Higgs が見えなくなる理論的可能性

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Introduction



At LHC, we have a good chance to discover Higgs boson!

SM Higgs boson search at LHC

SM Higgs production at LHC....



SM Higgs decay



SM Higgs decay



For $m_H < 160 \text{ GeV}$, Higgs decay width is very small. $(\Gamma_Z = 2.4952 \text{ GeV}, \ \Gamma_W = 2.141 \text{ GeV})$ new physics can easily change the decay branching ratios

LHC experiments have a great potential to discover a SM Higgs boson in various channels.



SM Higgsの発見は確実

Non Standard Model Higgs を考える理由

★ SM Higgs boson has a problem (Naturalness problem)

SM Higgs boson mass term receives large radiative corrections.



Why is electroweak scale so small? There is no symmetry (mechanism) which guarantees the small Higgs mass in the SM.

New Physics contribution to Higgs mass term may cancel the large corrections.



Higgs boson has new interactions with new particles.

new particles

When we introduce
such a new physics...h
th
th
th
t

 Higgs sector may be modified. Higgs can mix with other state.

 e.g. MSSM is a two Higgs doublet model Interactions with SM particles can be modified

 Higgs has new interactions with new particles Higgs may decay into new particles Higgs may decay into new particles Γ(h→ bb̄) ≪ Γ(h→ XX) The decay branching ratios can be changed gluon fusion (decay to photons) is modified



★current SM Higgs mass limits





★ Higgs-like events at around 98 GeV at LEP



This result may be indicating the nonstandard model Higgs boson ?!....

Higgs が見えなくなる可能性は あるのか?

• Higgs が他のスカラーとミックスする

dimension 2 operator $H^{\dagger}H$ is a gauge singlet $\mathcal{L} = -\mathcal{O}H^{\dagger}H$ $\mathcal{O} = N^{\dagger}N$: singlet in NMSSM $\mathcal{O} = R(g_{\mathrm{ind}})$:Ricci scalar of 4d metric in RS model "Higgs-radion mixing"

Higgs interactions with SM particles can be suppressed

• Higgs がSM particle以外の粒子にdecayする $\Gamma(h \rightarrow b\overline{b}) \ll \Gamma(h \rightarrow XX)$

Higgs decay branching ratios to SM particles can be reduced

• gluon fusionやtwo photon decayがsuppress される





- Higgs が他のスカラーとミックスする
- Higgs がSM particle以外の粒子にdecayする
- gluon fusionやtwo photon decayがsuppress される

SMで期待されるシグナルイベント数 ($\sigma \times BR$) が大幅に小さくなるとHiggsが見えなく (少なくとも見えづらく)なる可能性

例えば、シグナルの $\sigma \times BR$ がI/3になったとすれば、発見に必要なルミノシティーは単純には $3^2 = 9$ 倍必要になる $(30 \text{ fb}^{-1} \rightarrow 30 \times 9 = 270 \text{ fb}^{-1})$

Significance = $\frac{S}{\sqrt{B}} = \frac{\sigma_{\text{signal}}}{\sqrt{\sigma_{bkgd}}}\sqrt{\mathcal{L}}$

S: number of signal event B: number of background L: integrated luminosity



Introduction

Higgsが見えにくくなる可能性

I. Suppression of gluon fusion in Little Higgs models (and SUSY models)

by Chen, Tobe and Yuan, and more.....

- 2. Nonstandard Higgs boson decays in NMSSM by Dermisek, Gunion, and more...
- 3. Radion-Higgs mixing in Randall-Sundrum model by Guidice, Rattazzi, Wells,

Hewett, Rizzo,

Dominici, Grzadkowski, Gunion, Toharia, and more....

Light Higgs scenario in MSSM

by Belyaev et al, and more

Summary

Little Higgs mechanism (collective symmetry breaking)

- Higgs boson is a pseudo Nambu-Goldstone boson which is light because of approximate global symmetries. Georgi and Kaplan
- Global symmetries are broken explicitly by two sets of interactions.





The production cross section can be significantly suppressed

For example: SUSY (benchmarks) vs. little Higgs model



R: nomalized by the SM prediction

Higgs discovery may need more luminosity, but....



When the new physics contribution is large, the new particle (T in Little Higgs case) should be within the reach at LHC.

Heavy T search at LHC

Matsumoto-san's talk(?)

2. Nonstandard Higgs boson decays in NMSSM by Dermisek, Gunion Little hierarchy problem in minimal supersymmetric model (MSSM) LEP limit on SM Higgs mass $m_H > 114 \text{ GeV}$ MSSM Higgs mass prediction $m_{H}^{2} \simeq M_{Z}^{2} \cos^{2}\beta + \frac{3G_{F}m_{t}^{4}}{\sqrt{2}\pi^{2}} \left\{ \log \frac{m_{\tilde{t}}^{2}}{m_{t}^{2}} + \frac{A_{t}^{2}}{m_{\tilde{t}}^{2}} \left(1 - \frac{A_{t}^{2}}{12m_{\tilde{t}}^{2}} \right) \right\}$ To satisfy $m_H > 114 \text{ GeV}$ typically $m_{\tilde{t}} > 1$ TeV for $A_t/m_{\tilde{t}} \ll 1$ On the other hand, EW breaking condition requires $\frac{M_Z^2}{2} \simeq -\mu^2 - m_{H_u}^2 \sim m_{\tilde{t}}^2 + \cdots$ assuming some universality at GUT scale

need some tuning for the EW scale

One of the solutions may be

- If the LEP Higgs limit is $m_H \sim 100 \text{ GeV}$ $m_{\tilde{t}} > 300 \text{ GeV} (110 \text{ GeV}) \text{ for } \tan \beta = 5, \ A_t/m_{\tilde{t}} = 0 \ (\sqrt{3})$ no serious fine-tuning
- $m_H \sim 100~{\rm GeV}$ is totally consistent with EW precision measurements
- it is possible to explain "LEP Higgs excess" at 98 GeV e^+ Z_{max} $Z_{h} \rightarrow b\bar{b}$
 - all Higgs interactions to the SM particles are SM-like, but $~{\rm BR}(h\to b\bar{b})\sim 0.1$

This is possible if the Higgs has other decay mode.

$h \rightarrow aa$ in Next to Minimal Supersymmetric Model (NMSSM, that is, MSSM + singlet)

$$W = \lambda S H_u H_d + \frac{\kappa}{3} S^3$$

(h: SM like Higgs, a: CP - odd Higgs coming mostly from the singlet)

Since hbb coupling is so small, $h \rightarrow aa$ can be easily a dominant decay mode.

If dominant decay mode of a is $a \rightarrow b\bar{b}$, LEP limit $m_H > 110 \text{ GeV}$ When the mass of a is below $b\bar{b}$ threshold, the dominant decay mode will be $\tau^+\tau^-$ or 2 jets LEP limit $m_H > 86 \text{ GeV}$

m_{h_1}/m_{a_1}	Branching Ratios			$n_{\rm obs}/n_{\rm exp}$	s95	N_{SD}^{LHC}
(GeV)	$h_1 \to b\overline{b}$	$h_1 \rightarrow a_1 a_1$	$a_1 \to \tau \overline{\tau}$	units of 1σ		
98.0/2.6	0.062	0.926	0.000	2.25/1.72	2.79	1.2
100.0/9.3	0.075	0.910	0.852	1.98/1.88	2.40	1.5
100.2/3.1	0.141	0.832	0.000	2.26/2.78	1.31	2.5
102.0/7.3	0.095	0.887	0.923	1.44/2.08	1.58	1.6
102.2/3.6	0.177	0.789	0.814	1.80/3.12	1.03	3.3
102.4/9.0	0.173	0.793	0.875	1.79/3.03	1.07	3.6
102.5/5.4	0.128	0.848	0.938	1.64/2.46	1.24	2.4
105.0/5.3	0.062	0.926	0.938	1.11/1.52	2.74	1.2

Dermisek, Gunion PRD73, 111701 (2006)

TABLE I: Some properties of the h_1 and a_1 for the eight allowed points with F < 10 and $m_{a_1} < 2m_b$ from our $\tan \beta = 10$, $M_{1,2,3}(m_Z) = 100, 200, 300$ GeV NMSSM scan. The n_{obs} , n_{exp} and s95 values are obtained after full processing of all Zh final states using the preliminary LHWG analysis code (thanks to P. Bechtle). See text for details. N_{SD}^{LHC} is the statistical significance of the best "standard" LHC Higgs detection channel for integrated luminosity of L = 300 fb⁻¹.

SM particlesへのBRが抑制されるので、"Standard" LHC Higgs detection channelのStatistical significanceが大きく減ってしまう。

Search for $h \to aa\,$ at LHC

Cheung, Song, Yan (2007) $h \rightarrow aa \rightarrow bbbb$ case Carena, Han, Huang, Wagner (2007) $Wh \rightarrow 4jl\nu$ requiring three or four b-tagged jets For a 120 GeV Higgs, 5σ discovery at the LHC requires about $30~{
m fb}^{-1}$ (b-tagging efficiencies of 50 % at $p_T \sim 15 \text{ GeV}$) If this efficiency only hold for $p_T > 30 \text{ GeV}$ need 80 fb^{-1} for discovery $h \rightarrow aa \rightarrow \tau^+ \tau^- \tau^+ \tau^-$ case

 $WW \to h \to 4\tau$

"Studies of this mode have begun"

Chang, Dermisek, Gunion, Weiner (2008)

3. Radion-Higgs mixing in Randall-Sundrum model In the RS model, the background metric is defined by $ds^{2} = e^{-2kr_{c}|y|}\eta_{\mu\nu}dx^{\mu}dx^{\nu} - r_{c}^{2}dy^{2}$ This metric suggests two types of massless excitations described by $\eta_{\mu\nu} \rightarrow g_{\mu\nu}(x)$ graviton $r_c \rightarrow T(x)$ radion $ds^{2} = e^{-2k|y|T(x)}g_{\mu\nu}(x)dx^{\mu}dx^{\nu} - T^{2}(x)dy^{2}$ It is convenient to express the radion field in terms of a canonically normalized field φ $\varphi \equiv \Lambda_{\varphi} e^{-k\pi (T-r_c)}, \ \Lambda_{\varphi} \equiv \langle \varphi \rangle = \sqrt{\frac{24M^3}{k}} e^{-k\pi r_c}$

Goldberger and Wise

mechanism to stabilize T such that $k\pi r_c\sim 35$ which explains the hierarchy between weak and Planck scales

One consequence of the GW mechanism is that the radion should be somewhat lighter than the Kaluza-Klein modes of any bulk field.

The radion can mix with Higgs via

$$S = -\xi \int d^4x \sqrt{-g_{\rm ind}} R(g_{\rm ind}) H^{\dagger} H$$

R: Ricci scalar of the induced 4-d metric on the SM brane

This radion-Higgs mixing can change the Higgs phenomenology at the LHC.





gluon fusion can be small due to the top-loop and trace anomaly contributions. Higgs discovery in this channel will be difficult.

Higgs discovery vs. Radion discovery



Figure 15: The light grey (cyan) regions show the part of the (M_{ϕ}, ξ) parameter space where the significance of the Higgs boson discovery with $h \rightarrow \gamma\gamma$, tth $(h \rightarrow bb)$, $h \rightarrow ZZ^* \rightarrow 4\ell$, $h \rightarrow WW^* \rightarrow 2\ell$, qqh $(h \rightarrow \tau\tau)$ and Wh $(h \rightarrow \gamma\gamma)$ channels drops below 5σ . The regions inside thick (blue) curves are the ones where the significance of the $\phi \rightarrow ZZ^{(*)} \rightarrow 4\ell$ signal exceeds 5σ . The outermost contours define the theoretically allowed region. Results are present for $m_h=125 \text{ GeV}/c^2$, $\Lambda_{\phi} = 1 \text{ TeV}$ (a) and 2 TeV (b) and for 30 fb⁻¹.

 $\varphi \to hh \to \gamma\gamma + bb$

CMS NOTE-2005/007



Figure 14: The 5σ discovery contours for $\phi \to hh \to \gamma\gamma + b\bar{b}$ channel (m_{ϕ}=300 GeV/ c^2 , m_h=125 GeV/ c^2) with 30 fb⁻¹. In (a) the solid contour shows the discovery region for the renormalization and factorization scales $\mu_r = \mu_f = M_Z$. The dashed contours refer to $\mu_r = \mu_f = 0.5 M_Z$ and 2 M_Z. In (b) the solid (dashed) contours show the discovery region without (with) the effects of the systematic uncertainties for $\mu_r = \mu_f = M_Z$.

Higgs can be discoverd in $\varphi \rightarrow hh$ channel

Possibility of light MSSM Higgs bosons





•SM Higgs boson will be discovered at LHC if it exists.

• Non-SM Higgs can be realized in many well-motivated models

★ Gluon-fusion (and/or diphoton decay) of Higgs can be affected by the mechanism to solve the hierarchy problem

Little Higgs models and some SUSY models

★ non-SM Higgs decay can change the Higgs branching ratios to SM particles $h \rightarrow aa$ in NMSSM

Higgs mixing to other scalar can reduce the interactions to SM particles Higgs-radion mixing

Light MSSM Higgs scenario

reduction of Higgs signal rate

Non-standard Higgs discovery channels may need to be studied to discover Higgs boson!

backup slides

Collective symmetry breaking

Gauge symmetries $[SU(2) \times U(1)]_1 \times [SU(2) \times U(1)]_2$

are embedded in global SU(5)

$$Q_{SU(2)_{1}}^{a} = \begin{pmatrix} \sigma^{a}/2 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \qquad Y_{1} = \frac{1}{10} \begin{pmatrix} 3 & & & & \\ & 3 & & & \\ & & -2 & & \\ & & & -2 \end{pmatrix} \Rightarrow \text{preserve SU(3)}$$
$$Q_{SU(2)_{2}}^{a} = \begin{pmatrix} 0 & 0 & & & \\ 0 & 0 & & 0 & \\ 0 & 0 & & -\sigma^{a*}/2 \end{pmatrix} \qquad Y_{2} = \frac{1}{10} \begin{pmatrix} 2 & & & & \\ & 2 & & & \\ & & & -3 & & \\ & & & & -3 \end{pmatrix} \Rightarrow \text{preserve SU(3)}$$

Either SU(3) is enough to keep Higgs massless.

Sum of all gauge interactions break both SU(3)s and generate the Higgs mass.

 Λ^2 corrections are canceled.

★ Top sector

The largest quadratically divergent one-loop contribution to the Higgs mass parameter in the SM comes from the top quark loop. Thus the top sector has to be modified to cancel the large divergence.

Introducing a pair of weak-singlet Weyl fermions U_L and U_R and making the SU(3) triplet from the doublet $q_L = (u_L, d_L)^T$ and the singlet U_L : $Q_L = \begin{pmatrix} -\sigma_2 q_L \\ U_L \end{pmatrix}$

the Top Yukawa sector is given by

$$\mathcal{L} = -\frac{\lambda_1}{2} f \epsilon^{ijk} \epsilon^{xy} \bar{Q}_{Li} \Sigma_{jx} \Sigma_{ky} u_R - \lambda_2 f \bar{U}_L U_R + \text{h.c.}$$

collective symmetry breaking in the top sector

$$\mathcal{L} = -\frac{\lambda_1}{2} f \epsilon^{ijk} \epsilon^{xy} \bar{Q}_{Li} \Sigma_{jx} \Sigma_{ky} u_R - \lambda_2 f \bar{U}_L U_R + \text{h.c.}$$

If λ_1 is zero,

the Higgs does not couple to the top sector, so that there is no corrections to the Higgs mass parameter from the top sector.

If λ_2 is zero,

the global SU(3) is unbroken in the top Yukawa sector, so the Higgs is an NGB.

Any contributions to the Higgs mass have to involve both λ_1 and λ_2 . The one loop contributions are at most logarithmically divergent.

$$\begin{split} m_t &= 174.3 \text{ GeV}, \quad M_{SUSY} = 350 \text{ GeV}, \quad \mu = 300 \text{ GeV}, \quad M_2 = 300 \text{ GeV}, \\ X_t^{\text{OS}} &= -750 \text{ GeV} \text{ (FD calculation)}, \quad X_t^{\overline{\text{MS}}} = -770 \text{ GeV} \text{ (RG calculation)} \\ A_b &= A_t, \quad m_{\tilde{g}} = 500 \text{ GeV} \text{ .} \end{split}$$



Figure 3: $[\sigma \times BR]_{MSSM}/[\sigma \times BR]_{SM}$ is shown for the channels $gg \to h \to \gamma\gamma$ (left plot) and $t\bar{t} \to t\bar{t}h \to t\bar{t}b\bar{b}$ (right plot) in the $M_A - \tan\beta$ -plane for the gluophobic Higgs scenario. The white-dotted area is excluded by LEP Higgs searches.

(5)

Higgs total decay width normalized by the SM value



Higgs decay branching ratios, normalized by the SM values



In Case B, because of the largely reduced total decay width in small Higgs mass region, some of the Higgs boson decay branching ratios are increased.

$$R_{\sigma(X)} = \frac{\sigma^{\rm LH}(X)}{\sigma^{\rm SM}(X)} \qquad R_{\rm BR}(Y) = \frac{\rm BR^{\rm LH}(Y)}{\rm BR^{\rm SM}(Y)}$$

 $R_{\sigma(X)} \times R_{BR(Y)}$ for f = (600, 700, 1000) GeV

$m_h = 120 \text{ GeV}$	$R_{\mathrm{BR}(\gamma\gamma)}$	$R_{\mathrm{BR}(\tau\tau)}$	$R_{\mathrm{BR}(b\bar{b})}$	$R_{\mathrm{BR}(VV)}$	
$R_{\sigma(gg)}$ (Case A)	0.57, 0.68, 0.84	0.56, 0.67, 0.83	_	0.55, 0.66, 0.83	
(Case B)	0.81, 0.86, 0.93	0.51, 0.63, 0.81	_	0.78, 0.84, 0.92	
$R_{\sigma(VV)}$ (Case A)	0.97, 0.98, 0.99	0.95, 0.96, 0.98	_	0.94, 0.96, 0.98	
(Case B)	1.34, 1.22, 1.09	0.84, 0.89, 0.95	_	1.30, 1.19, 1.08	
$R_{\sigma(t\bar{t}h)}$ (Case A)	_	0.87, 0.90, 0.95	0.87, 0.90, 0.95	_	
(Case B)	_	0.77, 0.83, 0.92	0.77, 0.83, 0.92	_	
$R_{\sigma(Vh)}$ (Case A)	0.97, 0.98, 0.99	_	0.95, 0.96, 0.98	—	
(Case B)	1.34, 1.22, 1.09		0.84, 0.89, 0.95		
$m_h = 200 \text{ GeV}$	$R_{\mathrm{BR}(\gamma\gamma)}$	$R_{\mathrm{BR}(\tau\tau)}$	$R_{\mathrm{BR}(b\bar{b})}$	$R_{\mathrm{BR}(VV)}$	
$R_{\sigma(gg)}$ (Case A)	_	_	_	0.55, 0.67, 0.83	
(Case B)	_	_		0.56, 0.67, 0.83	
$R_{\sigma(VV)}$ (Case A)	_	_	_	0.90, 0.94, 0.97	
(Case B)	_	_	_	0.90, 0.94, 0.97	

- Higgs production via gluon fusion is suppressed.
- $\gamma\gamma$, VV decay modes via weak boson fusion can be enhanced in small Higgs mass region in Case B.



FIG. 1: Br($\Upsilon \rightarrow \gamma a_1$) for NMSSM scenarios with various ranges for m_{a_1} : dark grey (blue) = $m_{a_1} < 2m_{\tau}$; medium grey (red) = $2m_{\tau} < m_{a_1} < 7.5$ GeV; light grey (green) = 7.5 GeV $< m_{a_1} < 8.8$ GeV; and black = 8.8 GeV $< m_{a_1} <$ 9.2 GeV. The plots are for tan $\beta = 10$ and $M_{1,2,3}(m_Z) =$ 100, 200, 300 GeV. The left plot comes from the A_{λ}, A_{κ} scan described in the text, holding $\mu_{\text{eff}}(m_Z) = 150$ GeV fixed. The right plot shows results for F < 15 scenarios with $m_{a_1} <$ 9.2 GeV found in a general scan over all NMSSM parameters holding tan β and $M_{1,2,3}$ fixed as stated.



Figure 2: $\sigma(\text{gg} \rightarrow \phi)$ (a) and $\text{Br}(\phi \rightarrow \text{hh})$ (b) as a function of the parameter ξ for two values of Λ_{ϕ} , 1 and 5 TeV. On the left plot the cross section of $\text{gg} \rightarrow \text{H}_{\text{SM}}$ process for the SM Higgs boson of 300 GeV/c² mass is also shown as the horizontal line.





Figure 3: Precision electroweak allowed [solid (red) regions] and disallowed regions (at 90% CL) of the radion mass as a function of Λ_{ϕ} , while holding fixed $m_h = 350 \text{ GeV}$ and $\xi = -1$. The masses of the Higgs and radion physical eigenstates can be greater than the SM Higgs boson precision electroweak 95% CL upper limit of 219 GeV. The thick (pink) dashed line to the right of the theoretically disallowed tower is the LHC contour for $r^h \equiv N_{SD}^h/N_{SD}^{SM} = 0.9$ – to the right of this contour $0.9 < r^h < 1$. The thick (blue) solid line to the left of the tower is the contour for $r^h = 1.1$ – above this contour $1 < r^h < 1.1$. Between the tower and the thinner dotted (cyan) line, $N_{SD}^{\phi} > 5$. See text for more details.

Light Higgs scenario (LHS) and "LEP excess" scenario







Higgs Production at hadron colliders



$hH^{+}/AH^{+} \text{ production at LHC}$ $\sin(\beta - \alpha) \qquad \cos(\beta - \alpha)$ $\approx V - WZ \qquad \approx W^{\pm} \qquad A \qquad \swarrow$

 $-\frac{h}{V} = W, Z$





suppressed in LHS

enhanced in LHS





Since all MSSM Higgs bosons are not heavy in LHS, this production can be sizable at LHC.

AH^+ production rate

PLB530,188 (hep-ph/0112165): Kanemura, Yuan PRD69,075008(hep-ph/0311083): Cao, Kanemura, Yuan



• CP-odd Higgs is light (~100 GeV), the production cross section is big at LHC.

• In addition to AH+ mode, we have hH+ mode in our LHS.

Signature rate at Tevatron and LHC

 $pp(p\bar{p}) \rightarrow H^{*} h(A) \rightarrow \tau^{*} \nu \ b\bar{b} \rightarrow \pi^{*} \ \bar{\nu} \ \nu b\bar{b}$ rates in fb



Signal process



SM background

$$\begin{split} Wb\bar{b} \ : \ qq' &\rightarrow b\bar{b}W^+, W^+ \rightarrow \tau^+\nu, \tau^+ \rightarrow \pi^+\bar{\nu}, \\ t\bar{b} \ : \ qq' \rightarrow W^* \rightarrow t\bar{b}, t \rightarrow bW^+, W^+ \rightarrow \tau^+\nu, \tau^+ \rightarrow \pi^+\bar{\nu}, \\ WZ \ : \ qq' \rightarrow W^+Z^0, Z^0 \rightarrow b\bar{b}, W^+ \rightarrow \tau^+\nu, \tau^+ \rightarrow \pi^+\bar{\nu}. \\ Wg \ : \ qg \rightarrow q't\bar{b}, t \rightarrow W^+b, W^+ \rightarrow \tau^+\nu, \tau^+ \rightarrow \pi^+\bar{\nu}, \\ t\bar{t} \ : \ qq(gg) \rightarrow t\bar{t}, t \rightarrow W^+b, W^+ \rightarrow \tau^+\nu, \tau^+ \rightarrow \pi^+\bar{\nu}, \bar{t} \rightarrow \bar{b}W^- \end{split}$$

Effect of cuts

TABLE II: Numbers of AH^+ signal and background events for the sample point in the $b\bar{b}\pi^+ \not\!\!\!E_T$ channel at the LHC with an integrated luminosity of 100 fb⁻¹. The *b*-tagged efficiency defined in Eq. 55 is included and the kinematics cuts listed in each column are applied sequentially.

	Basic cut	$\not\!\!\!E_T > 50 \mathrm{GeV}$	$p_T^{\pi} > 40 \mathrm{GeV}$	$ m_{b\bar{b}} - m_A < 10 \mathrm{GeV}$	$m_T > 80 \mathrm{GeV}$
AH^+	214	169	107	103	40
hH^+	259	199	122	1	0
$W b ar{b}$	3765	1229	394	30	2
WZ	361	128	40	10	1
$tar{b}$	778	387	106	8	0
Wg	298	153	43	2	0
$t\bar{t}$	50	37	8	1	0
Signal (S)	214	169	107	103	40
Background (B)	5511	2133	713	52	3
S/B	0.04	0.08	0.15	1.98	13.33
S/\sqrt{B}	2.88	3.66	4.01	14.28	23.09

Basic cuts

 $p_T(b, \overline{b}, \pi^+) > 15 \text{ GeV}, \ |\eta(b, \overline{b}, \pi^+)| < 3.5,$

 $\Delta R > 0.4$ between any two observable final state partons

 $\Delta R \ (\equiv \sqrt{(\Delta \phi)^2 + (\Delta \eta)^2})$ $\Delta \phi$ and $\Delta \eta$ are the separation in azimuthal angle and rapidity, respectively.

	Basic cut	$\not\!\!\!E_T > 50 \mathrm{GeV}$	$p_T^{\pi} > 40 \mathrm{GeV}$	$\left m_{b\bar{b}} - m_h\right < 10 \mathrm{GeV}$	$m_T > 80 \mathrm{GeV}$
hH^+	259	199	122	119	49
AH^+	214	169	107	1	0
$W b ar{b}$	3765	1229	394	39	3
$tar{b}$	778	387	106	8	0
Wg	298	153	43	4	0
$t \overline{t}$	50	37	8	1	1
WZ	361	128	40	9	1
Signal (S)	259	199	122	119	49
Background (B)	5466	2103	698	62	5
S/B	0.05	0.09	0.17	1.92	9.8
S/\sqrt{B}	3.50	4.34	4.62	15.11	21.9



FIG. 30: Distributions of invariant mass $m_{b\bar{b}}$ (after imposing the basic, E_T and p_T^{π} cuts) and transverse mass m_T (after imposing the basic, E_T , p_T^{π} and the Higgs mass window cuts): (b) AH^+ and (c) hH^+ . Here $m_T = \sqrt{2p_T^{\pi}E_T^{\text{mis}}(1-\cos\phi')}$

Significance contour of AH*/hH*



FIG. 32: Contours of the significance and event numbers of the AH^+/hH^+ processes at LHC after imposing the mass window cut (first row) and the transverse mass cut (second row) in the case of positive μ .

To reach 5-sigma significance, only 5-10 fb^-1 integrated luminosity is required!