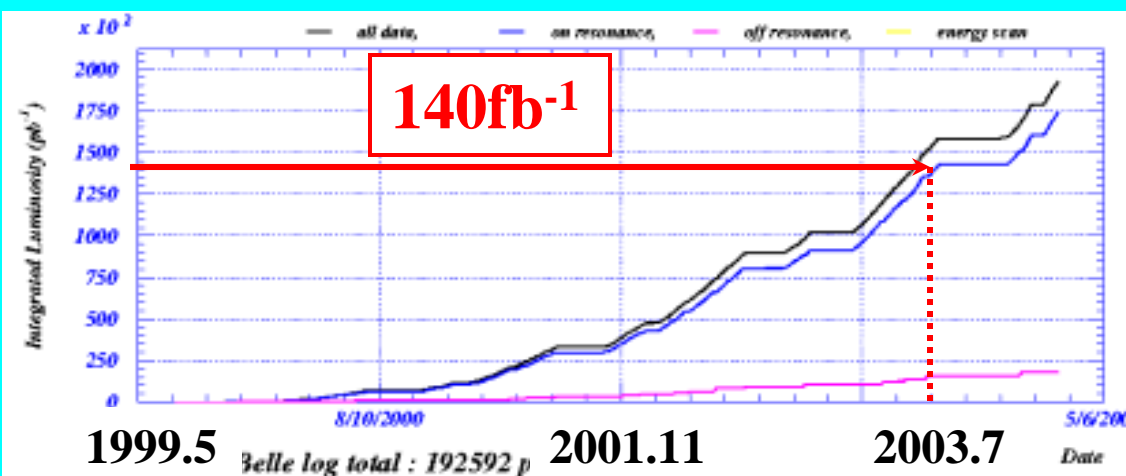
B0 Reconstruction

**Vertex
Reconstruction**

**Background
Rejection**



Data Sample for Analysis



$$\frac{(\text{Luminosity})dt}{= 140\text{fb}^{-1}}$$

$$\#B\bar{B} = 150 \times 10^6$$

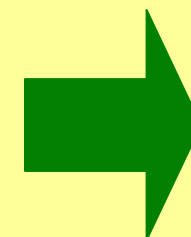
Estimate Events

$$\text{Br}(B^0 \rightarrow K_s^0) \sim 4 \times 10^{-6}$$

(Physics Letters B407(1997))

$$\text{Br}(B^0 \rightarrow K_s^+ K_s^-) \sim 98.8\%$$

$$\text{Br}(K_s^+ K_s^-) \sim 68.6\%$$



~ 400events
Efficiency=100%

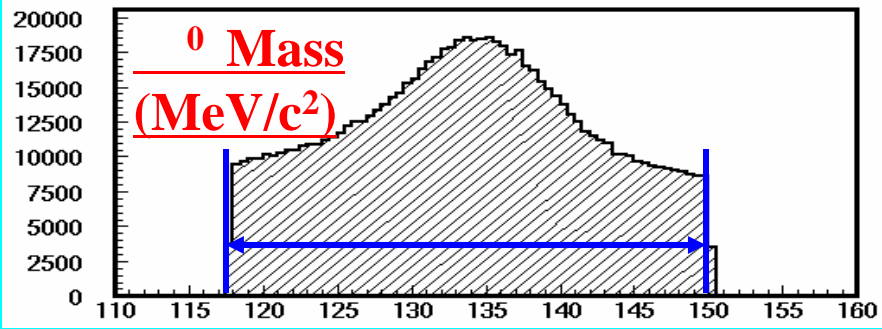
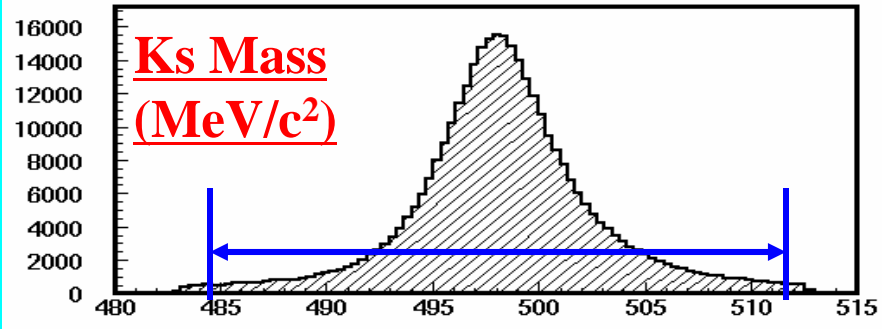
**Ks & 0
Selection**

**B0
Reconstruction**

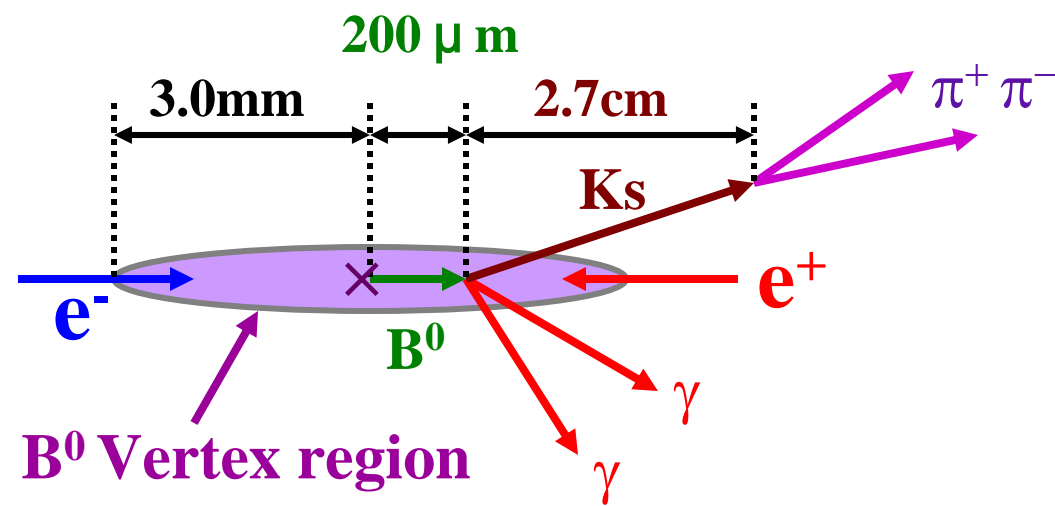
Ks + -
 $|M_{Ks} - 497.672| < 15 \text{ MeV}/c^2$
0
118 < M_{0} < 150 \text{ MeV}/c^2

Beam Constrained Mass
 $M_{bc} \equiv \sqrt{(E_{Beam}^{cms})^2 - (P_B^{cms})^2}$
 $5.20 < M_{bc} < 5.29 (\text{GeV} / c^2)$
Energy Difference
 $\Delta E \equiv E_B^{cms} - E_{Beam}^{cms}$
 $|\Delta E| < 0.5 (\text{GeV})$

$E_{Beam}^{cms} = 5.29 (\text{GeV})$
: Beam Energy
 E_B^{cms} : Energy of B
 P_B^{cms} : Momentum of B
All of them are CMS



Vertex Reconstruction



Vertexing process

Calculate K_s Momentum

↓

Vertex Fit used K_s with B^0 Vertex region constrained

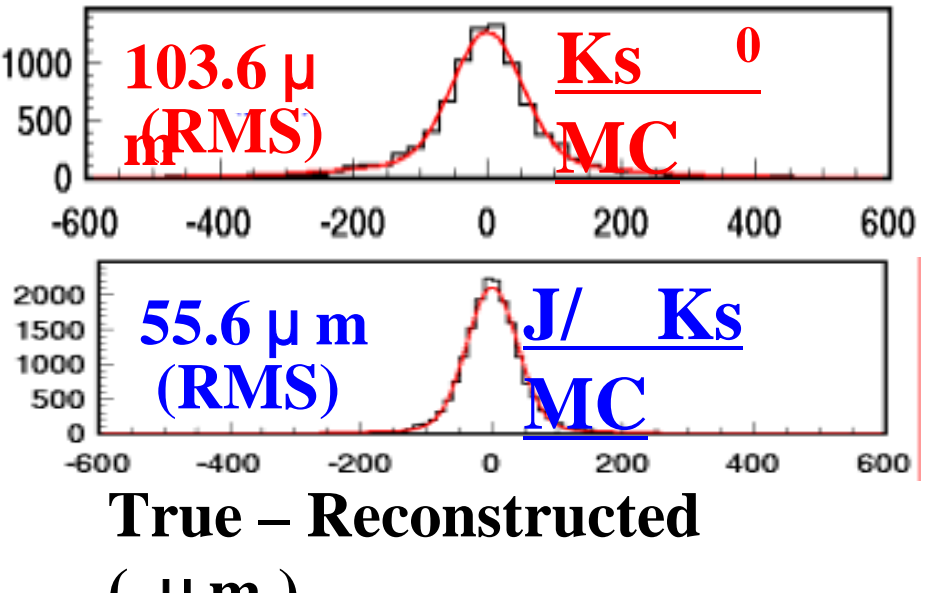
Vertexing efficiency

$B^0 \rightarrow K_s \pi^0$:

= 25.9%

$B^0 \rightarrow J/\psi K_s$ (Not official value)

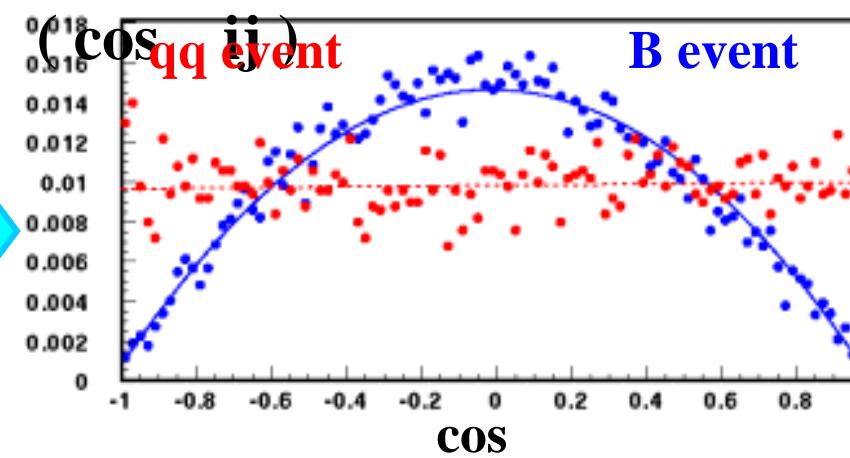
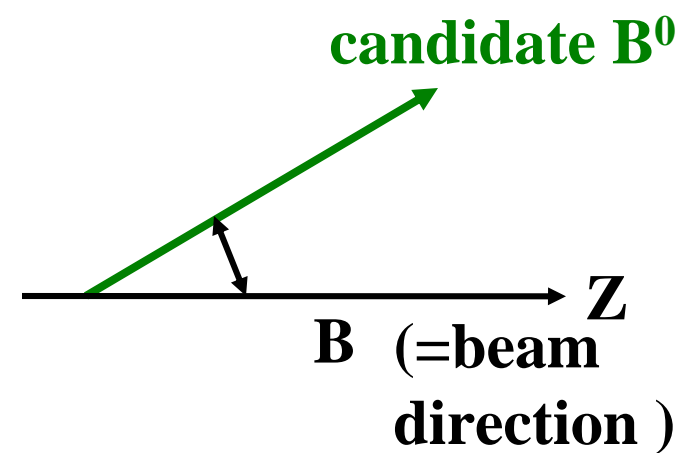
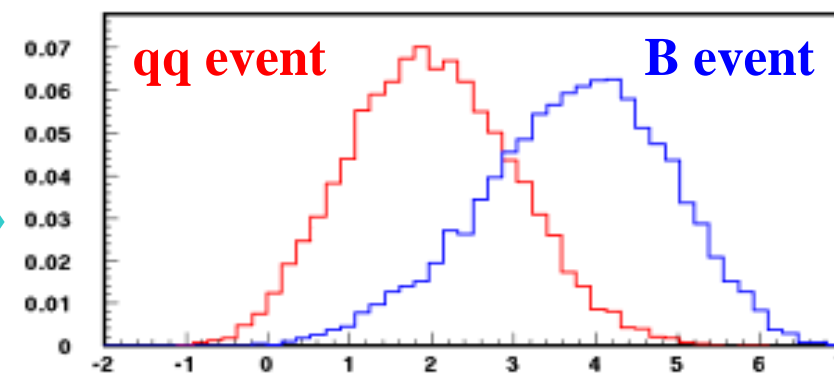
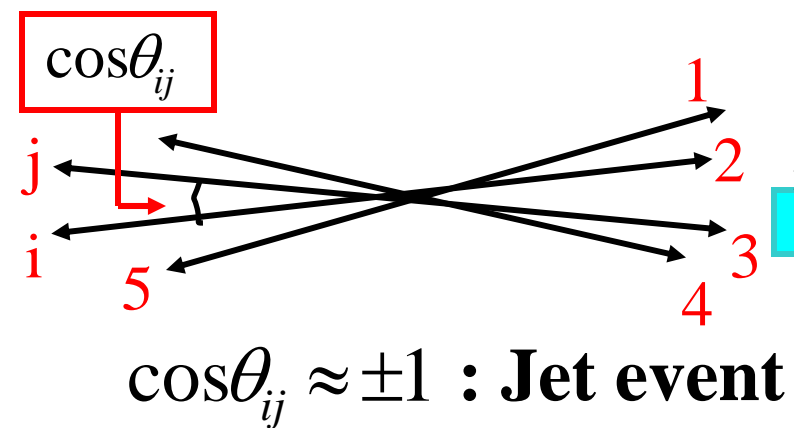
= 95.8%



Background Rejection

Main Background is Jet events ($e^+e^- \rightarrow q\bar{q}$)

→ Rejected used difference of Topology of events



**Background
Rejection**

Likelihood Ratio Cut

Likelihood

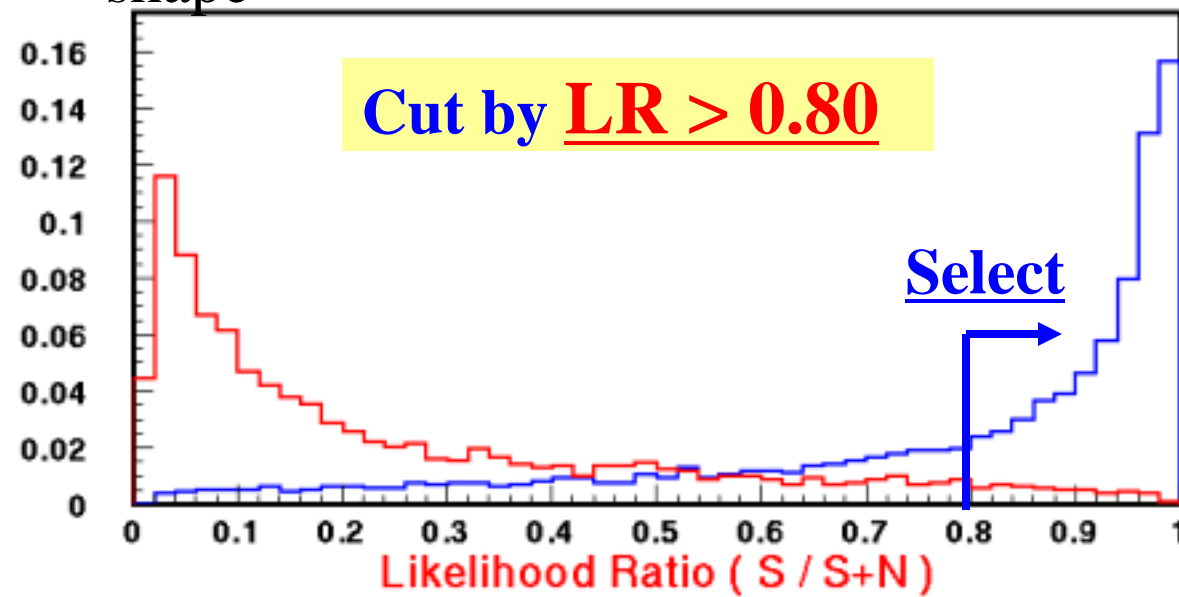
$$L_{BB,qq} = L(SFW) \times L(\cos \theta_B)$$

L(SFW)=SFW shape

L(cos θ_B)= $\cos \theta_B$
shape

Likelihood Ratio

$$LR = \frac{L_{BB}}{L_{BB} + L_{qq}}$$



LR>0.8 was defined
as

$$\frac{N_{sig}}{\sqrt{N_{sig} + N_{qq}}}$$

became Maximum

$N_{sig,qq}$...#of signal,qq

Signal Yield Extraction



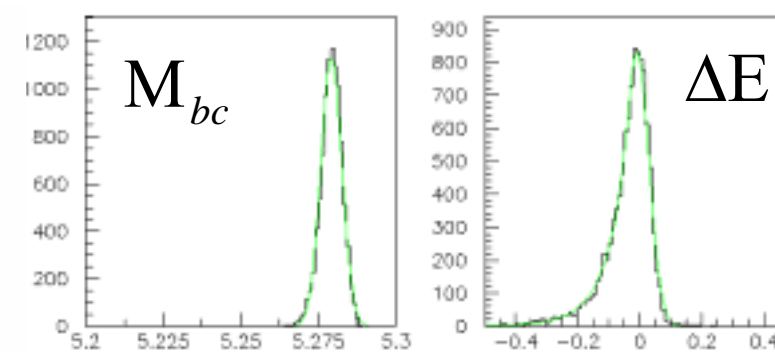
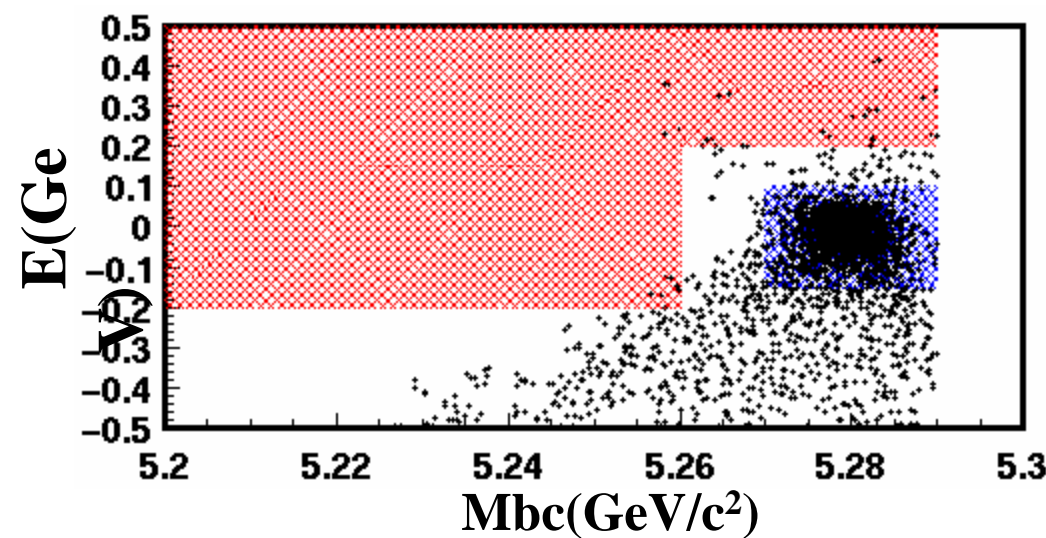
Tukuba hall in KEK

Signal Yield is calculated by

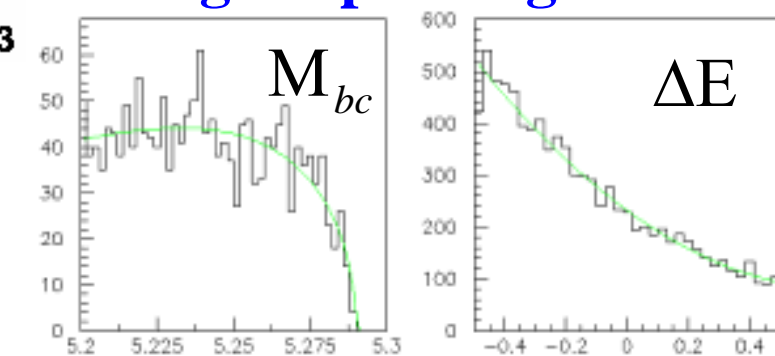
Unbinned Maximum Likelihood Fit to M_{bc} & E

$$Likelihood = \prod_{i=1}^N L_i(M_{bc}, \Delta E)$$

$$L_i(M_{bc}, \Delta E) = f_{sig} \cdot P_{sig}(M_{bc}, \Delta E) + (1 - f_{dig}) \cdot P_{bkg}(M_{bc}, \Delta E)$$



P_{sig} shape = Signal MC



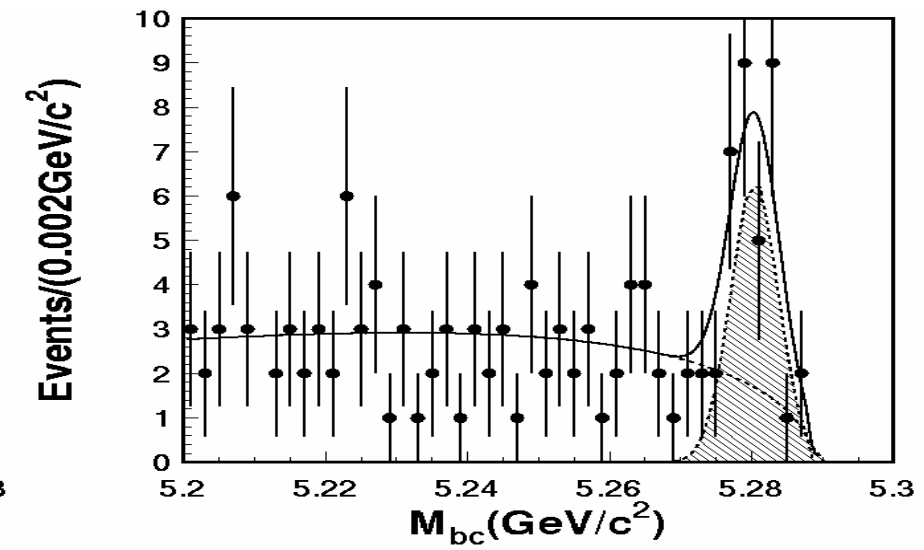
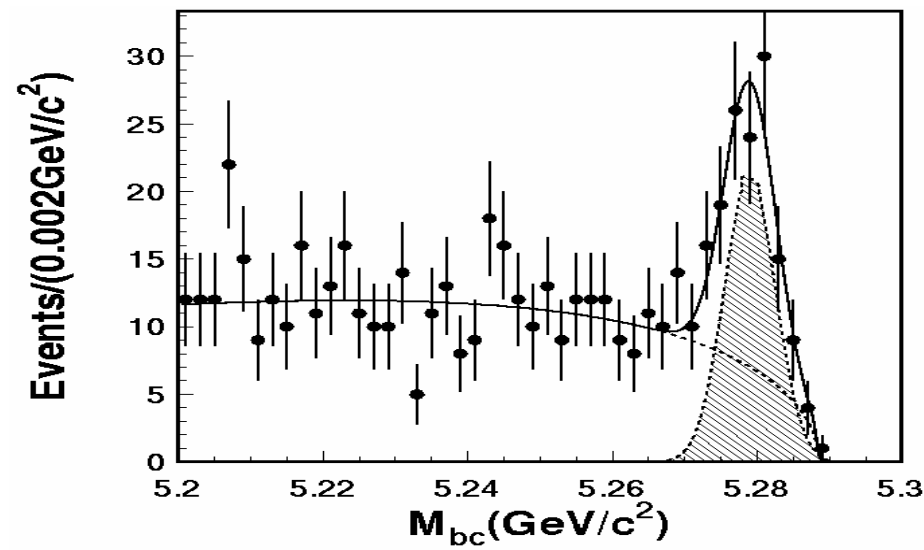
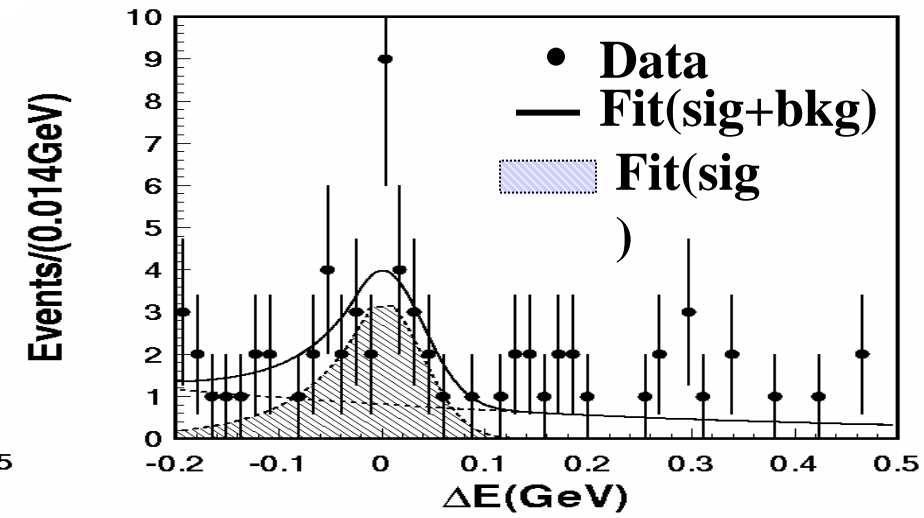
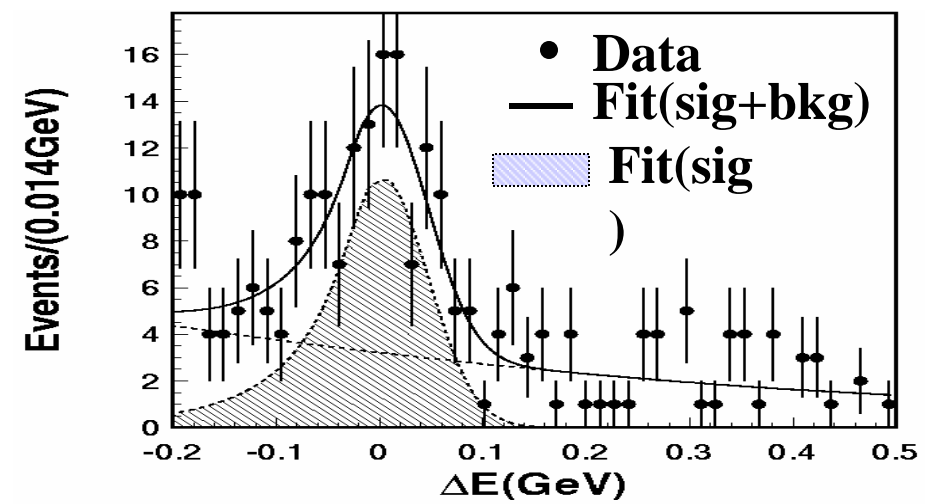
P_{bkg} shape = Sideband data

Signal Region

$5.27 < M_{bc} < 5.29 \text{ (GeV/c}^2\text{)}$

$-0.15 < E < 0.10 \text{ (GeV)}$

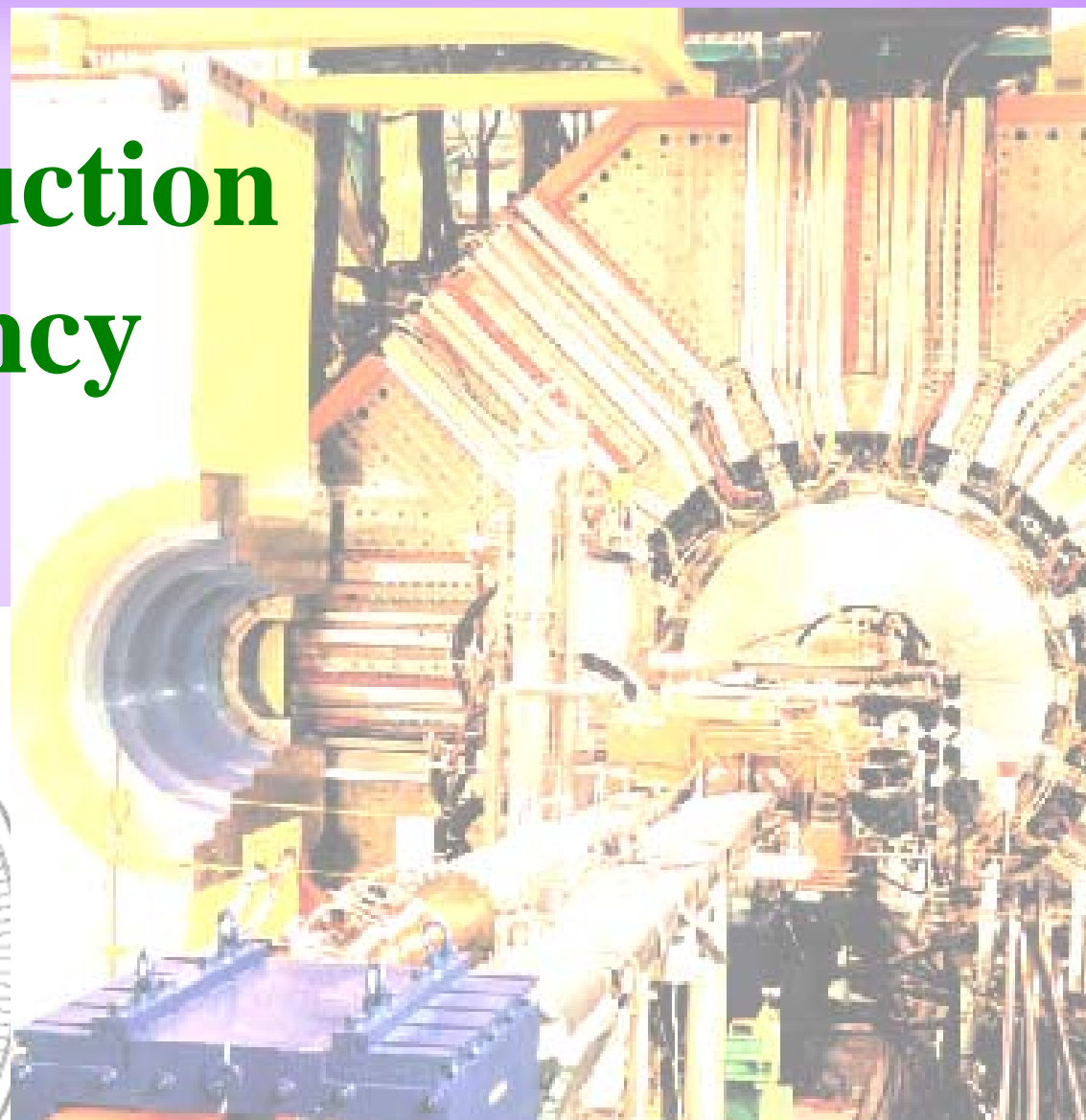
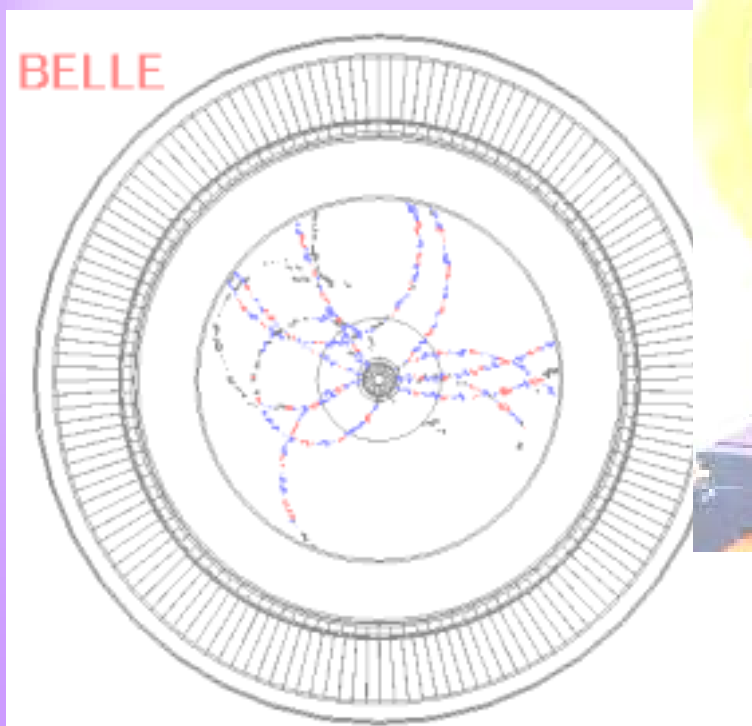
Fitting Result without(L) & with(R) Vertexing



LR>0.80
Signal Yield = 92.8 ± 11.3

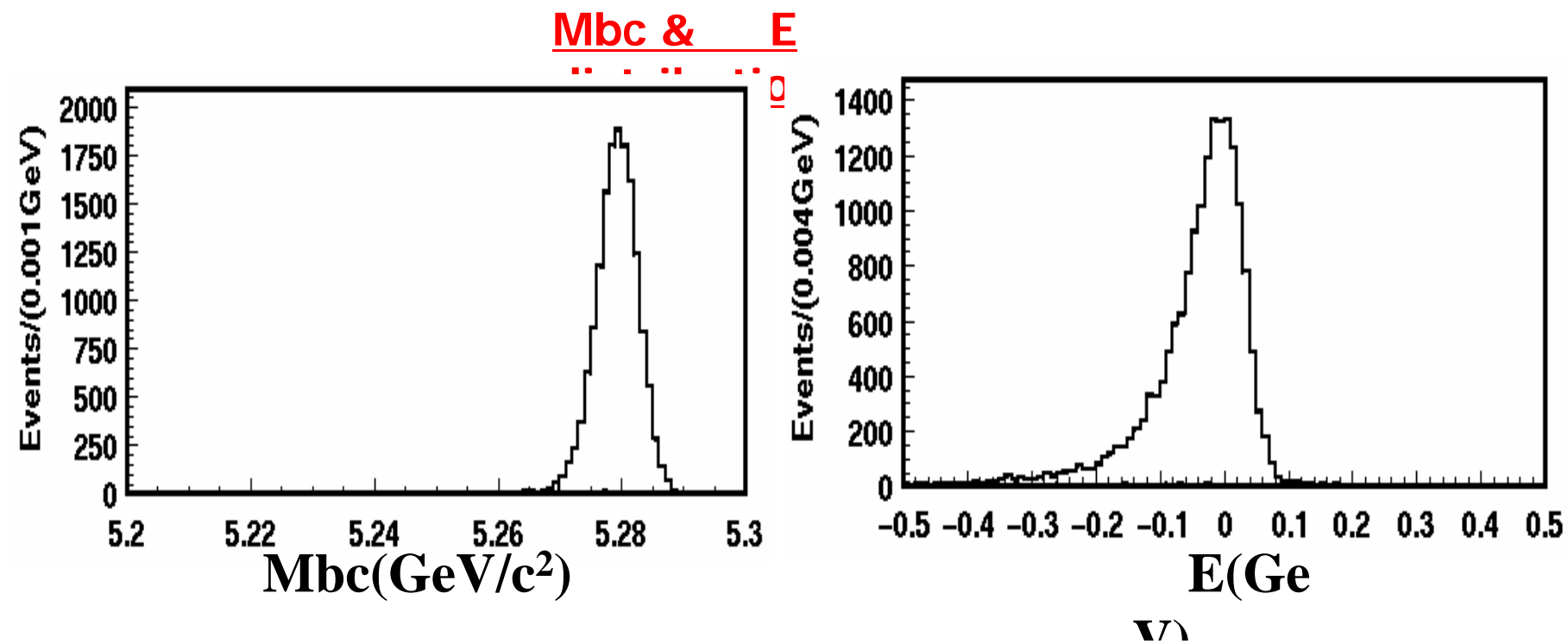
LR>0.80
Signal Yield = 26.2 ± 5.6

Reconstruction Efficiency



Reconstruction Efficiency was Calculated by Monte Carlo

	<u>W/o Vertex Cut</u>	<u>W/ Vertex Cut</u>
Not LR Cut	<u>30.6 %</u>	<u>7.6</u>
LR > 0.80 Cut	<u>18.8</u> %	<u>4.7</u> %



Summary

Used data sample 140fb^{-1}

w/o Vertexing	Signal Yield	Reconstruction Efficiency
LR > 0.8 Cut	92.8 ± 11.3	18.8 (%)

w/ Vertexing	Signal Yield	Reconstruction Efficiency
LR > 0.8 Cut	26.2 ± 5.6	4.7(%)

Vertex Efficiency	25.9 (%)
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We could estimate the K_s^0 events without vertexing (93), but vertex efficiency is very small(25%). The #events for CP-fit is 26.

Future Plan

Background Study by MC

→ Estimate peaking background

Measurement CP-Asymmetry

→ Define the **special ' t' Resolution**,
because this resolution is different
from J/ mode(Golden mode)

→ **This is very difficult problem**



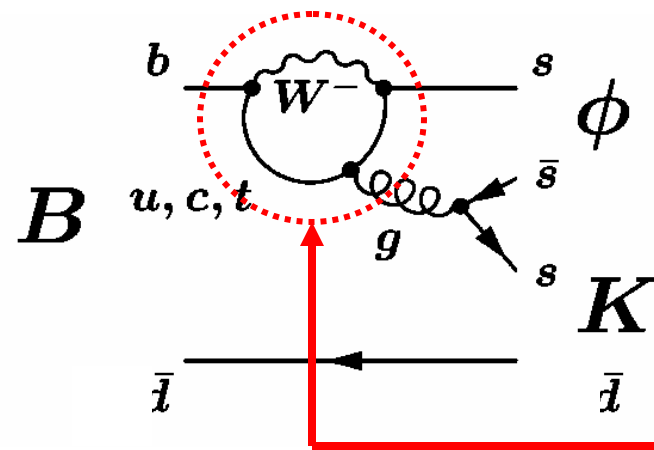
Finish until JPS(2004 Spring) ???

Appendix

Physics Motivation

LP03 Conference

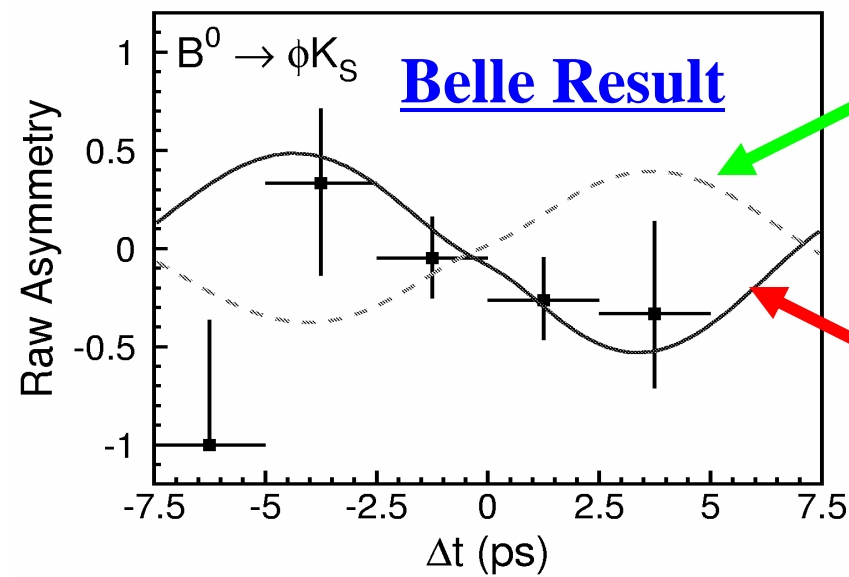
$B_d^0 \rightarrow \phi + K_S$ Measurement ϕ_1 by B^0 Mixing



Theoretical uncertainty is
Small in Standard Model



Clean Mode for New Physics



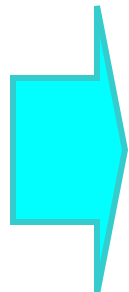
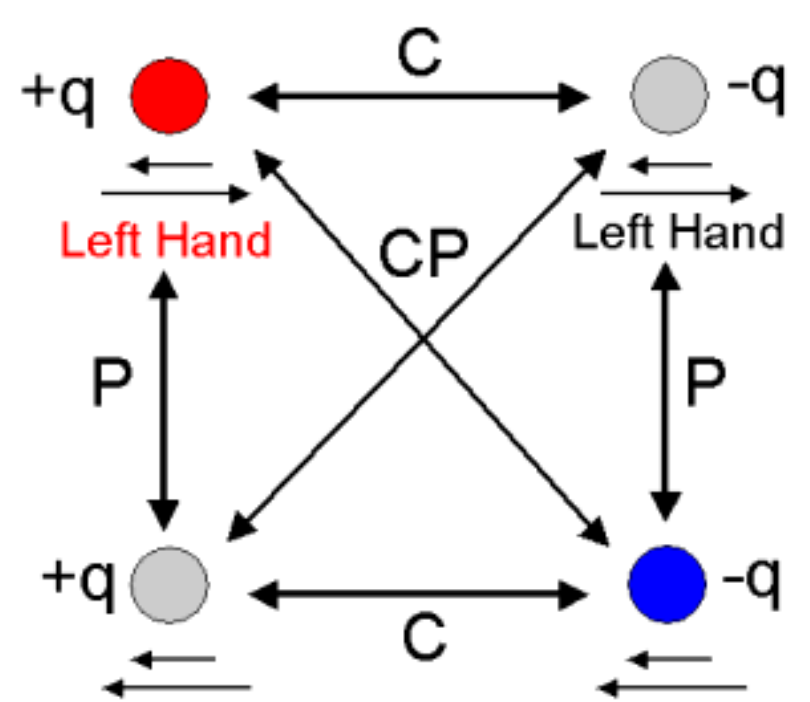
$\sin 2\phi_1$ (Belle 2003, 140 fb⁻¹)
 $= 0.733 \pm 0.057 \pm 0.028$

$\sin 2\phi_{1\text{eff}} = -0.96 \pm 0.50^{+0.09}_{-0.11}$

Introduction to CP-Violation(1)

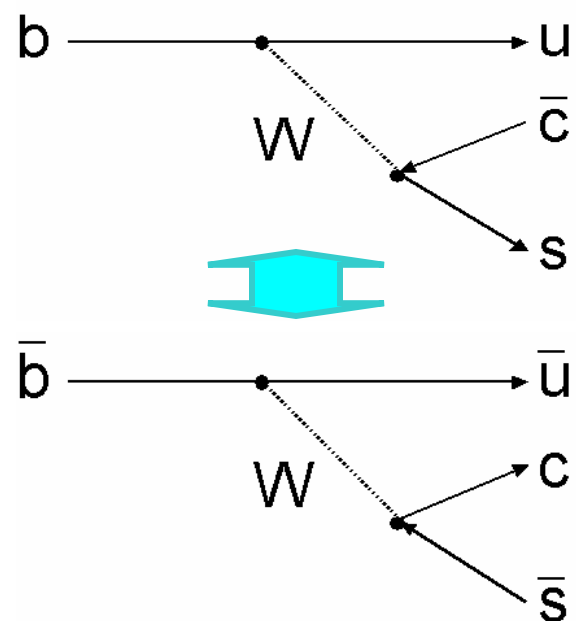
Dynamics of Physics = Lagrangian

$$\mathbf{L}_{\text{physics}} = \mathbf{L} + \mathbf{L}_{\text{h.c}}$$



In Weak Interaction
Particle \leftrightarrow Anti-Particle
||
CP transformation

Introduction to CP-Violation(2)



$$L = -\frac{g_w}{\sqrt{2}} U_{ub}^* \bar{\psi}_u \gamma^\mu (1 - \gamma^5) \psi_b W_\mu^-$$

Hermite $L_{H.C} = -\frac{g_w}{\sqrt{2}} U_{ub} \bar{\psi}_b \gamma^\mu (1 - \gamma^5) \psi_u W_\mu^+$

CP $L_{CP} = -\frac{g_w}{\sqrt{2}} U_{ub}^* \bar{\psi}_b \gamma^\mu (1 - \gamma^5) \psi_u W_\mu^+$

CP Conservation & CP Violation

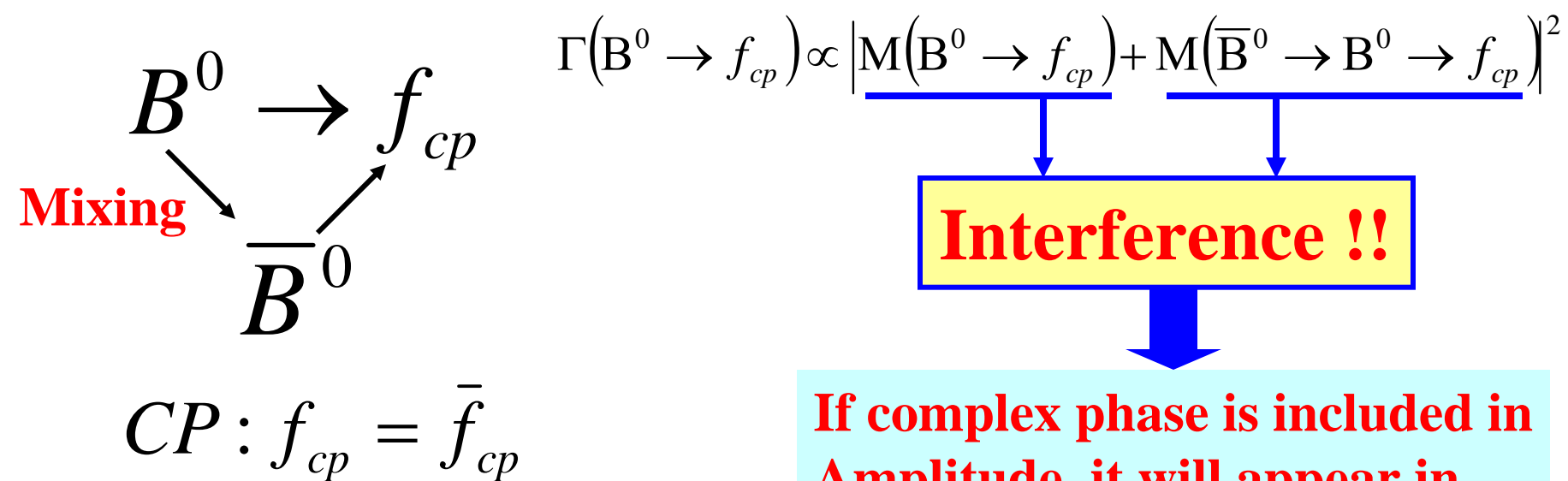
- (i) $U_{ub}^* = U_{ub} \rightarrow L_{H.C} = L_{cp} = L$
 \rightarrow **Particle = Antiparticle** \rightarrow CP Conservation
- (ii) $U_{ub}^* \neq U_{ub} \rightarrow L_{H.C} \neq L_{cp} \neq L$
 \rightarrow **Particle \neq Antiparticle** \rightarrow CP Violation

Introduction to CP-Violation(3)

Requirement for CP-Violation Observation

- 1) More than Two Decay Process
- 2) Current has complex phase (CKM matrix)

B⁰ decay to CP eigenstate



Introduction to CP-Violation(4)

Time Dependent CP Violation in B-B Mixing

Time dependent
B Wave function

$$|B^0(t)\rangle = e^{-i(M+\Gamma/2)t} \left\{ \cos\left(\frac{\Delta mt}{2}\right) |B^0\rangle + i \frac{q}{p} \sin\left(\frac{\Delta mt}{2}\right) |\bar{B}^0\rangle \right\}$$

$$|\bar{B}^0(t)\rangle = e^{-i(M+\Gamma/2)t} \left\{ \cos\left(\frac{\Delta mt}{2}\right) |\bar{B}^0\rangle + i \frac{p}{q} \sin\left(\frac{\Delta mt}{2}\right) |B^0\rangle \right\}$$

Time Dependence & CP-Asymmetry

$$\Gamma(B^0 \rightarrow f_{cp}) \propto e^{-\Gamma t} \left[1 + |\lambda|^2 \mp (|\lambda|^2 - 1) \cos(\Delta mt) + 2 \operatorname{Im}(\lambda) \sin(\Delta mt) \right]$$

$$A_{cp} = \frac{\Gamma(B^0 \rightarrow f_{cp}) - \Gamma(\bar{B}^0 \rightarrow f_{cp})}{\Gamma(B^0 \rightarrow f_{cp}) + \Gamma(\bar{B}^0 \rightarrow f_{cp})} = -\frac{|\lambda|^2 - 1}{|\lambda|^2 + 1} \cdot \cos(\Delta mt) - \frac{2 \operatorname{Im}(\lambda)}{|\lambda|^2 + 1} \sin(\Delta mt)$$

$$\lambda = \frac{q}{p} \cdot \frac{\bar{A}(\bar{B}^0 \rightarrow f_{cp})}{A(B^0 \rightarrow f_{cp})} \quad \langle f_{cp} | T | B^0 \rangle \equiv A$$

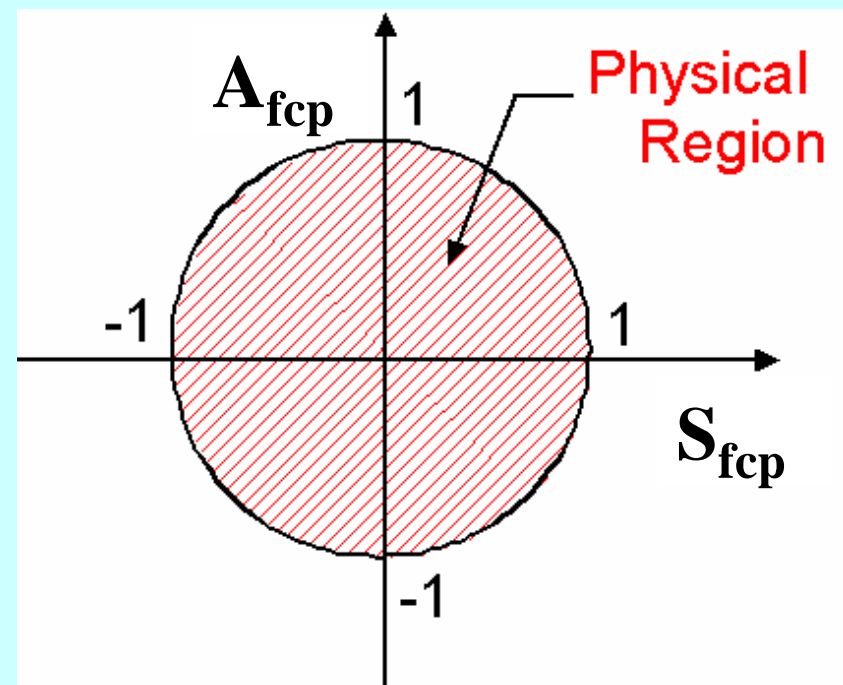
Introduction to CP- Violation(5)

Physical Region

$$A_{CP} = -A_{fcp} \cos(\Delta mt) - S_{fcp} \sin(\Delta mt)$$
$$\frac{|\lambda|^2 - 1}{|\lambda|^2 + 1} = A_{fcp} \quad \frac{2 \operatorname{Im}(\lambda)}{|\lambda|^2 + 1} = S_{fcp}$$

$$A_{fcp}^2 + S_{fcp}^2 + \left(\frac{2 \operatorname{Re}(\lambda)}{|\lambda|^2 + 1} \right)^2 = 1$$

$$\Leftrightarrow A_{fcp}^2 + S_{fcp}^2 \leq 1$$



Event Selection

K_s^0 Selection Criteria

0 $E > 50\text{MeV}$ (No match with Charged track)

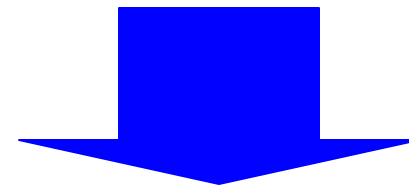
$0.118 < M < 0.150(\text{GeV}/c^2)$

K_s $| M - 497.672(\text{MeV}/c^2) | < 15\text{MeV}/c^2$

Fang-san's Cut

Other Cut

IF Both tracks have $\text{SVD_zhit} > 0 \rightarrow dz < 2.0\text{cm}$
IF One of track has $\text{SVD_zhit}(1) > 0 \rightarrow dr > 0.1\text{mm}$
IF Both track have no $\text{SVD_zhit} \rightarrow d < 2.0\text{cm}$



B^0 Reconstruction

Background Rejection by Super Fox-Wolfram

Super Fox-Wolfram (moment)

$$H_l^{so} = \sum_{i,j} |p_i| |p_j| P_l(\cos \theta_{ij})$$

$$H_l^{oo} = \sum_{j,k} |p_j| |p_k| P_l(\cos \theta_{jk})$$

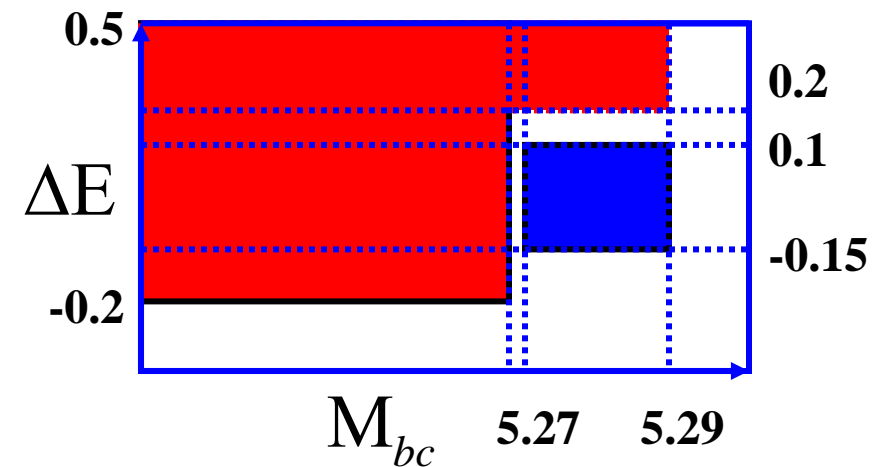
P_i : B-Candidate Particle
 $P_j P_k$: Other Particle (charge&neutral
 $P_l^{m=0}(\cos \theta_{ij})$: Legendre Function

Fisher discriminant

$$F = \sum_{l=2,4} \alpha_l \cdot \frac{H_l^{so}}{H_o^{so}} + \sum_{l=1-4} \beta_l \cdot \frac{H_l^{oo}}{H_o^{oo}}$$

, are optimized with

Signal MC & Sideband Data



Background Rejection by New Super Fox-Wolfram

**I used N-SFW in
this Analysis**

$$NSFW = \sum_{l=0,4} R_l^{so} + \sum_{l=0,4} R_l^{oo} + \gamma \sum_{n=1} |(P_t)_n|$$

$$R_l^{so} = \frac{(\alpha_c)_l \cdot (H'_{charged})_l^{so} + (\alpha_n)_l \cdot (H'_{neutral})_l^{so} + (\alpha_m)_l \cdot (H'_{missing})_l^{so}}{E_{beam} - \Delta E}$$

Missing Mass $mm^2 = \left(E_{Y(4s)} - \sum_{n=1} E_n \right)^2 - \left(\left| \sum_{n=1} P_n \right| \right)^2$

$$\begin{aligned} (H'_X)_{l=1,3}^{so} \quad (H'_{charged})_l^{so} &= \sum_i \sum_{j_X} \beta_l^{so} Q_i Q_{j_X} |p_{j_X}| P_l (\cos \theta_{ij_X}) \\ (H'_{neutral})_l^{so} &= (H'_{missing})_l^{so} = 0 \end{aligned}$$

$$(H'_X)_{l=0,2,4}^{so} \quad (H'_X)_l^{so} = \sum_i \sum_{j_X} \beta_l^{so} |p_{j_X}| P_l (\cos \theta_{ij_X})$$

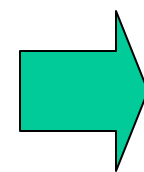
$$NSFW = \sum_{l=0,4} R_l^{so} + \sum_{l=0,4} R_l^{oo} + \gamma \sum_{n=1} |(P_t)_n| \quad \mathbf{N-SFW(2)}$$

$$R_{l=1,3}^{oo} = \frac{\sum_j \sum_k \beta_l^{oo} Q_j Q_k |p_j| |p_k| P_l(\cos \theta_{jk})}{(E_{beam} - \Delta E)^2}$$

$$R_{l=0,2,4}^{oo} = \frac{\sum_j \sum_k \beta_l^{oo} |p_j| |p_k| P_l(\cos \theta_{jk})}{(E_{beam} - \Delta E)^2}$$

$\sum_{n=1} |(P_t)_n|$: **Scalar sum of the transverse momentum**

**Divide mm² region into
7 region for correlation
between SFW and mm²**

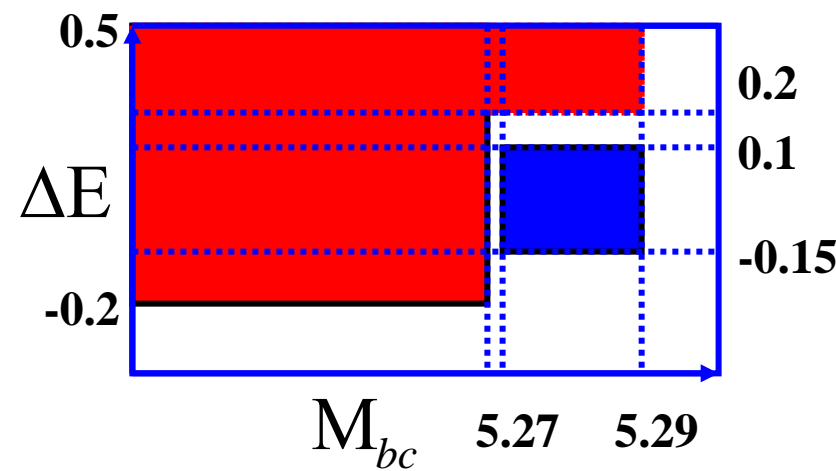


**Total Parameter
= (11+5+1) × 7**

Optimized N-SFW

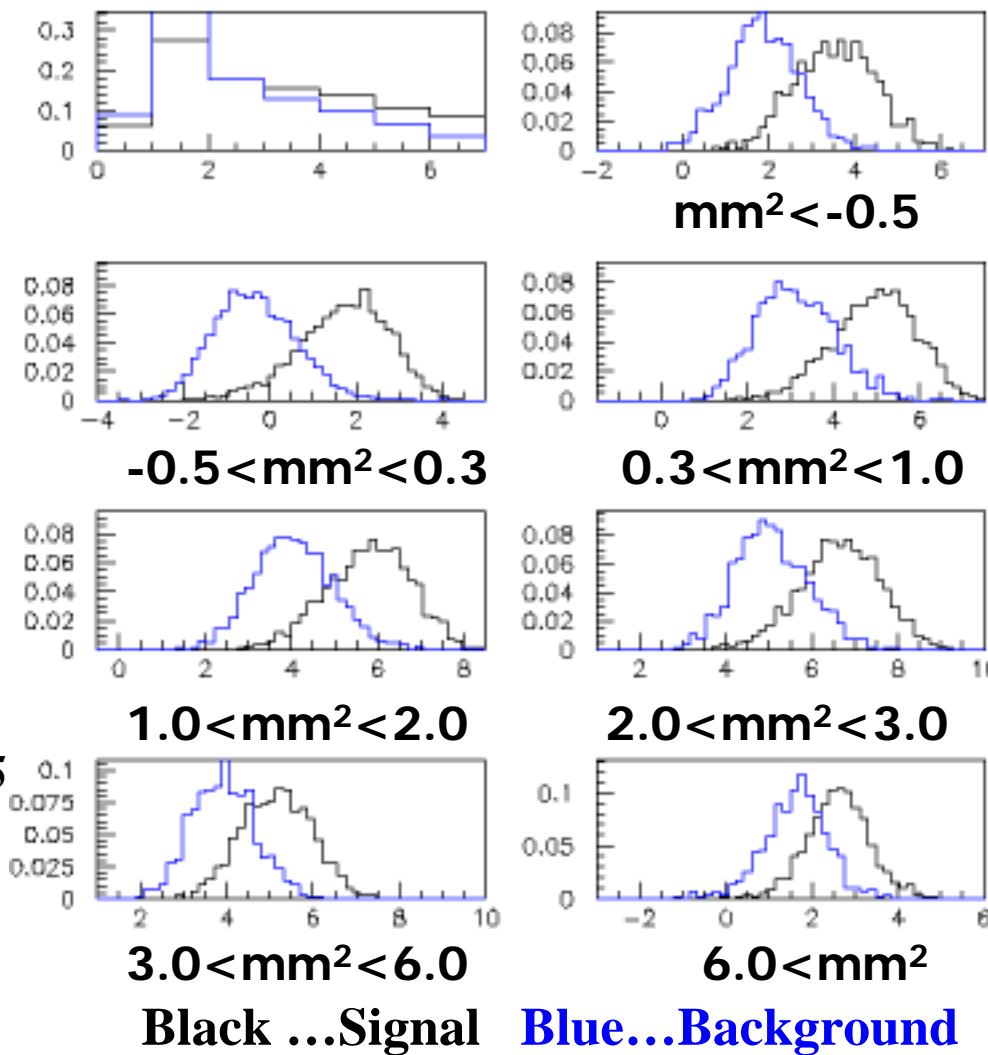
7 Missing Mass
Regions 

Parameters are optimized
with Signal MC &
Sideband Data



N-SFW(3)

K-SFW (7 Missing Mass
region) Unit = GeV/c²



**Background
Rejection**

Likelihood Ratio Cut

Likelihood

$$L_{BB,qq} = L(SFW) \times L(\cos \theta_B)$$

Likelihood Ratio

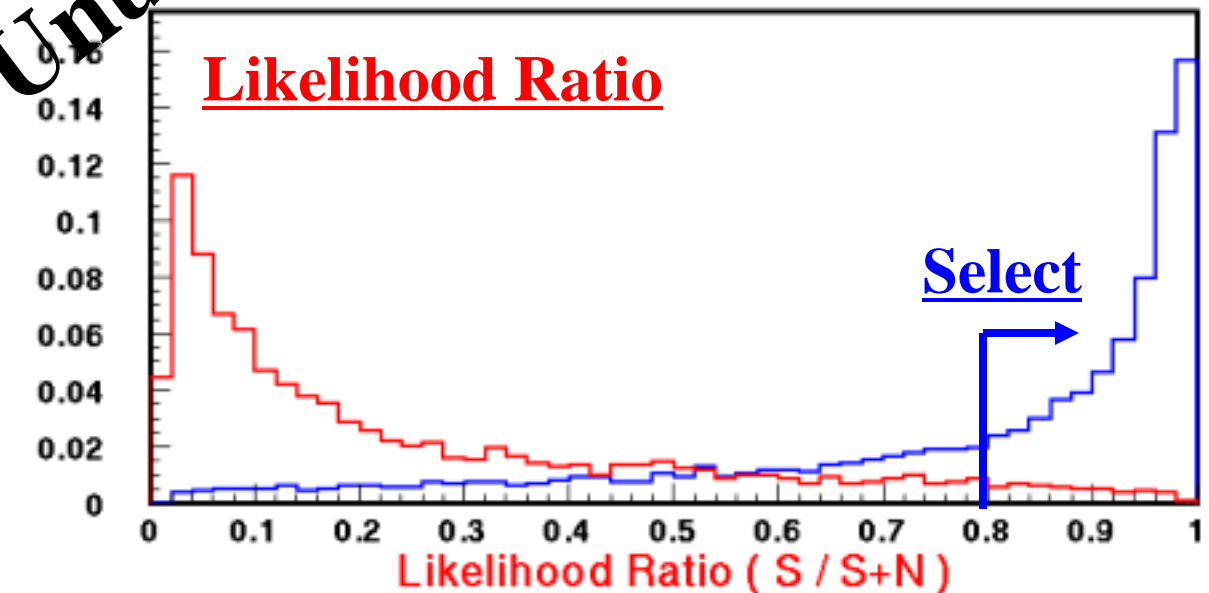
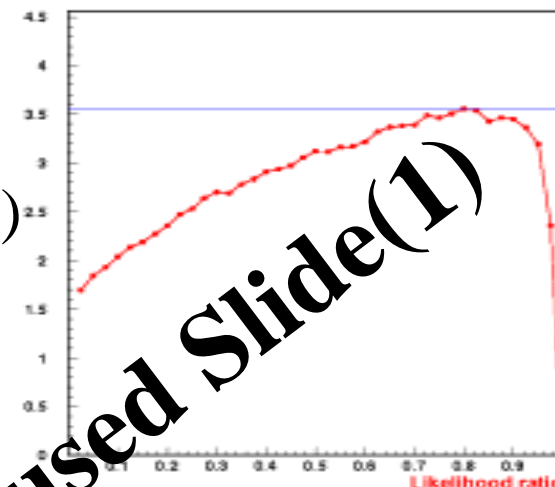
$$LR = \frac{L_{BB}}{L_{BB} + L_{qq}}$$

**Cut by
LR > 0.80**

Threshold was defined by **Figure of Merits**

$$F.o.M = \frac{N_{sig}}{\sqrt{N_{sig} + N_{qq}}}$$

LR at Max of F.o.M

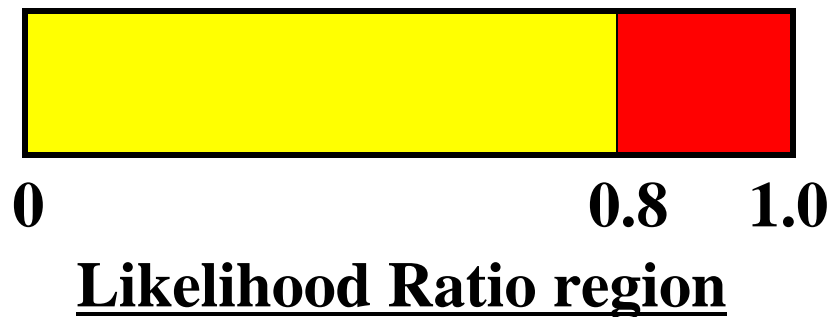


Background
Rejection

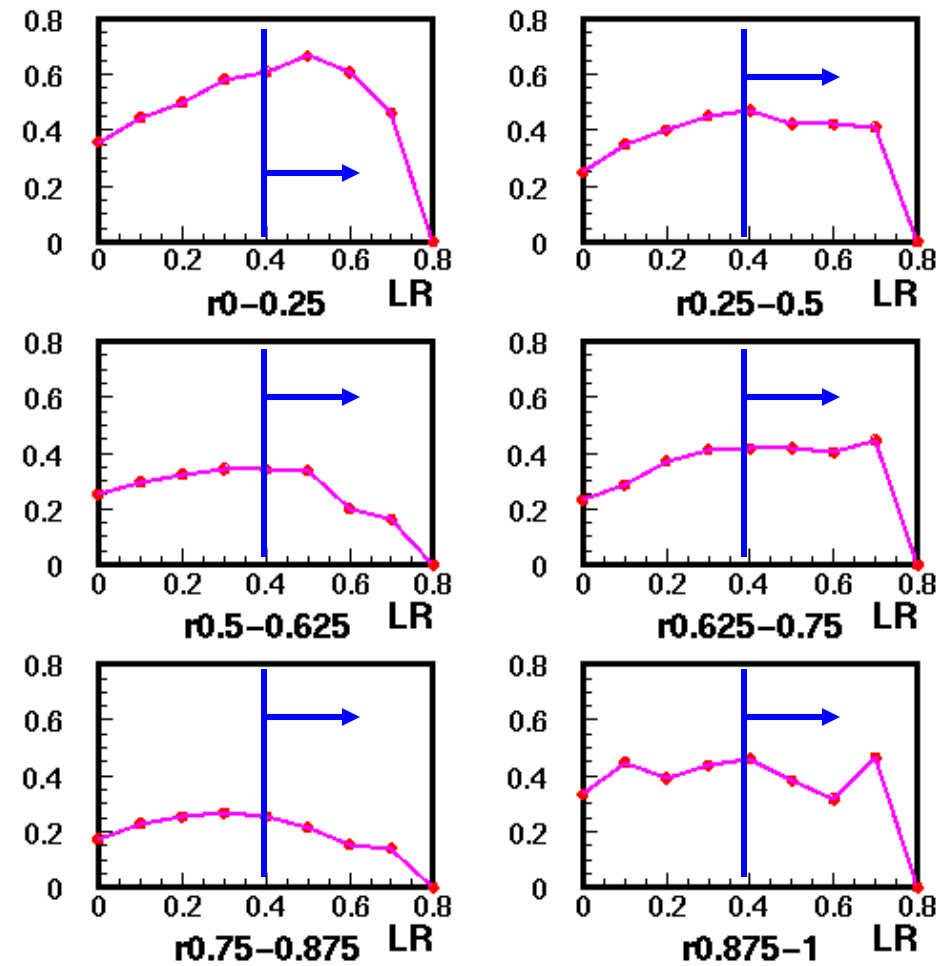
Second Likelihood Ratio Cut

We want to use more events
Even if $LR < 0.80$

Likelihood Ratio Cut in
 $0 < LR < 0.80$



6 r-regions (r = Wrong tag fraction)



Loose Cut : $0.4 < LR \leq 0.8$

Fitting Function(Signal Shape)

Signal Shape is obtained from Signal MC

Signal Mbc : Single Gaussian

$$P(M_{bc}) = N_{norm} \cdot \frac{1}{\sqrt{2\pi}\sigma_{Mbc}} \exp\left(-\frac{(\langle\mu_{Mbc}\rangle - M_{bc})^2}{2\sigma_{Mbc}^2}\right)$$

μ_{Mbc}	5.2792(GeV/c²)
Mbc	34.1(MeV/c²)

Signal E : Single Gaussian

$$P(\Delta E) = \begin{cases} \Delta E - \mu_{\Delta E} \leq -a\sigma_{\Delta E} : N_{norm} \cdot \exp\left(-\frac{1}{2a}\right) \cdot \left[1 - \frac{a}{n} \left(\frac{\Delta E - \mu_{\Delta E}}{\sigma_{\Delta E}} - a\right)\right] \\ \Delta E - \mu_{\Delta E} > -a\sigma_{\Delta E} : N_{norm} \cdot \exp\left(-\frac{\Delta E - \mu_{\Delta E}}{2\sigma_{\Delta E}^2}\right) \end{cases}$$

μ_E	-9.3(MeV/c²)	a	0.6518
σ_E	39.0(MeV/c²)	n	11.934

Fitting Function(Background Shape)

Background Shape is obtained from Sideband data

Background Mbc : ARGUS function

$$P(M_{bc}) = M_{bc} \cdot \exp\left(\alpha - \alpha \left(\frac{M_{bc}}{E_{beam}}\right)^2\right) \cdot \sqrt{1 - \left(\frac{M_{bc}}{E_{beam}}\right)^2}$$

-22.63

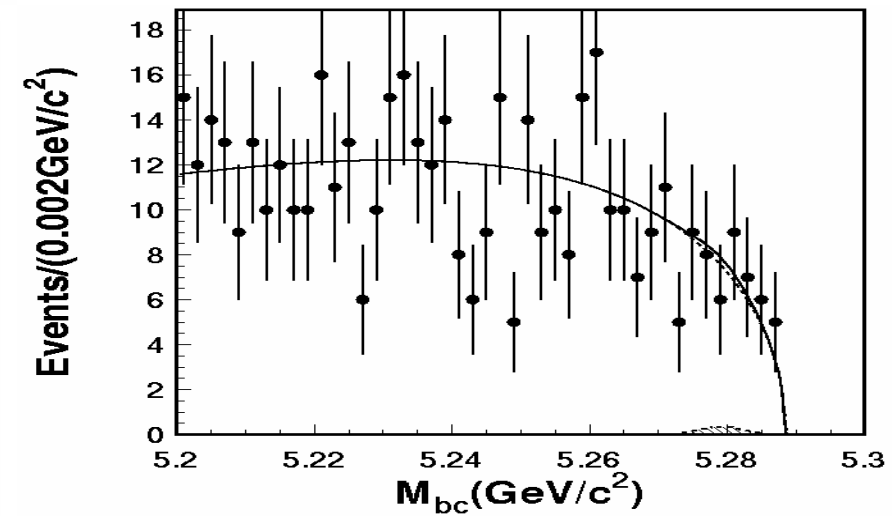
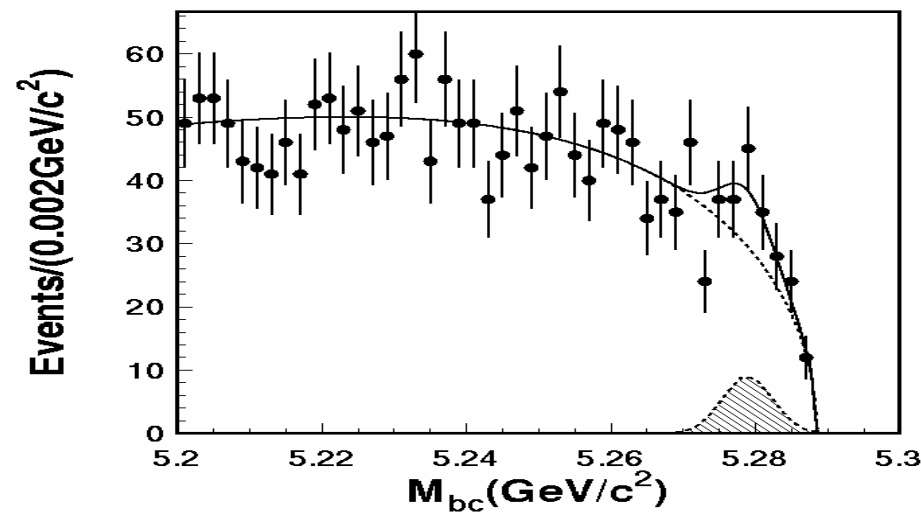
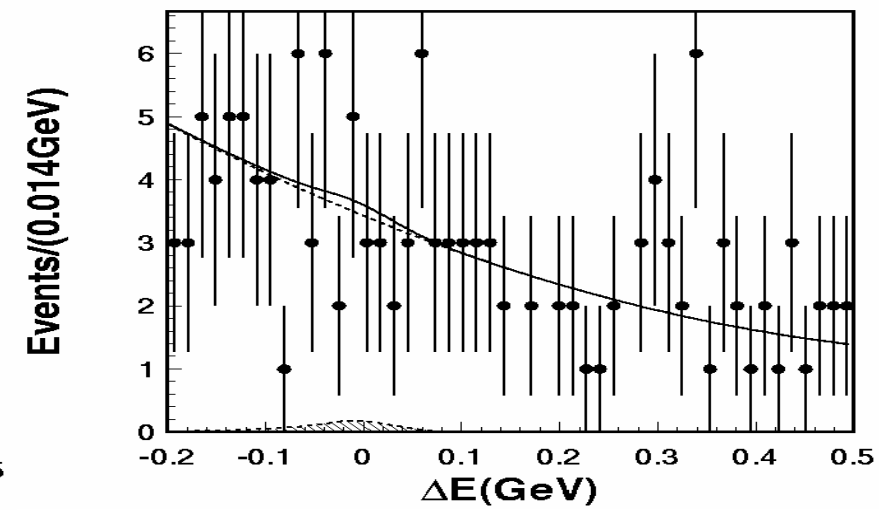
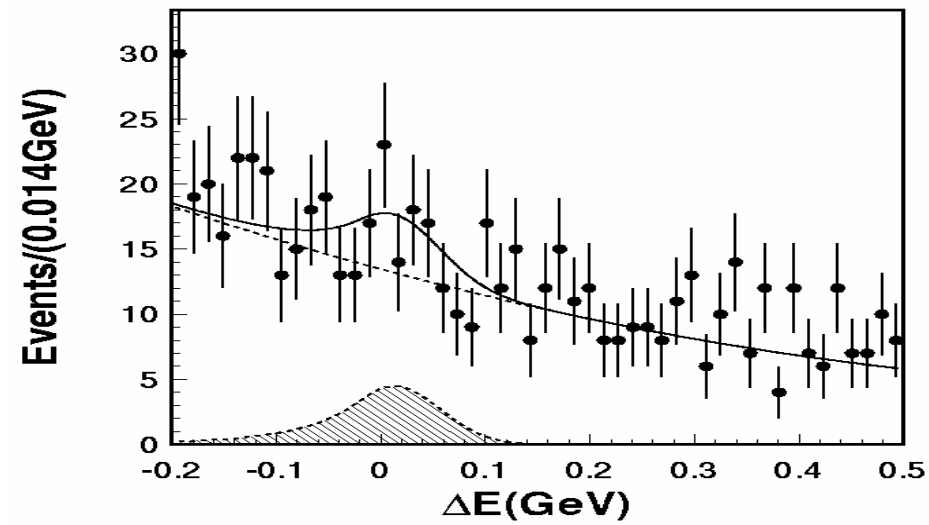
Background E : Chebyshev Function

$$P(\Delta E) = N_{norm} \cdot \left(1 + a_1 \cdot C + a_2 \cdot (2 \cdot C^2 - 1)\right)$$

$$C = \frac{2.0 \cdot \Delta E - \Delta E_{min} - \Delta E_{max}}{\Delta E_{max} - \Delta E_{min}}$$

E _{max}	0.5 (GeV/c²)
E _{min}	-0.2 (GeV/c²)
a ₁	-0.7961
a ₂	0.1421

Fitting Result before(L) & after(R) Vertexing



$0.4 < LR \leq 0.80$
Signal Yield = 38.9 ± 13.0

$0.4 < LR \leq 0.80$
Signal Yield
= 1.4 ± 5.5

Reconstruction Efficiency by MC

Used Signal MC(200,000events)

Genhep
Infomation

Ks efficiency	125510	62.77(%)
B^0 efficiency	97749	48.89(%)
B0 efficiency	74719	37.37(%)

Reconstruction efficiency (Before & after Vertexing)

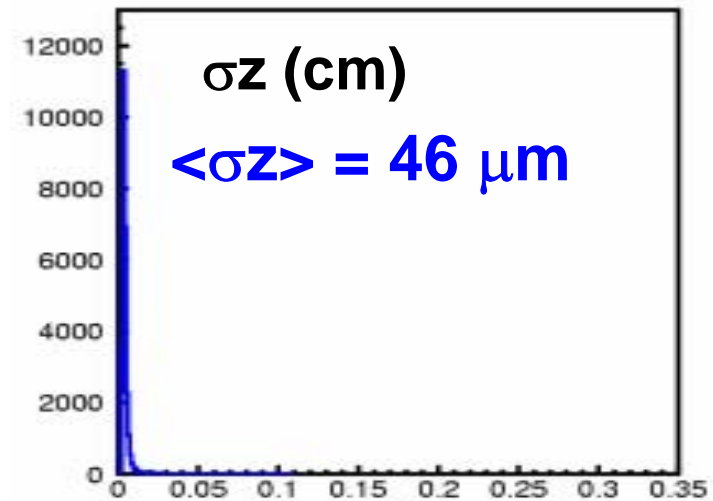
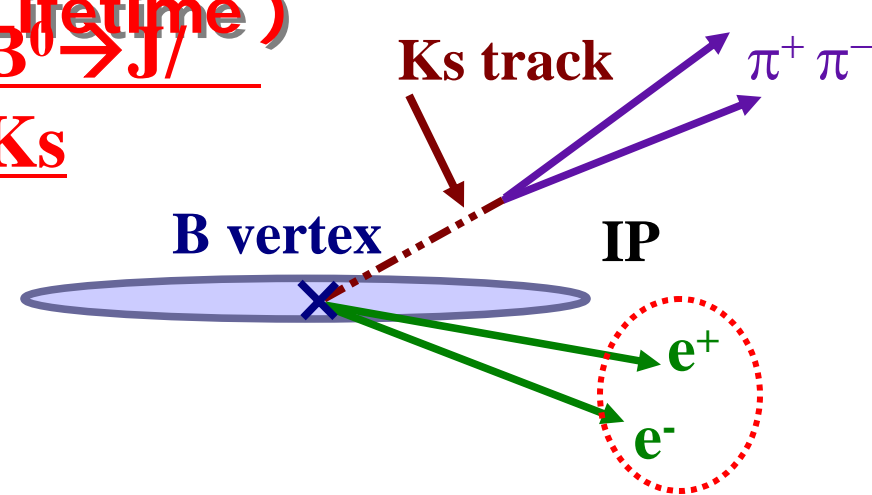
	Before Vertexing	After Vertexing
Reconstructed B^0 all Mbc& E region	71184 True : 70276 = 35.14(%)	
Reconstructed B^0 before LR cut	61795 True : 61187 = 30.60(%)	15346 True : 15226 = 7.61(%)
Reconstructed B^0 after LR cut	37922 True : 37611 = 18.81(%)	9528 True : 9470 = 4.74(%)

B⁰-Vertexing by Ks

B⁰-J/ψ Vertexing process (J/ψ → e⁺e⁻ - Short

Lifetime)
B⁰ → J/ψ

Ks

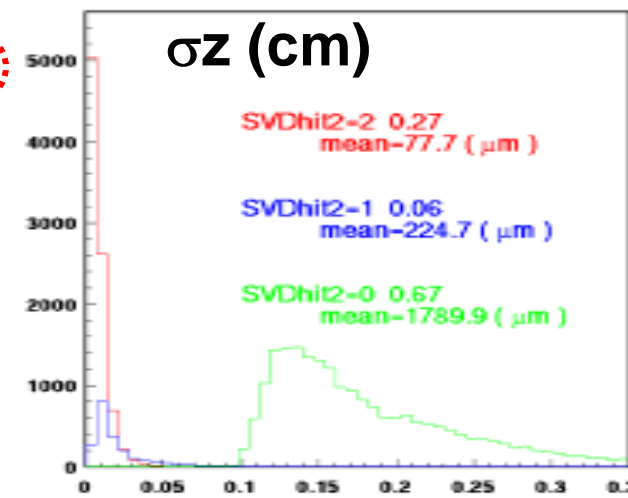
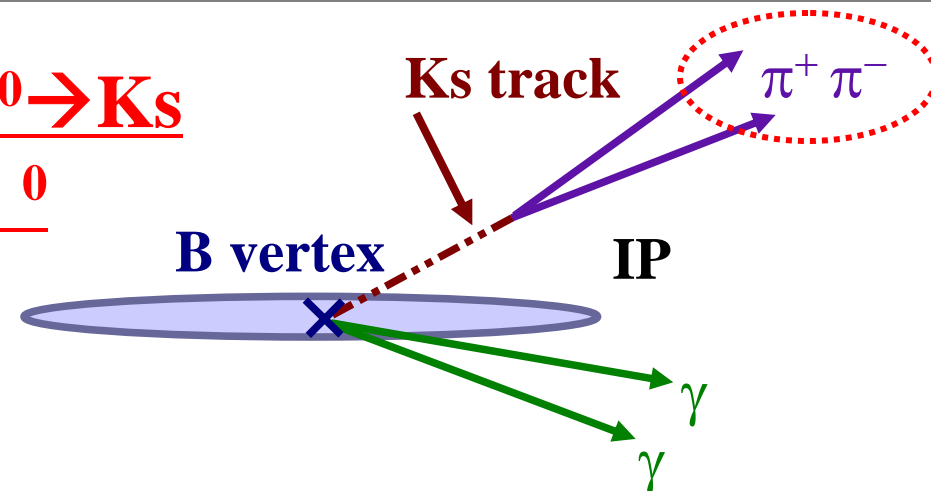


0.35(cm)

B⁰-Ks Vertexing process (Ks → + - Long Lifetime)

B⁰ → Ks

0



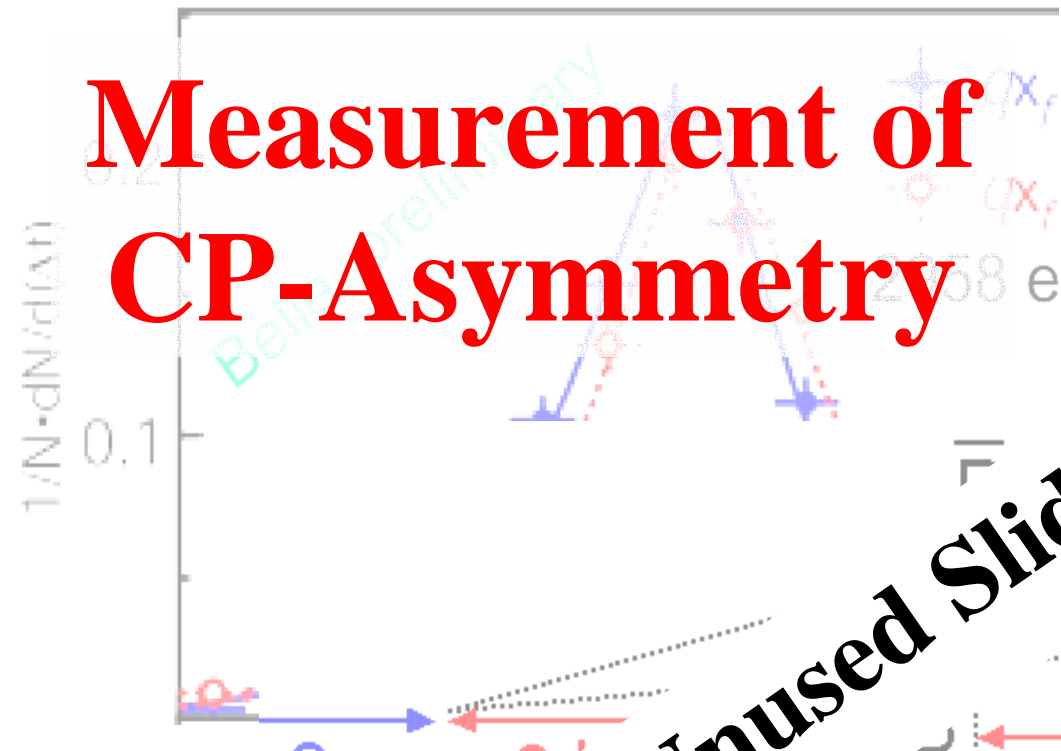
0.35(cm)

Measurement of CP-Asymmetry

未知の粒子が存在か？ 標準理論で説明できない現象発見の可能性

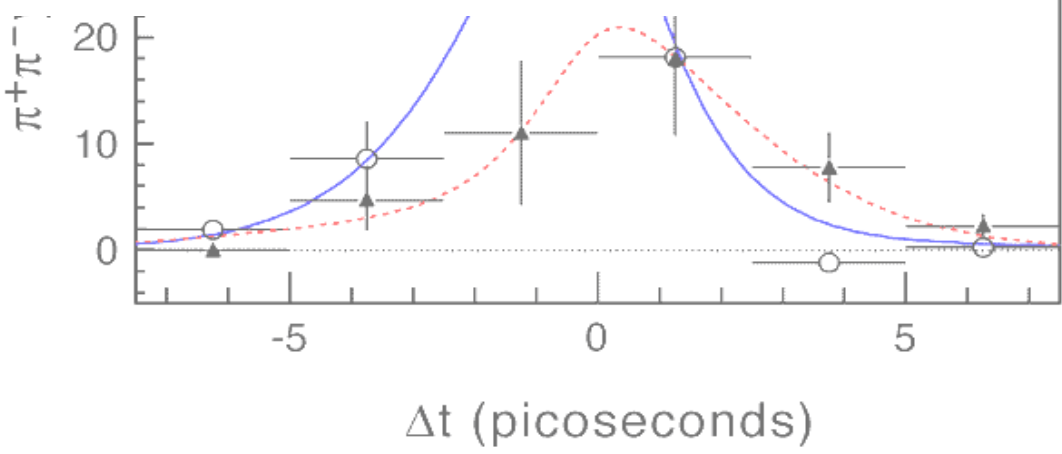
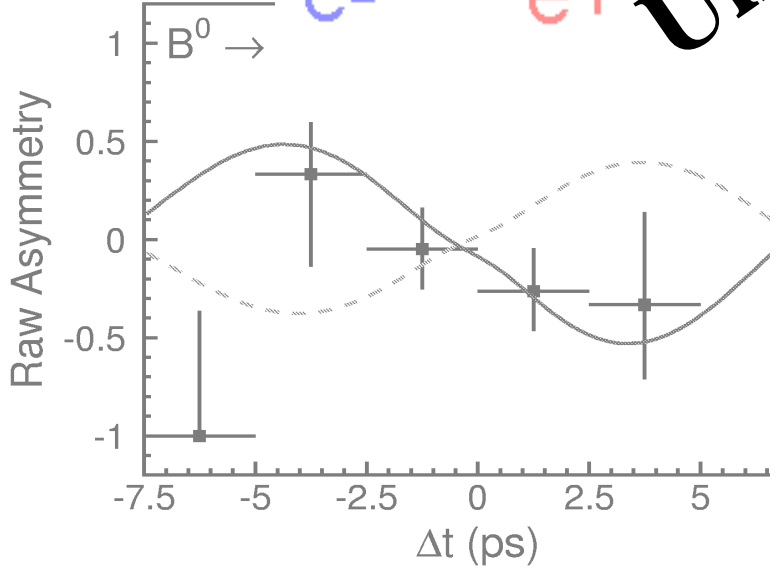
yoosee による 2003年08月14日 17時09分 の投稿, 物理学の明日へ 部門より.

endor の夕しこみに加筆して曰く
 "asahi.comの記事によると、物理学の世界で30年間定説となっている「標準理論」を覆すかもしれない発表が、米シカゴで聞かれている Lepton & P にてあったようです。



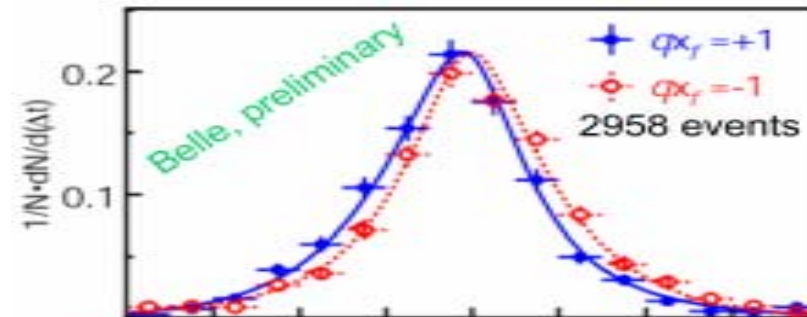
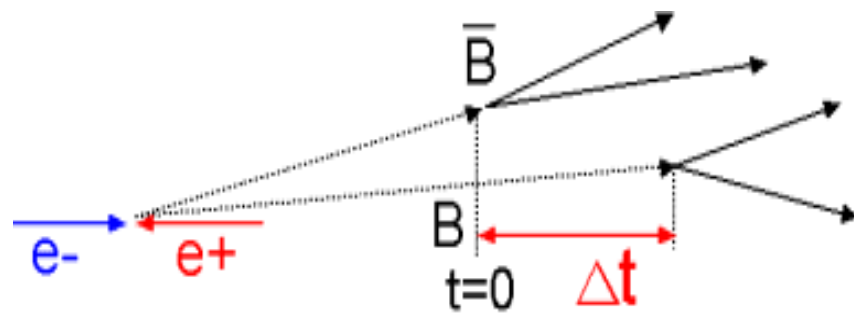
Unused Slide(2)

GeV加速器研究の
 ルミノシティを
 LE検出器では、
 となる「標準理
 れは「宇宙誕生
 はすなのに、な
 るのだろう」と言
 と呼ばれる現象
 結果も出てきて



CP-Fit

Fitting ' t' distribution & Asymmetry which free parameter are A_{fcp} & S_{fcp}



J/ψ mode presented at ICHEP2002

$$P_{q(=\pm 1)}(\Delta t) = \frac{1}{4\tau_{B^0}} e^{-\frac{|\Delta t|}{\tau_{B^0}}} \left\{ 1 + q \cdot \left(A_{fcp} \cos(\Delta m \Delta t) + S_{fcp} \sin(\Delta m \Delta t) \right) \right\}$$

⇒ $A_{cp}(\Delta t) = \frac{P_{q=-1}(\Delta t) - P_{q=1}(\Delta t)}{P_{q=-1}(\Delta t) + P_{q=1}(\Delta t)}$

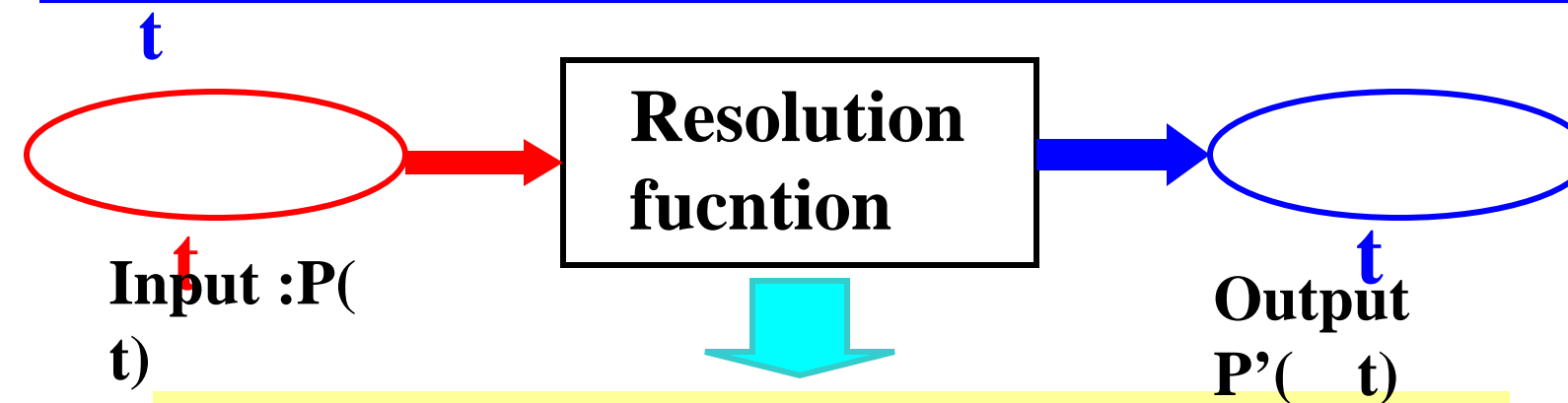
⇒ $A_{CP}(\Delta t) = -A_{fcp} \cos(\Delta m \Delta t) - S_{fcp} \sin(\Delta m \Delta t)$

Free Parameters

CP-fit : Resolution Function(1)

Most important work is define a Resolution Function of ' t'

Resolution Function = Response Function of



$$P'(\Delta t) = \int_{-\infty}^{\infty} P(\Delta t') R(\Delta t - \Delta t') d\Delta t'$$

$R(\Delta t - \Delta t')$ **Resolution Function**

CP-fit : Resolution Function(2)

P(Δt) include Resolution Function

Signal Probability Density Function

$$P_{sig}^{q(=\pm 1)}(\Delta t) = \frac{1}{4\tau_{B^0}} e^{-\frac{|\Delta t|}{\tau_{B^0}}} \left\{ 1 + q \cdot (1 - 2w) \cdot \left(A_{f_{cp}} \cos(\Delta m \Delta t) + S_{f_{cp}} \sin(\Delta m \Delta t) \right) \right\}$$

Background (qq) Probability Density Function

$$P_{q\bar{q}}(\Delta t) = \frac{1 + q\delta_{bg}}{2} \left\{ \frac{f_\tau}{2\tau_{bg}} e^{-\frac{|\Delta t|}{\tau_{bg}}} + (1 - f_\tau)\delta(\Delta t) \right\}$$

Proper time difference include resolution function

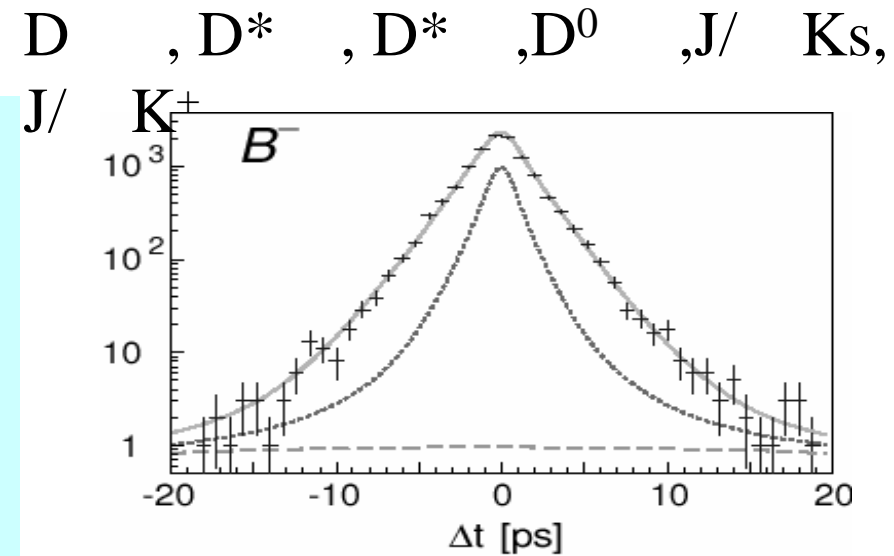
$$P(\Delta t) = (1 - f_{ol}) \int_{-\infty}^{+\infty} \left\{ f_{sig} P_{sig}(\Delta t') R_{sig}(\Delta t - \Delta t') + f_{q\bar{q}} P_{q\bar{q}}(\Delta t') R_{q\bar{q}}(\Delta t - \Delta t') \right\} d\Delta t' + f_{ol} P_{ol}(\Delta t)$$

CP-fit : Resolution Function(3)

Component of Resolution Function

- (1) Detector Resolution
- (2) Secondary Particle effect
- (3) Kinematic Approximation

In Belle, Resolution Function
Parameters are defined by B^0
Lifetime Fitting by Unbinned
Maximum likelihood fit used
Control Sample.



$$\tau_{B^0} = \text{????} \pm \text{????} \pm \text{????}$$